

Lepton Flavor Violation at a High-Energy Muon Collider

[arXiv:2203.08825]

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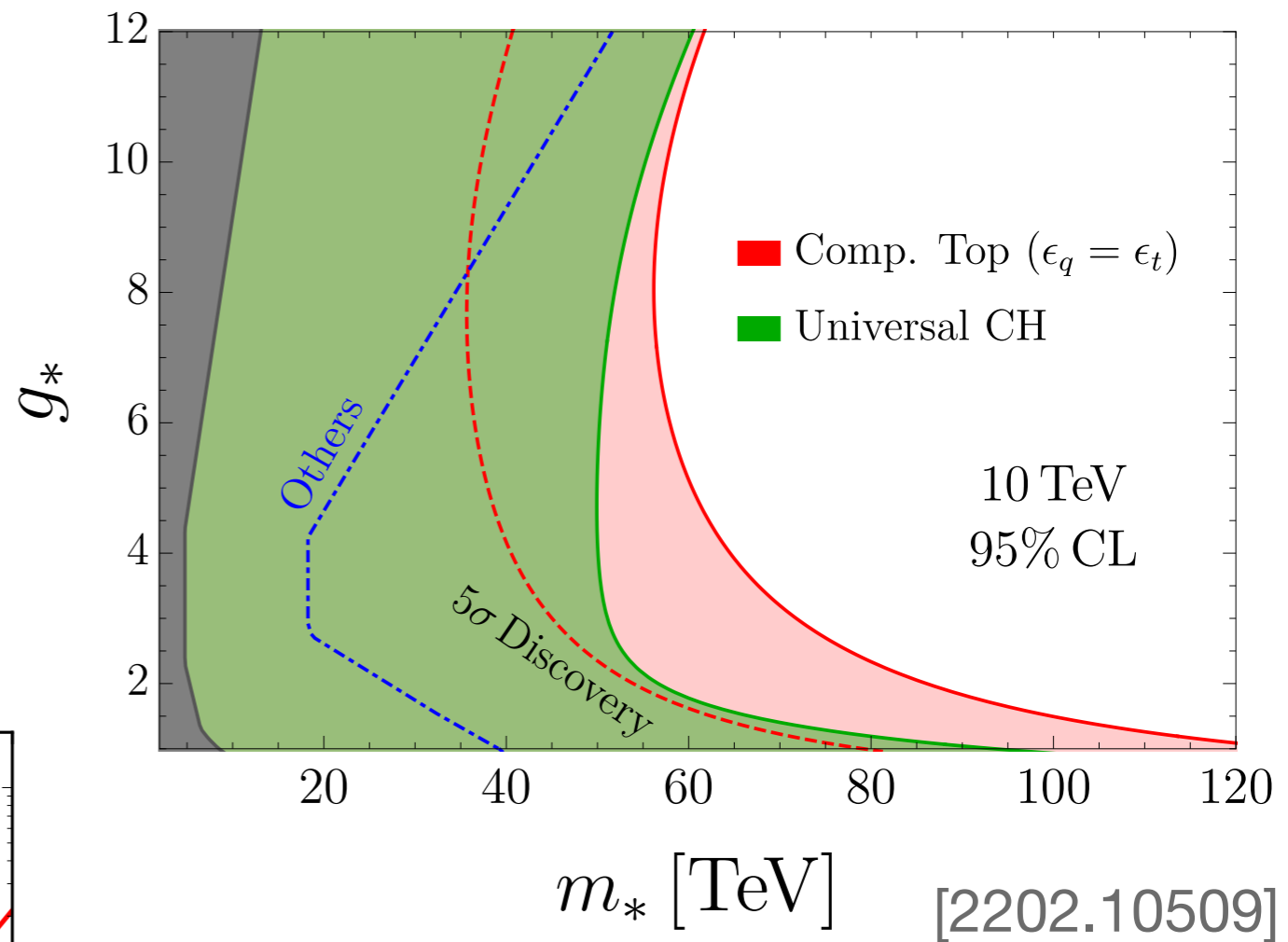
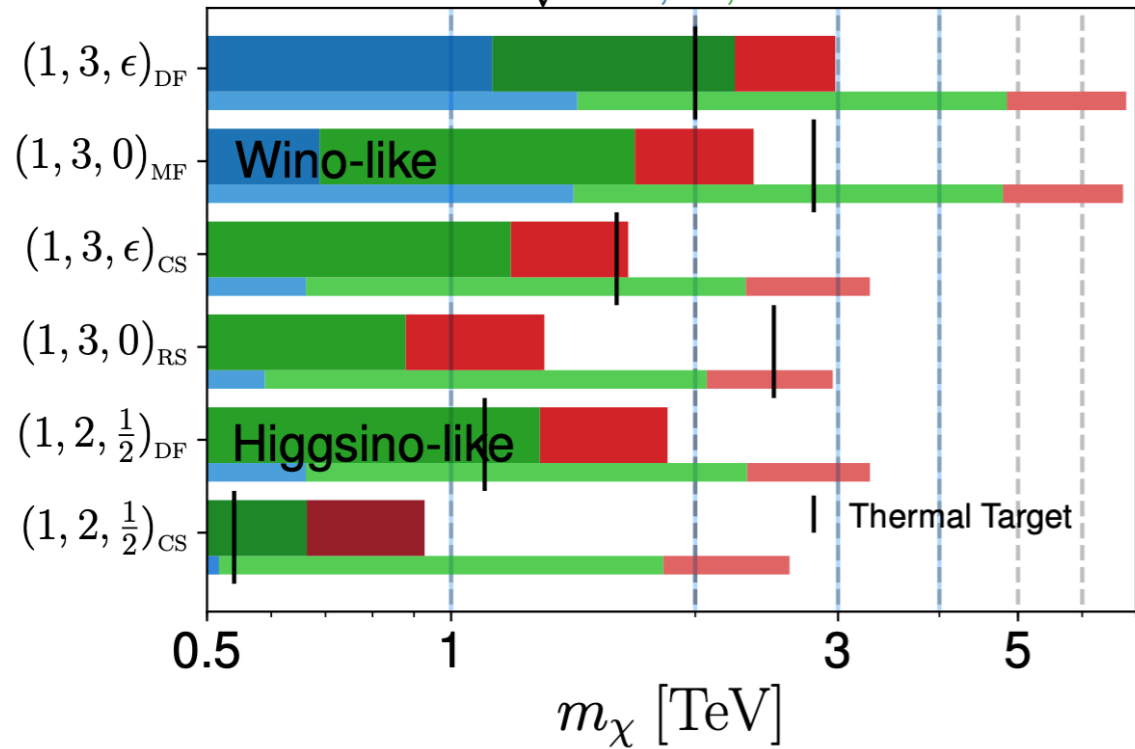
Pushing the Energy Frontier is Essential

Muon Colliders Can Extend Our Reach

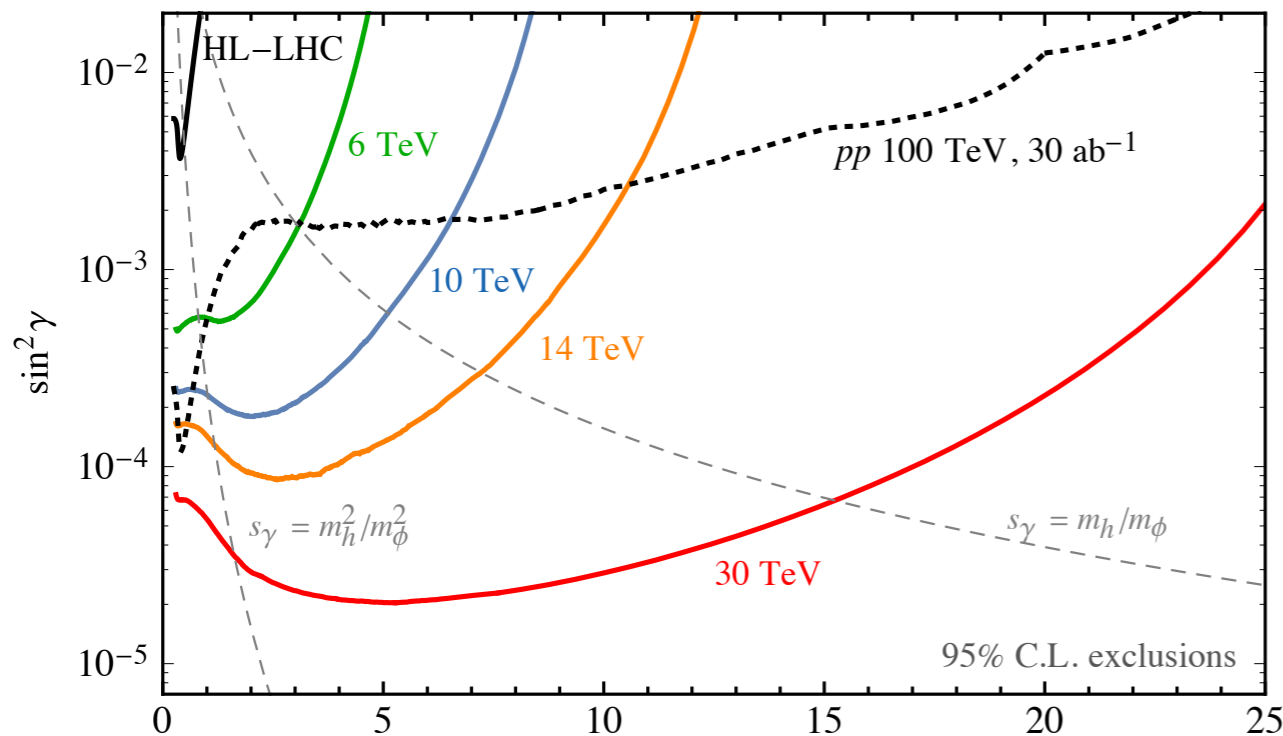
Electroweak DM 2σ reach

$\sqrt{s} = 3, 10, 14$ TeV

[2009.11287, 2203.07531]



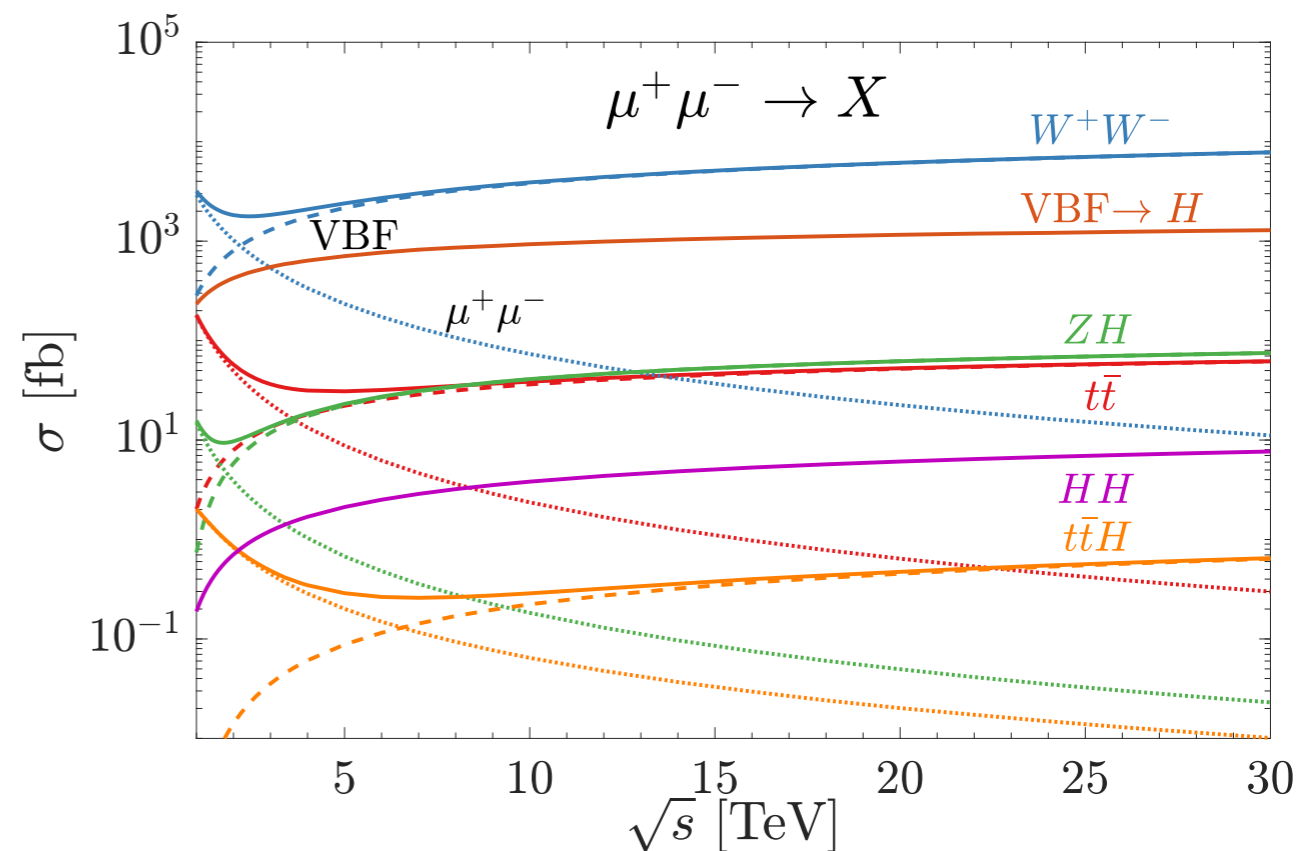
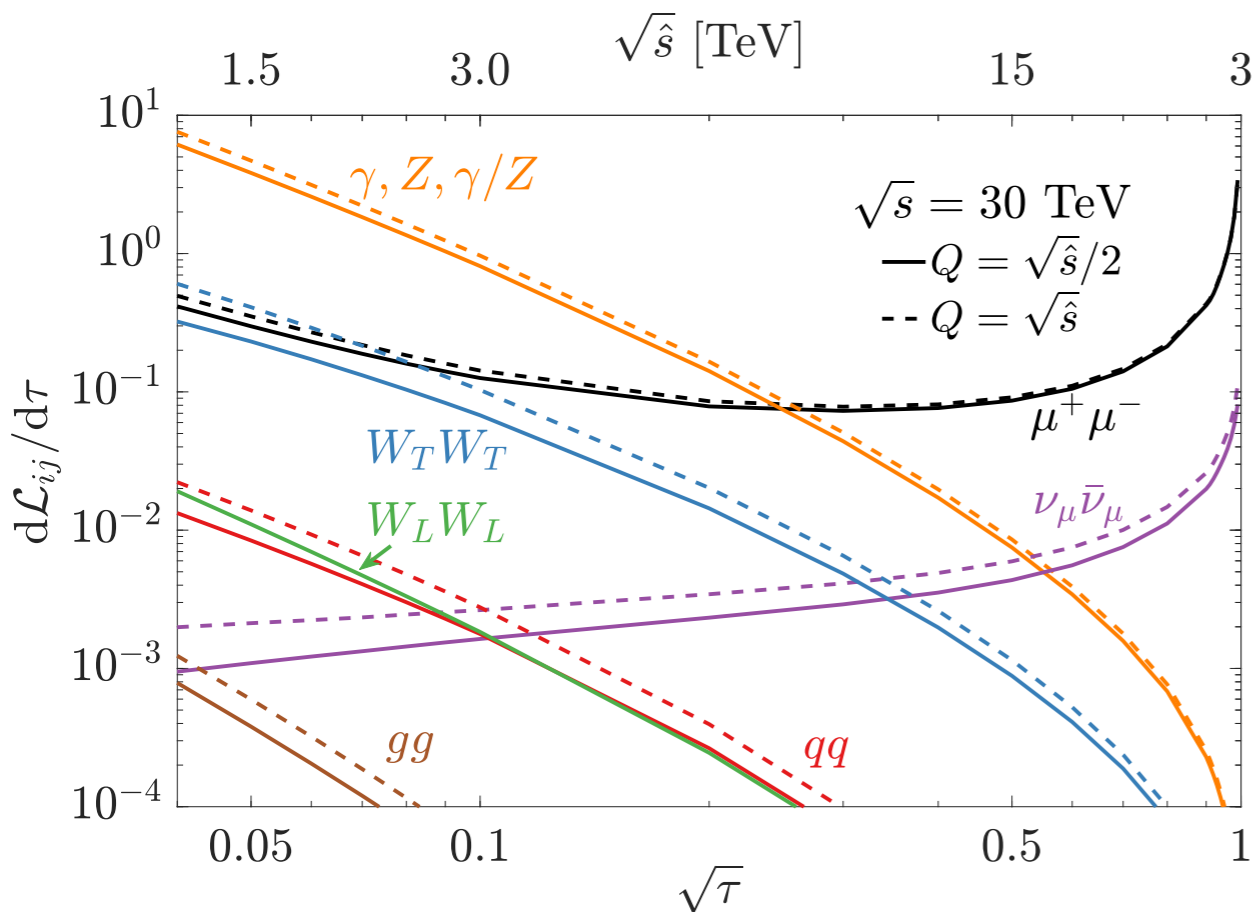
[2202.10509]



[2103.14043]

Muon Colliders Can Study the Higgs

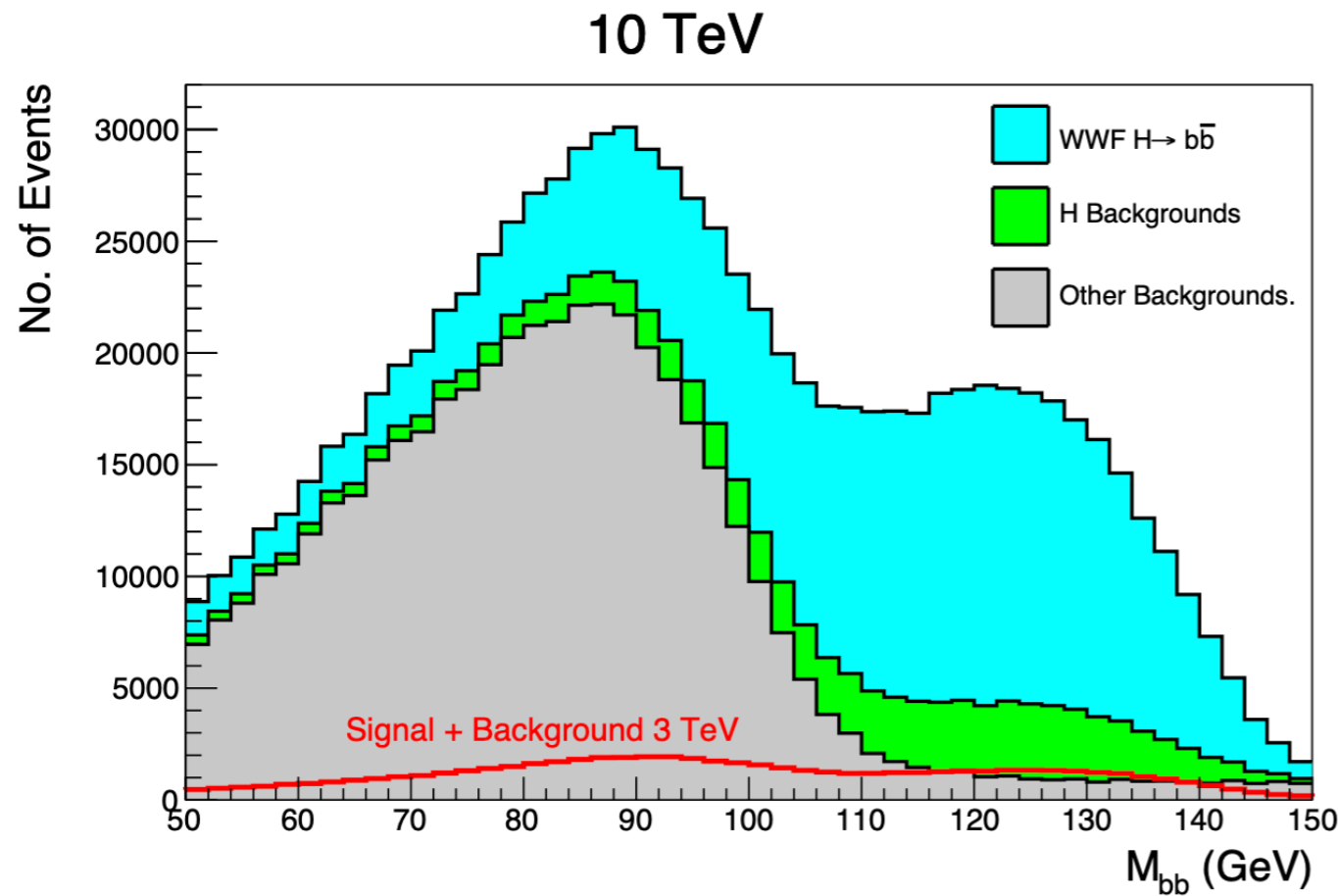
Han, Ma, Xie [2007.14300]



Large Higgs production rates from VBF in clean backgrounds

\implies precision measurements of the Higgs

Muon Colliders Can Study the Higgs

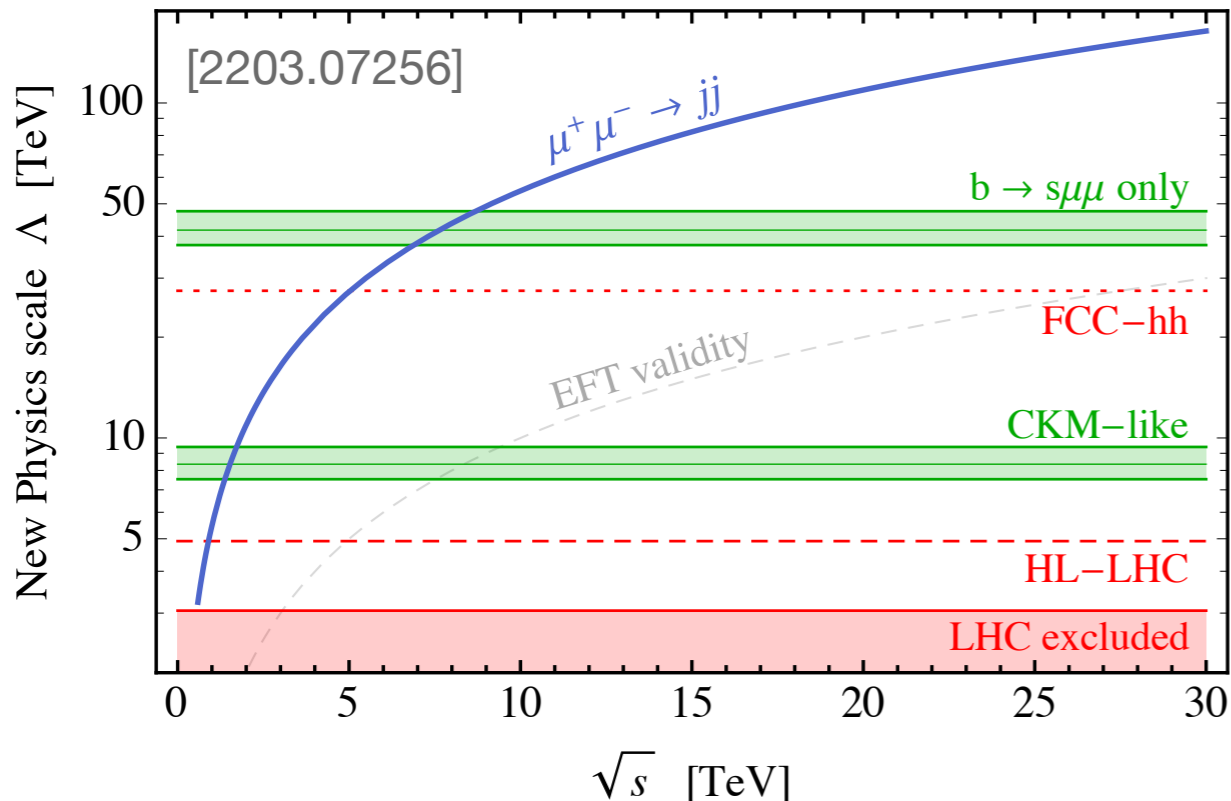
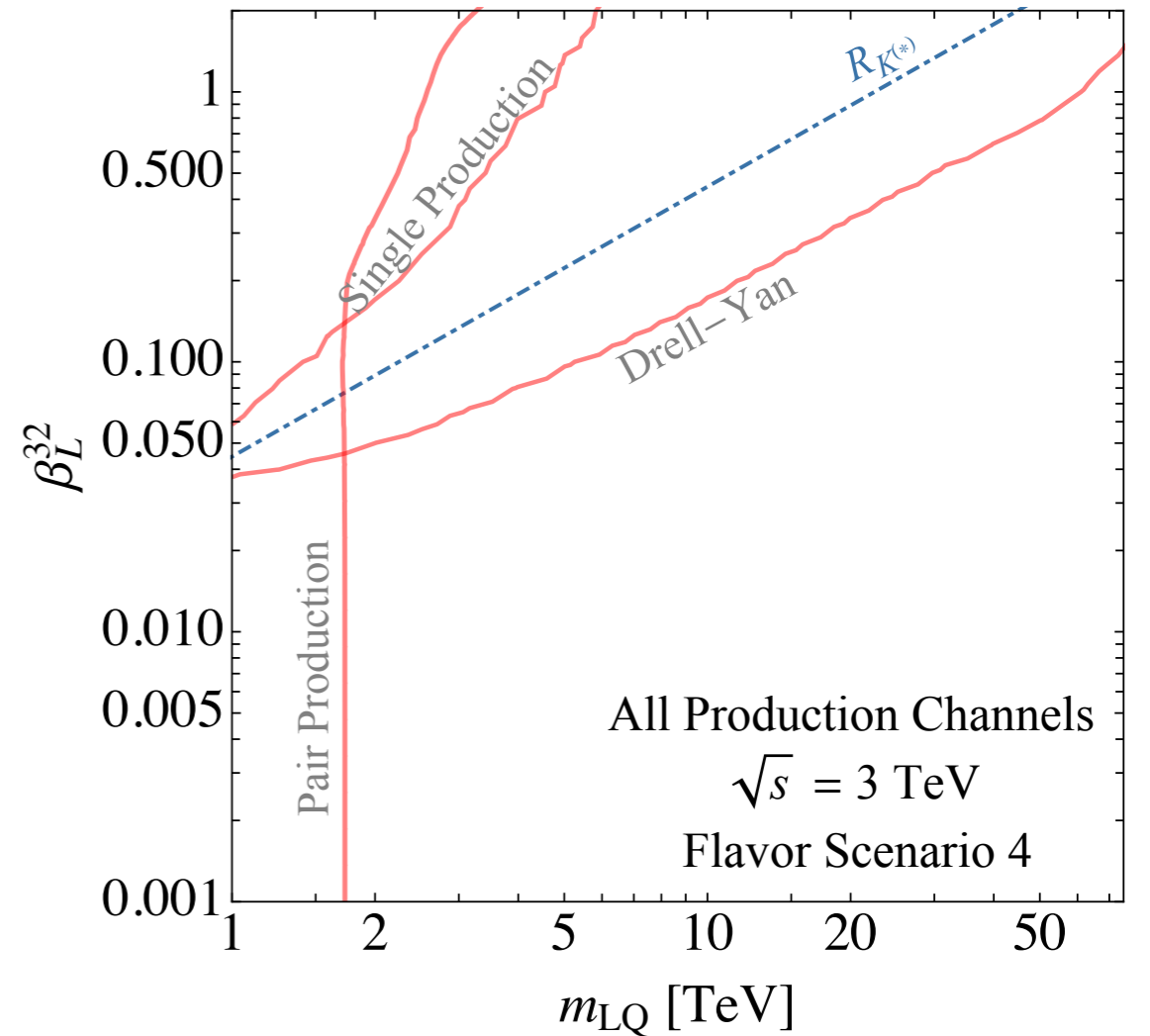
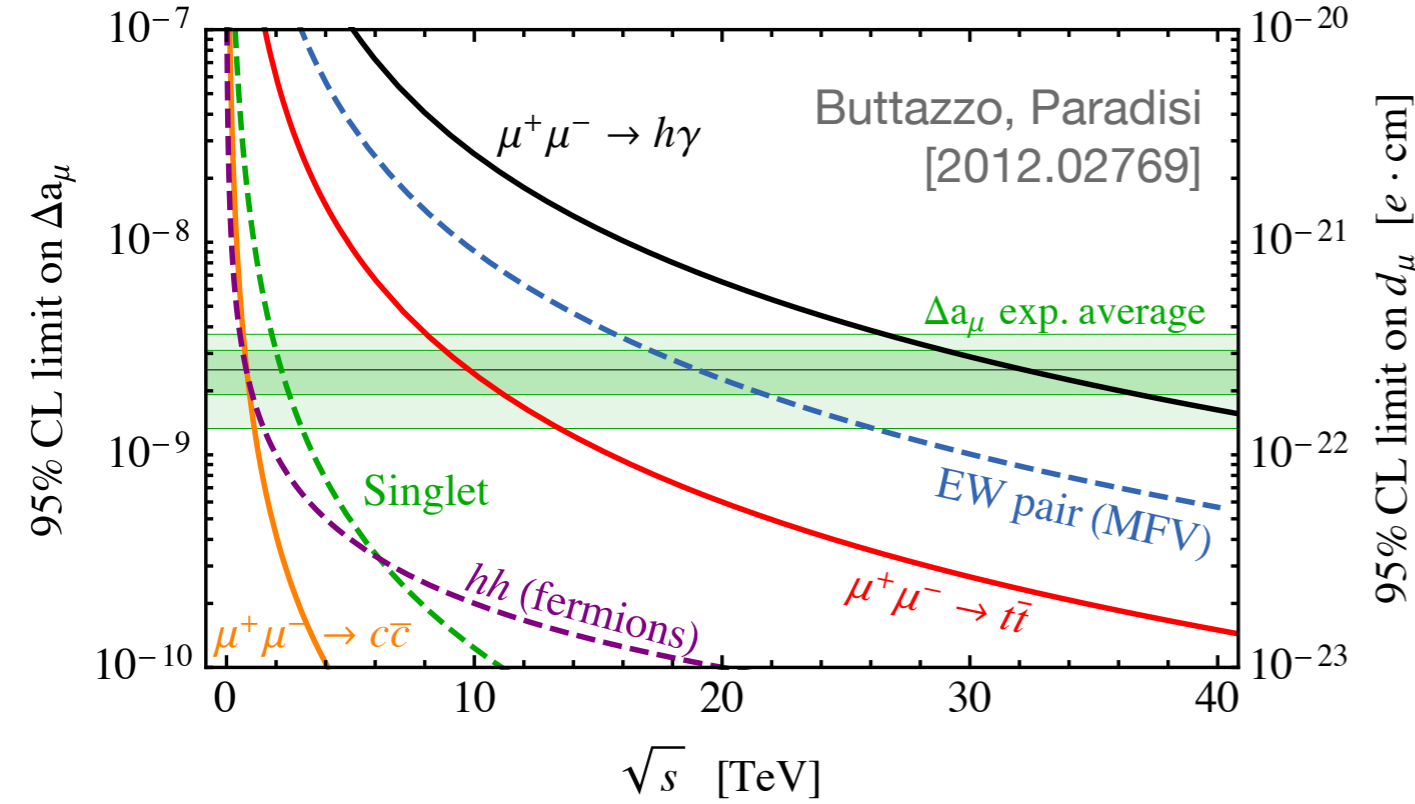


Forslund, Meade [2203.09425]

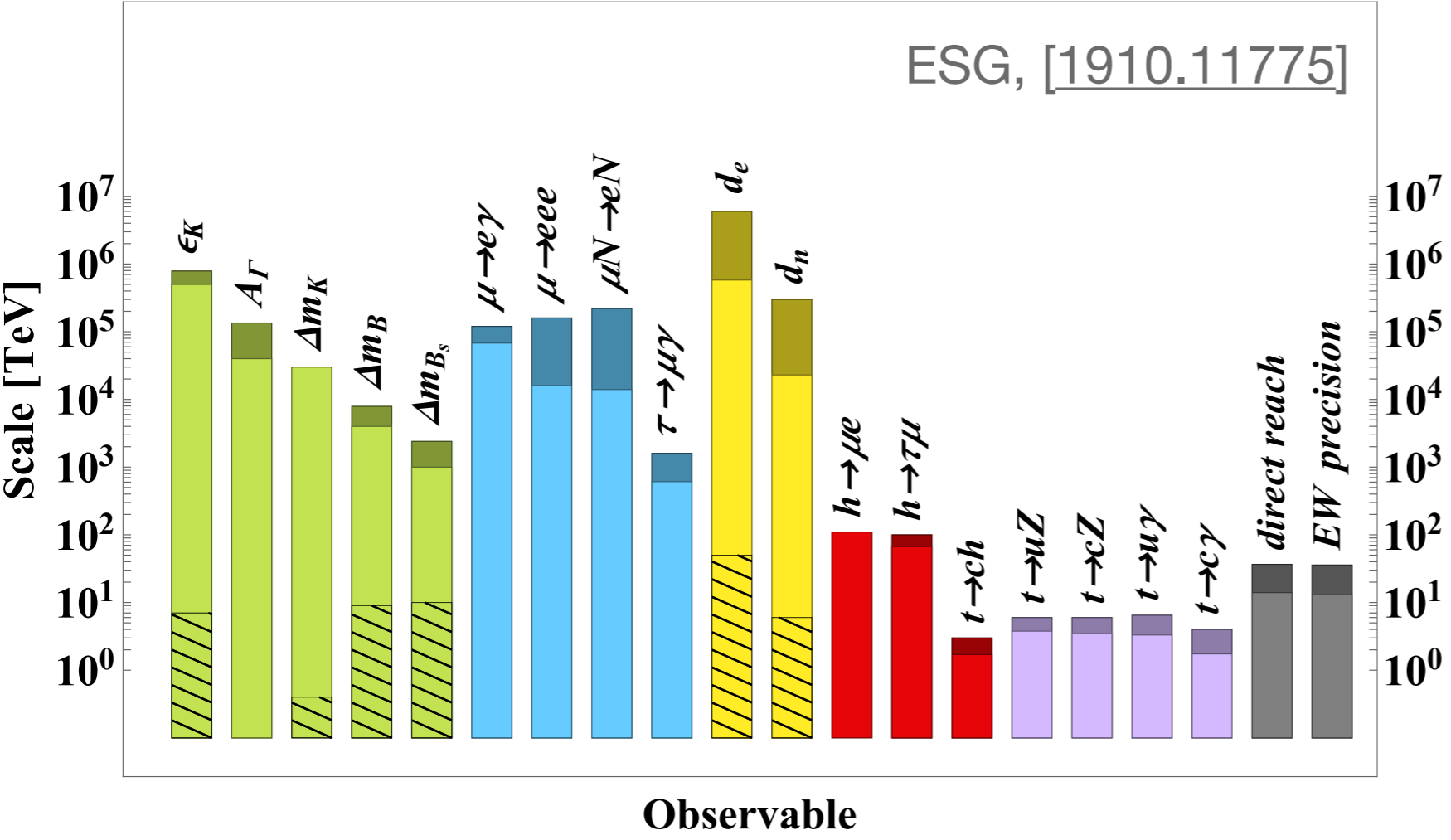
See also 2112.12507, 2203.04324,
2203.08874, ...

	$\mu^+\mu^-$	
	3 TeV	10 TeV
κ_W	0.44	0.13
κ_Z	1.3	0.40
κ_g	2.4	0.67
κ_γ	3.9	1.1
$\kappa_{Z\gamma}$	37	10
κ_c	7.5	2.3
κ_t	35	52
κ_b	0.96	0.27
κ_μ	22	5.4
κ_τ	2.5	0.71

Muon Colliders Have Unique Probes



Can (Flavorful) New Physics Be Nearby?



Flavor Anarchy is Too Pessimistic!

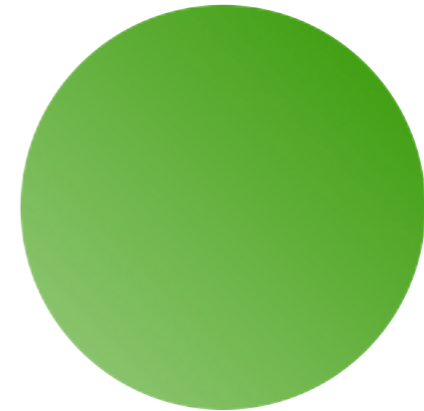
The only theory we've observed certainly doesn't look anarchic:



$$m_e = 0.511 \text{ MeV}$$



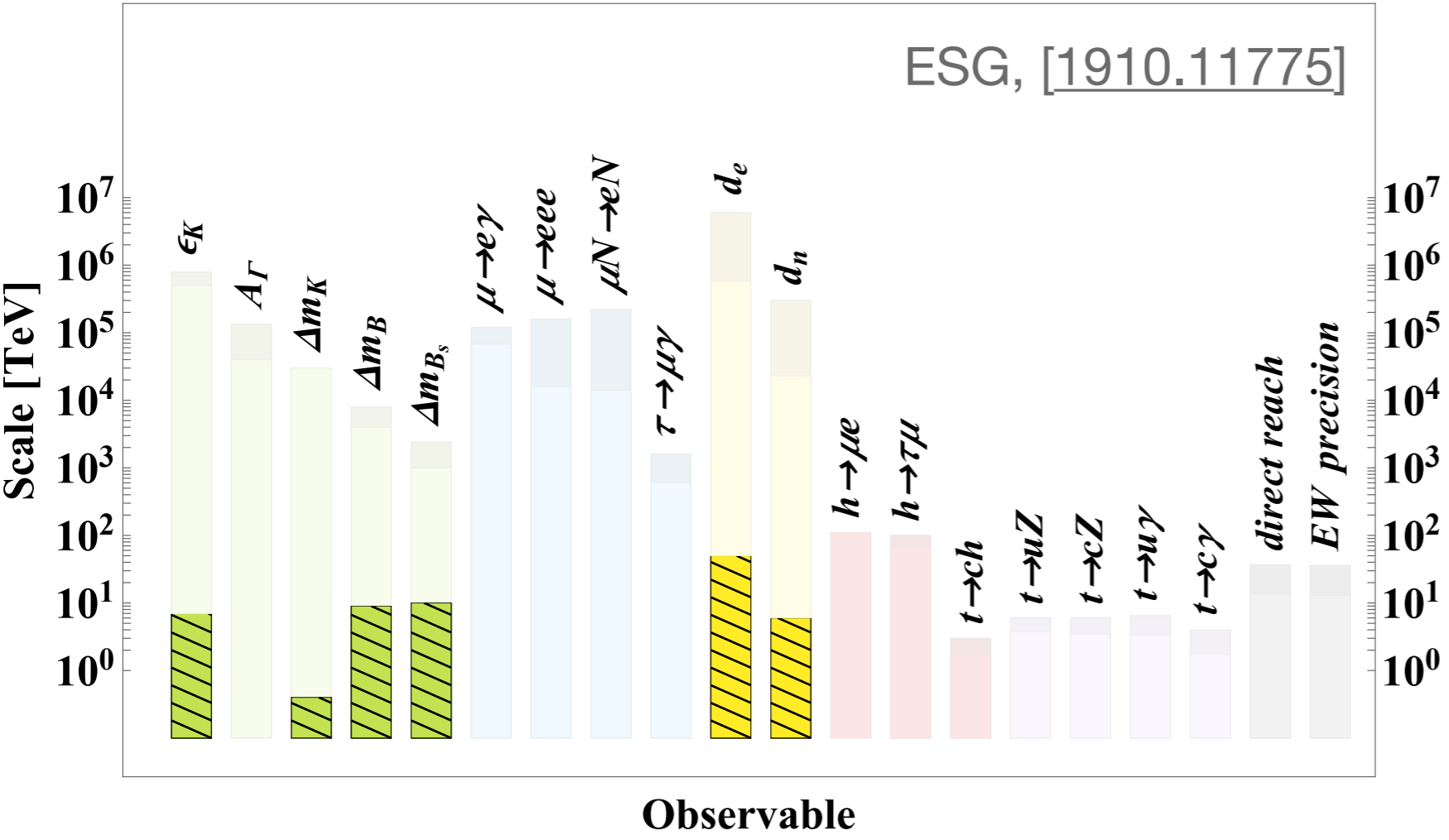
$$m_\mu = 105.7 \text{ MeV}$$



$$m_\tau = 1776.9 \text{ MeV}$$

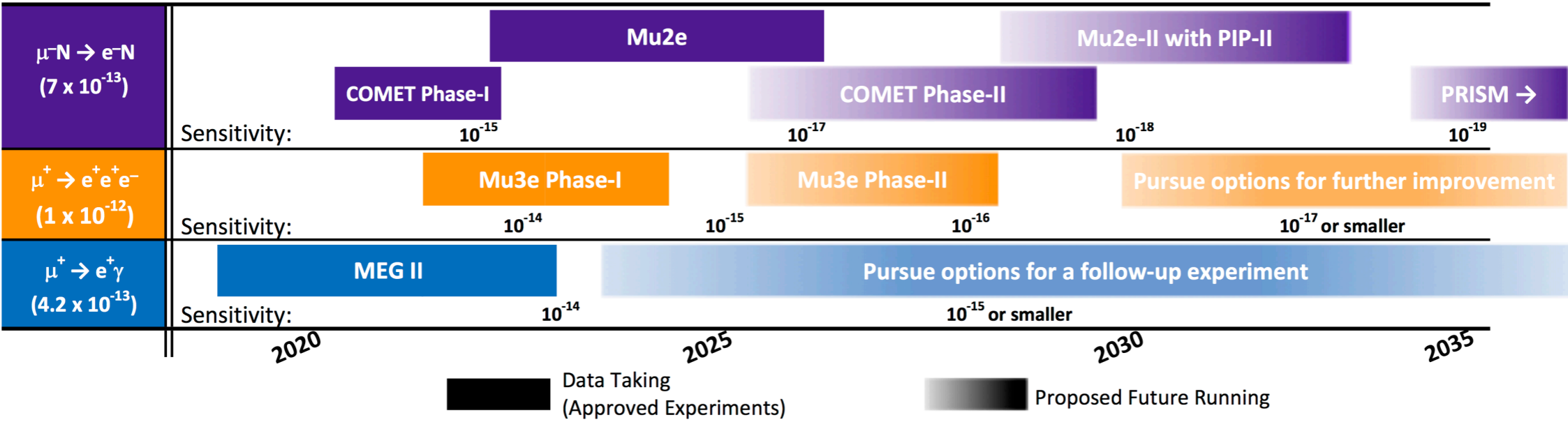
$$|V_{\text{CKM}}| = \begin{pmatrix} 0.974 & 0.225 & 0.0037 \\ -0.225 & 0.973 & 0.042 \\ 0.0087 & -0.041 & 0.999 \end{pmatrix} \sim \begin{pmatrix} 1 - \frac{1}{2}\lambda^2 & \lambda & \lambda^3 \\ -\lambda & 1 - \frac{1}{2}\lambda^2 & \lambda^2 \\ \lambda^3 & -\lambda^2 & 1 \end{pmatrix}$$

Flavor Anarchy is Too Pessimistic!

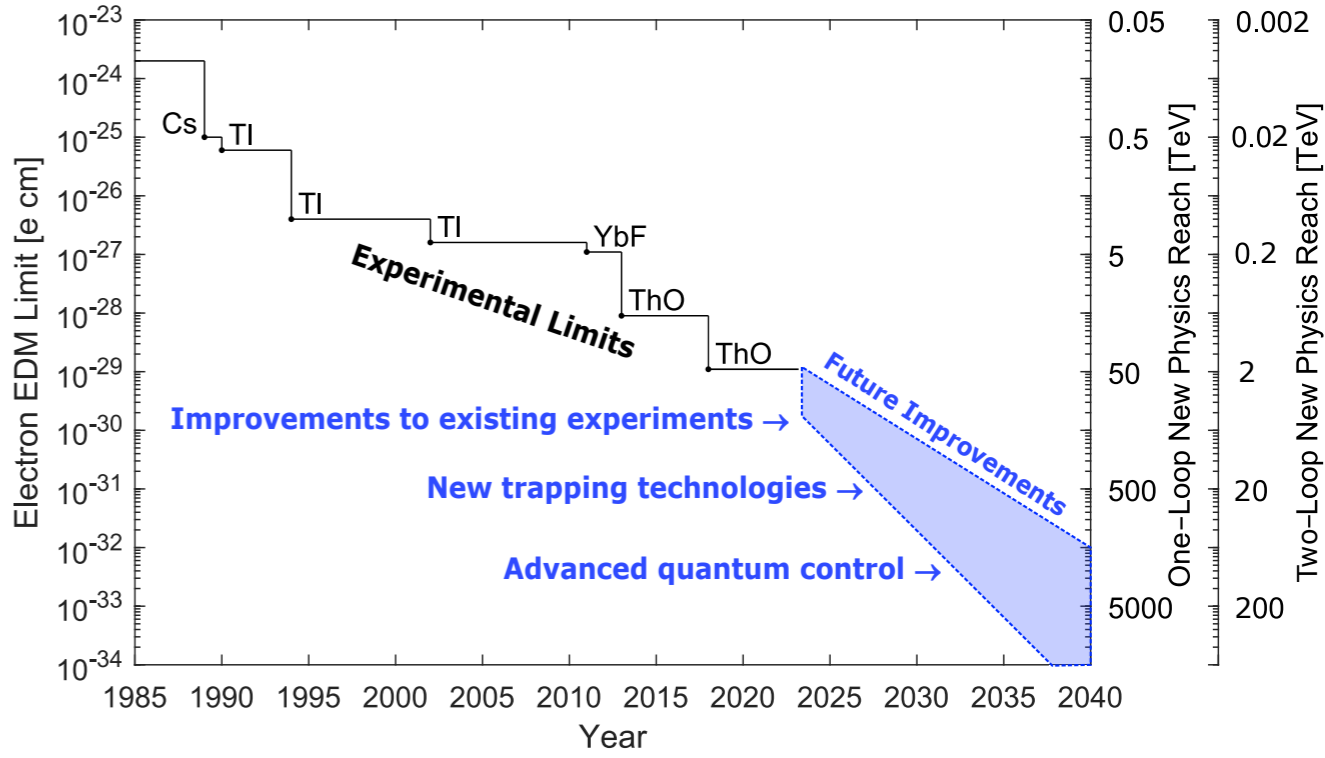


A Promising Decade of Precision Experiments

Searches for Charged-Lepton Flavor Violation in Experiments using Intense Muon Beams



Put differently: precision probes have a fantastic chance at discovering signals of new physics in the coming decade, and that physics could very well be near the TeV scale!

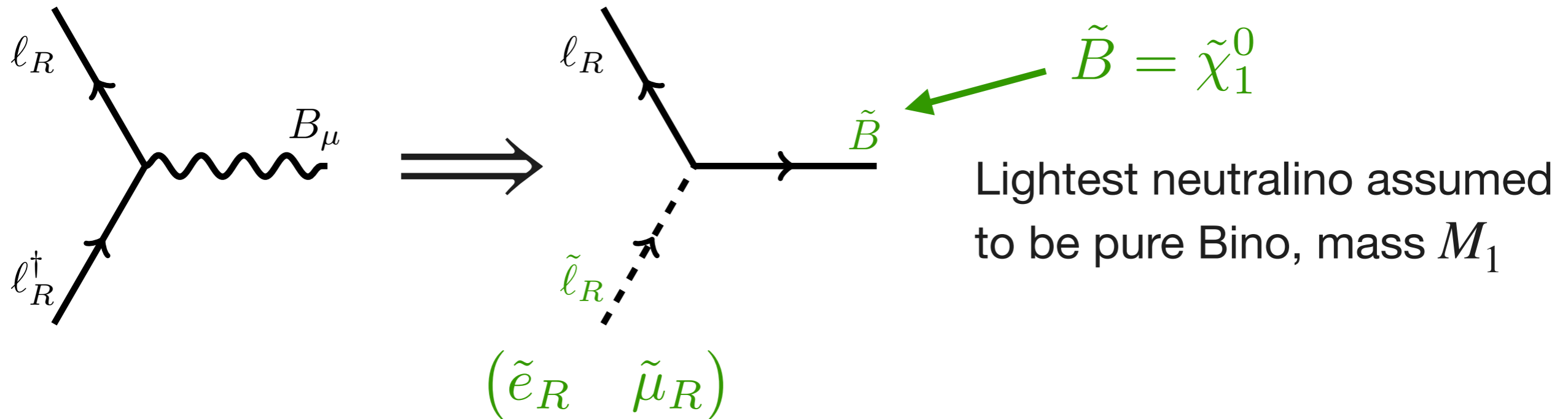


High-Energy Muon Colliders Uniquely Complementary to Precision Flavor Probes

Goal Today: demonstrate this in context of lepton flavor violation in an explicit scenario

Lepton Flavor Violation in the MSSM

Supersymmetry introduces scalar partners of LH, RH leptons



In what follows, we'll assume all the LH, color-charged superpartners are parametrically heavier, and can be ignored

For now, we'll also ignore $\tilde{\tau}_L, \tilde{\tau}_R$

Lepton Flavor Violation in the MSSM

We're left with a 2×2 mixing problem:

$$\begin{pmatrix} \tilde{e}_R^\dagger & \tilde{\mu}_R^\dagger \end{pmatrix} \begin{pmatrix} m_R^2 + \Delta_{ee}^{RR} & \Delta_{e\mu}^{RR} \\ (\Delta_{e\mu}^{RR})^* & m_R^2 + \Delta_{\mu\mu}^{RR} \end{pmatrix} \begin{pmatrix} \tilde{e}_R \\ \tilde{\mu}_R \end{pmatrix}$$

Universal terms dictated by SUSY, gauge invariance

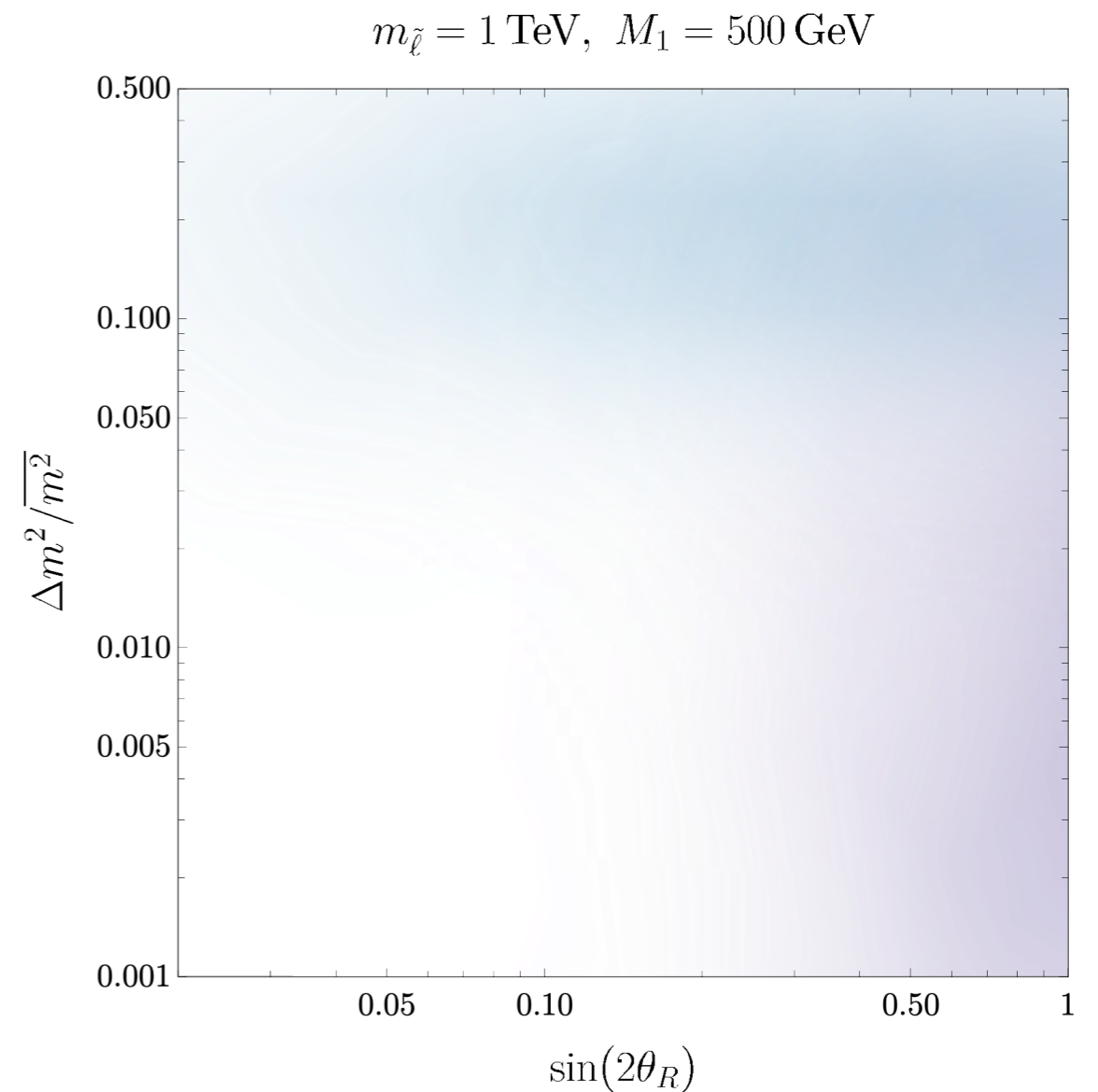
Flavor-violating, soft supersymmetry breaking terms

\implies flavor-violation a window into theory of SUSY-breaking

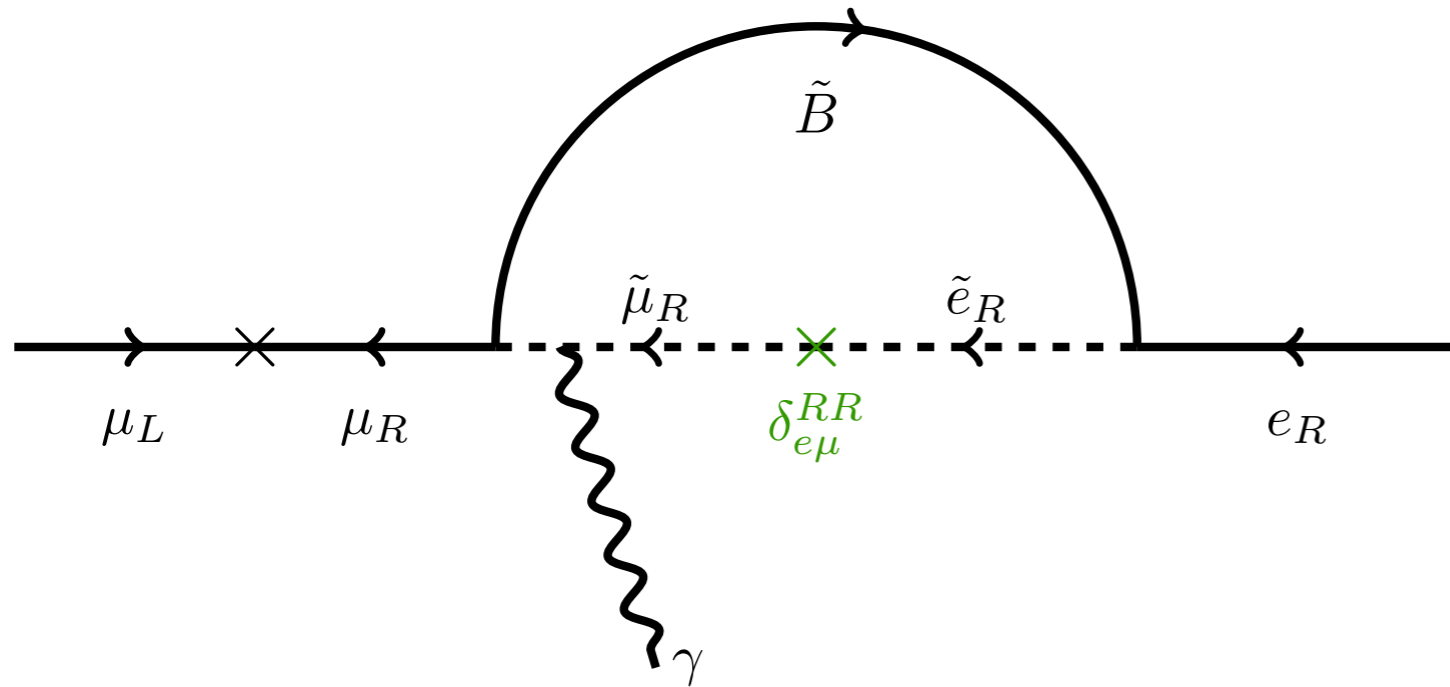
Diagonalize via unitarity matrix with mixing angle θ_R

Phenomenology described by $\sin 2\theta_R$, Δm^2 , $\overline{m^2}$, and M_1

Expectations in Models of ~~SUSY~~

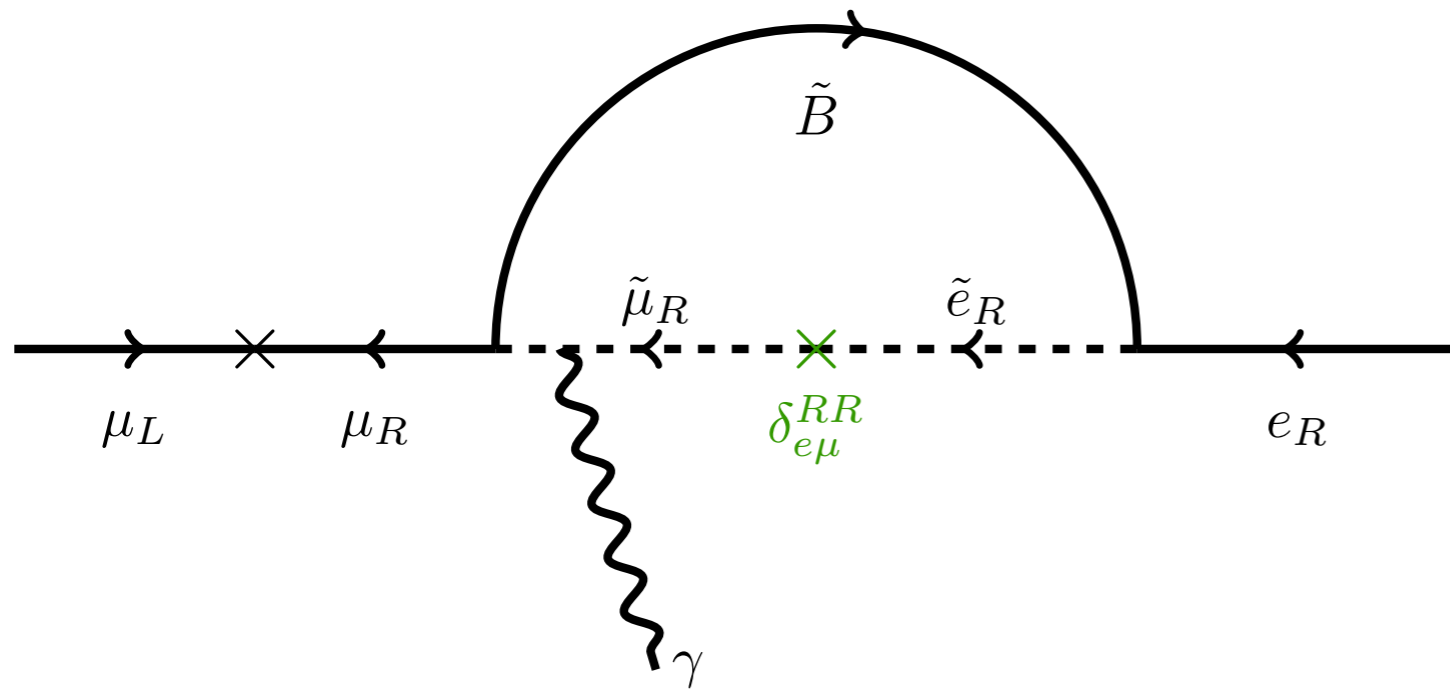


$\mu \rightarrow e\gamma$ Decays



$$\mathcal{A}_{\mu e}^R = m_\mu \frac{\alpha_Y}{8\pi} \sin(2\theta_R) \left[\frac{1}{m_{\tilde{\ell}_1}^2} \bar{A}\left(\frac{|M_1|^2}{m_{\tilde{\ell}_1}^2}\right) - \frac{1}{m_{\tilde{\ell}_2}^2} \bar{A}\left(\frac{|M_1|^2}{m_{\tilde{\ell}_2}^2}\right) \right]$$

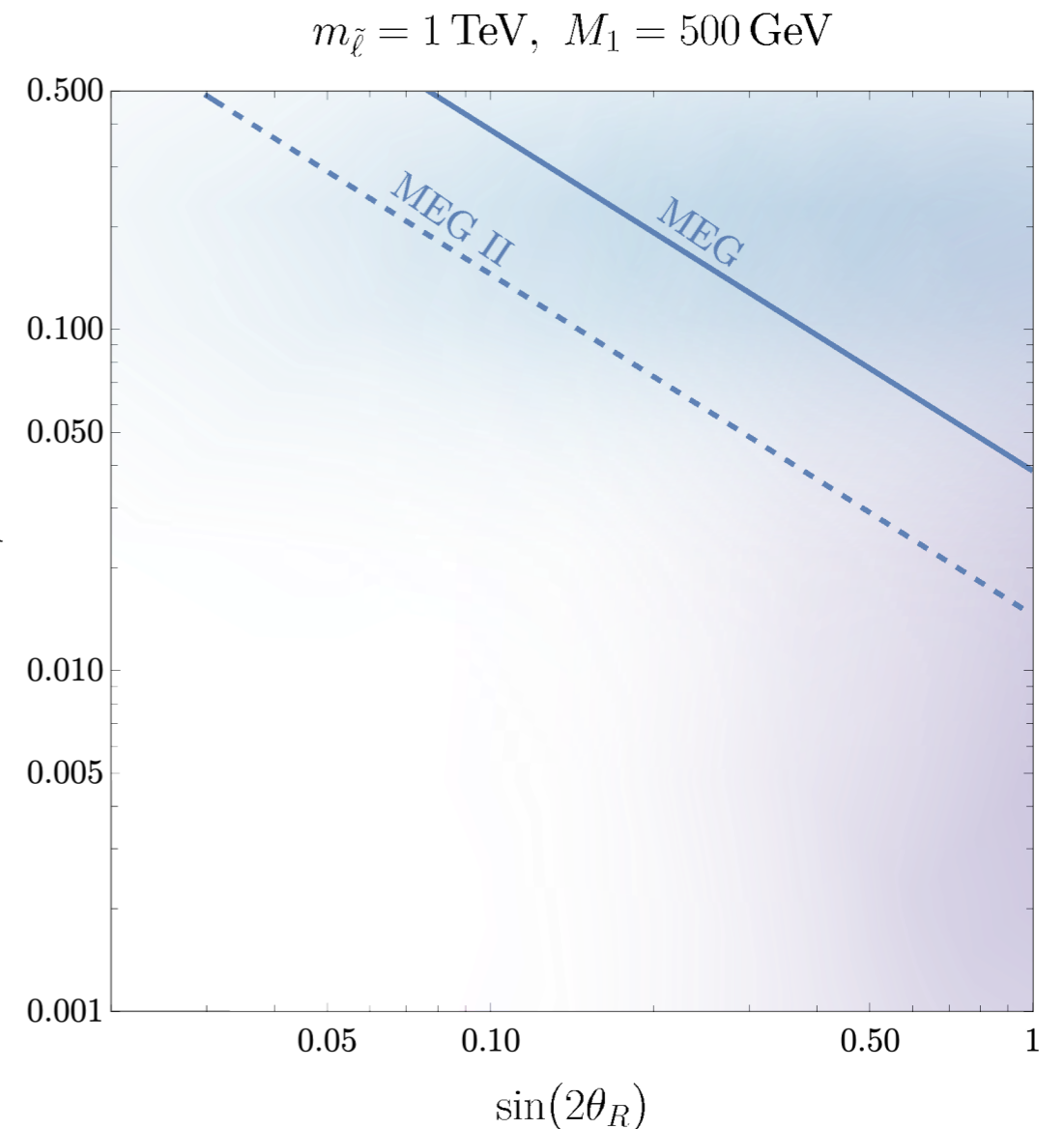
$\mu \rightarrow e\gamma$ Decays



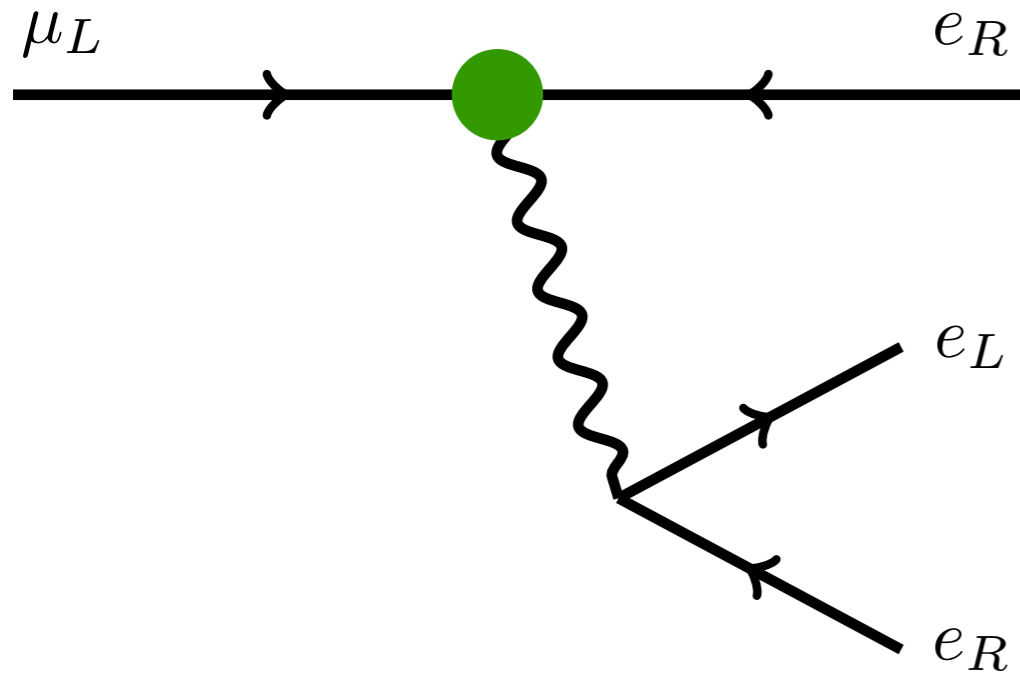
$$A_{\mu e}^R = m_\mu \frac{\alpha_Y}{\pi} \delta_{\mu e}^{RR} \frac{1}{m^2} f_{1n} \left(\frac{|M_1|^2}{m^2} \right) \Delta m^2 / m^2$$

$$\delta_{\mu e}^{RR} = \frac{1}{2} \frac{\Delta m^2}{m^2} \sin(2\theta_R)$$

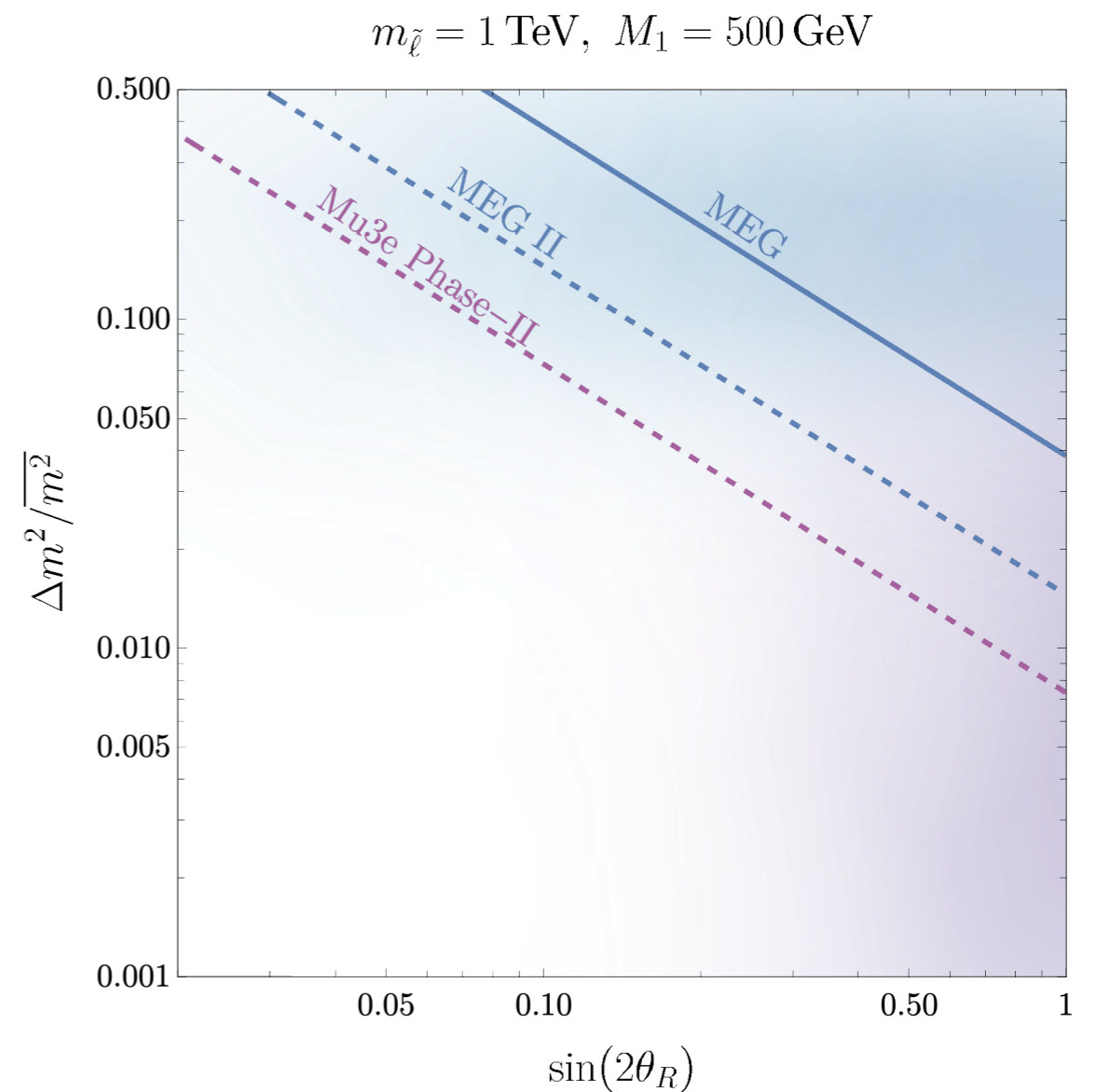
Mass-insertion parameter governing flavor violation



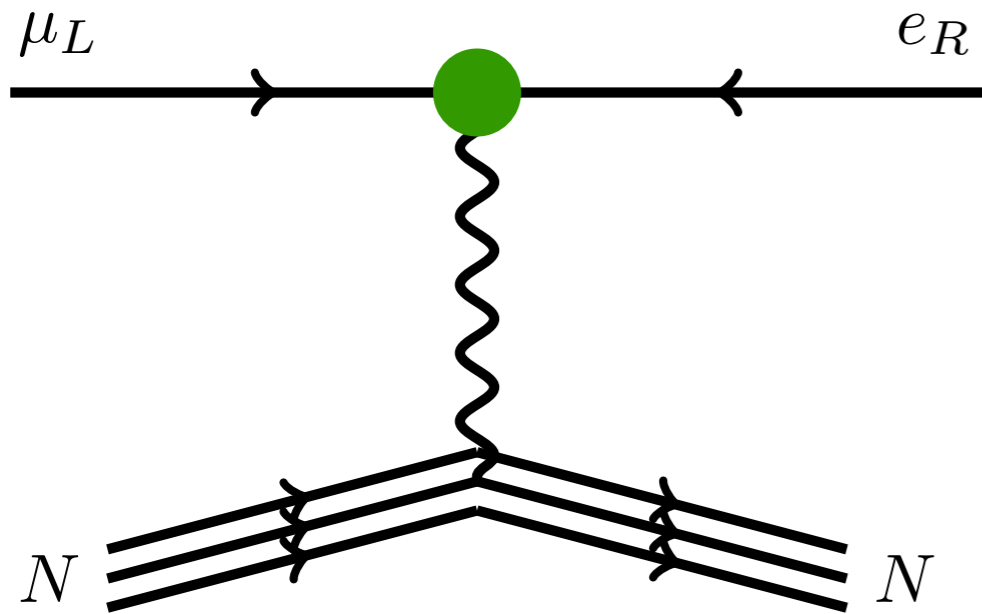
$\mu \rightarrow 3e$ Decays



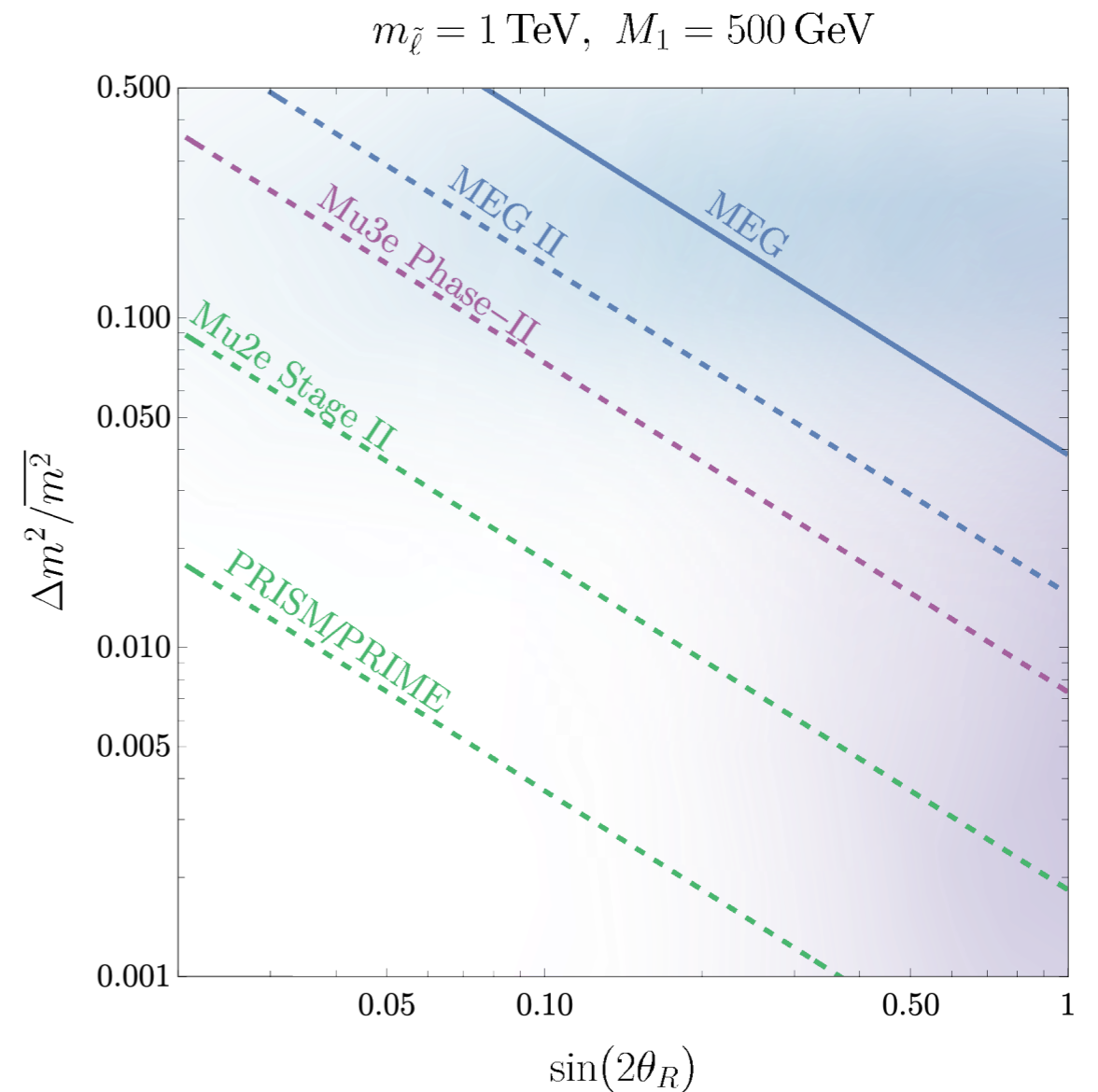
$$\text{BR}(\mu \rightarrow 3e) = \frac{\alpha}{3\pi} \left(\log \frac{m_\mu^2}{m_e^2} - \frac{11}{4} \right) \text{BR}(\mu \rightarrow e\gamma)$$



$\mu N \rightarrow e N$ Conversions



$$\text{CR}(\mu \rightarrow e)_N = C_N \alpha \text{BR}(\mu \rightarrow e \gamma)$$



Superpartners at a Muon Collider

Subtitle

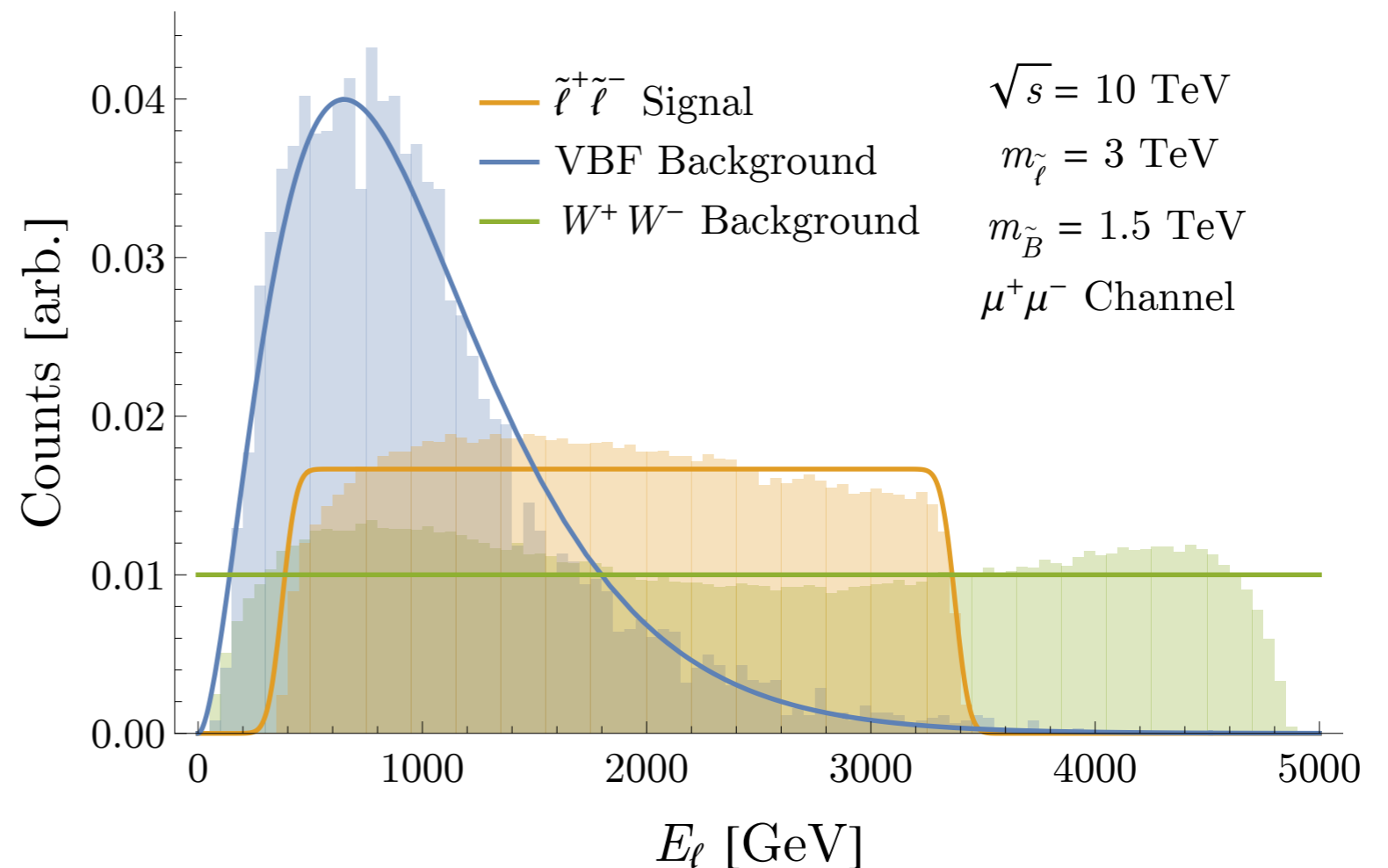
Measuring the Slepton/Neutralino Masses

Subtitle

$$E_\ell = \frac{\sqrt{s}}{4} \left(1 - \frac{M_1^2}{m_{\tilde{\ell}}^2} \right) (1 + \beta \cos \theta_0)$$

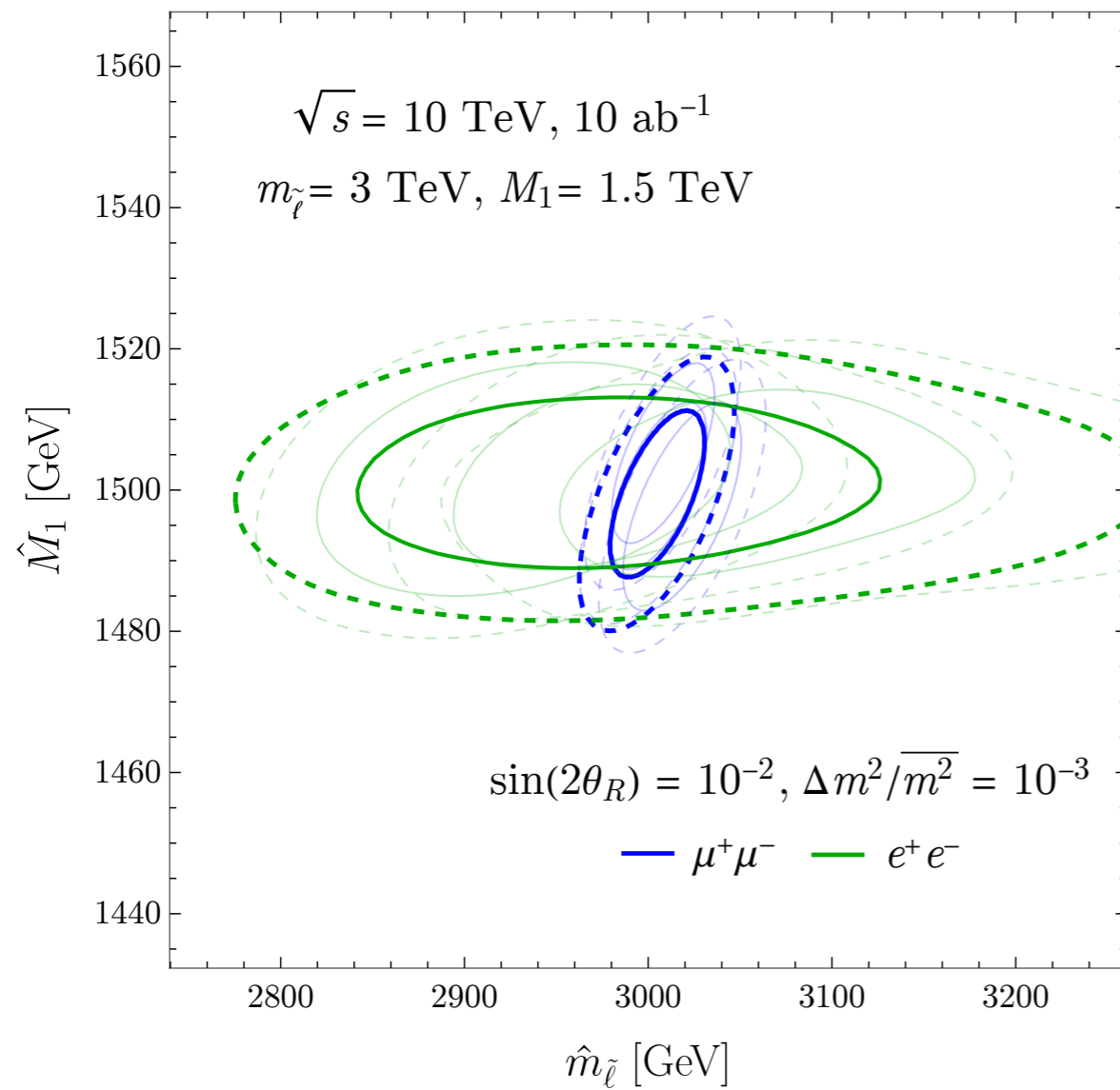
$$m_{\tilde{\ell}}^2 = s \frac{E_{\min} E_{\max}}{(E_{\min} + E_{\max})^2}$$

$$M_1^2 = m_{\tilde{\ell}}^2 \left(1 - \frac{2(E_{\min} + E_{\max})}{\sqrt{s}} \right)$$



Measuring the Slepton/Neutralino Masses

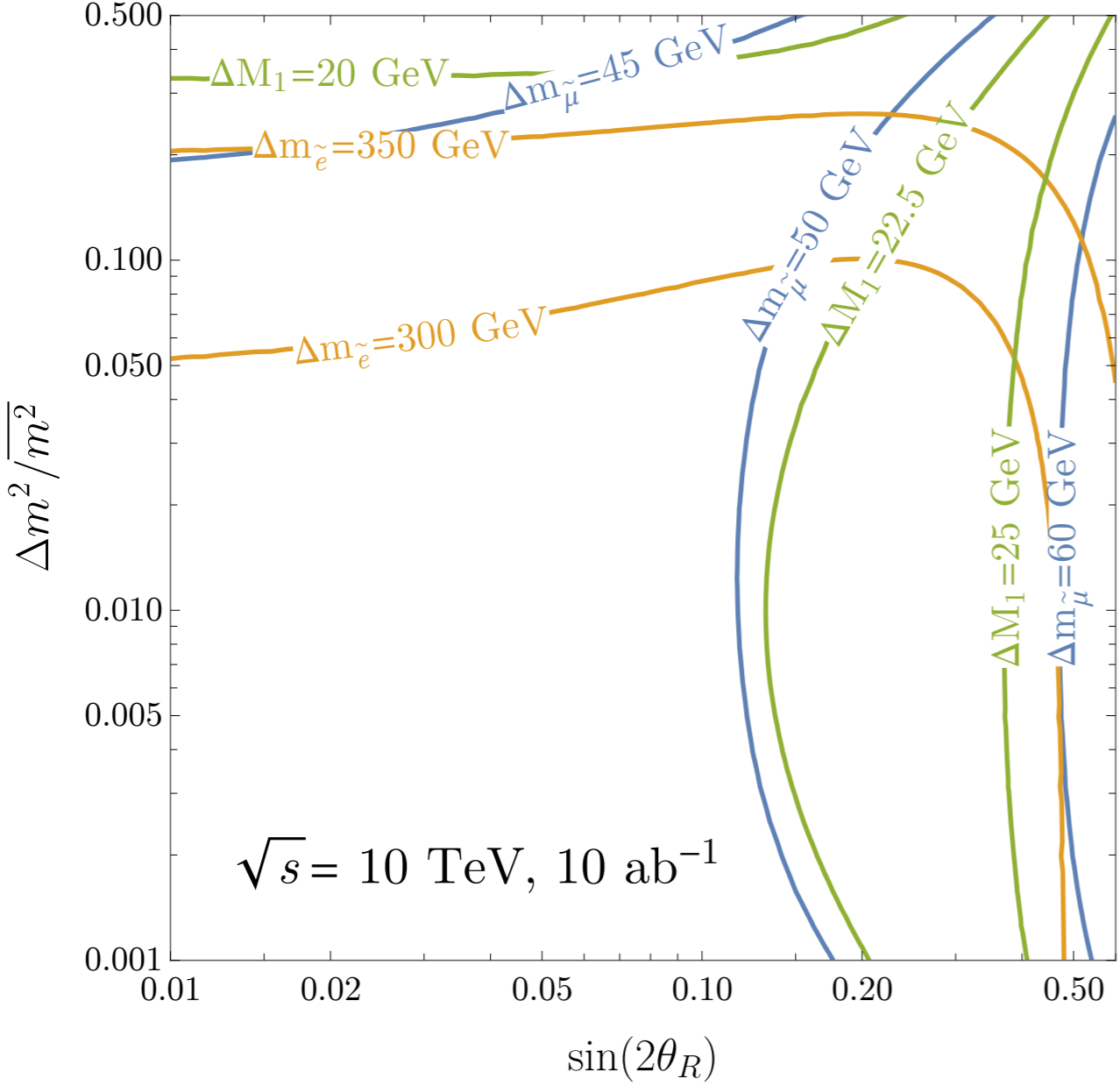
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Measuring the Slepton/Neutralino Masses

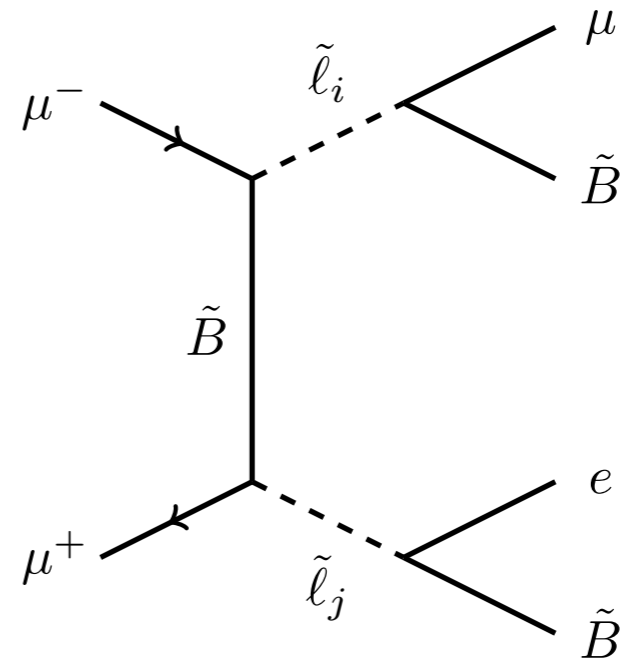
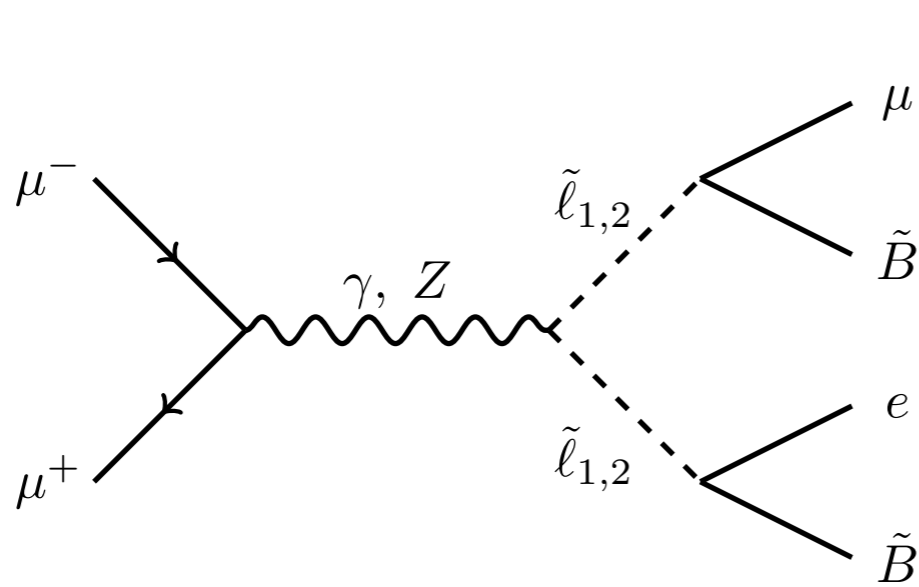
Subtitle

$$m_{\tilde{\ell}} = 3 \text{ TeV}, M_1 = 1.5 \text{ TeV}$$



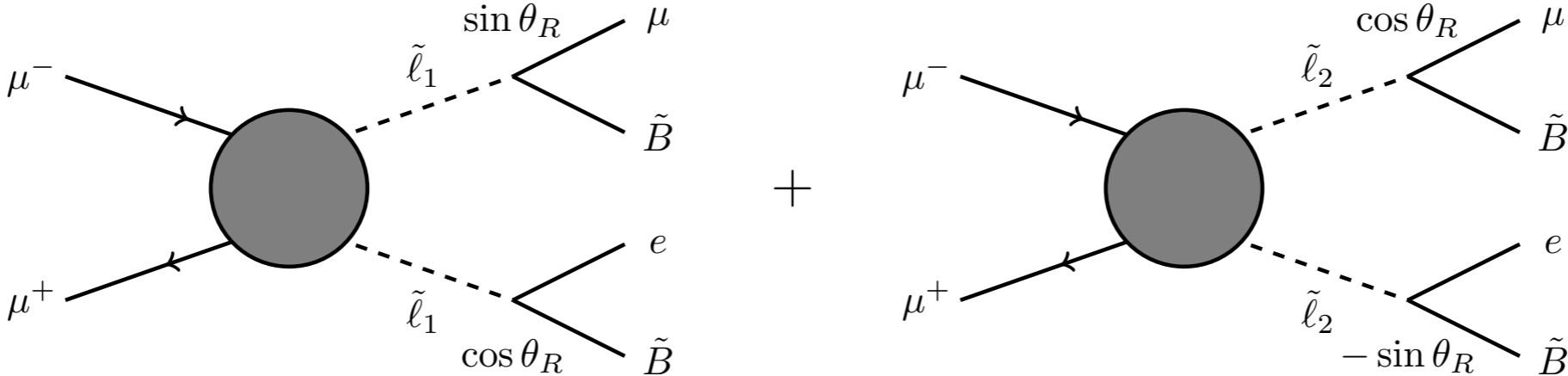
LFV Signals at a Muon Collider

Subtitle



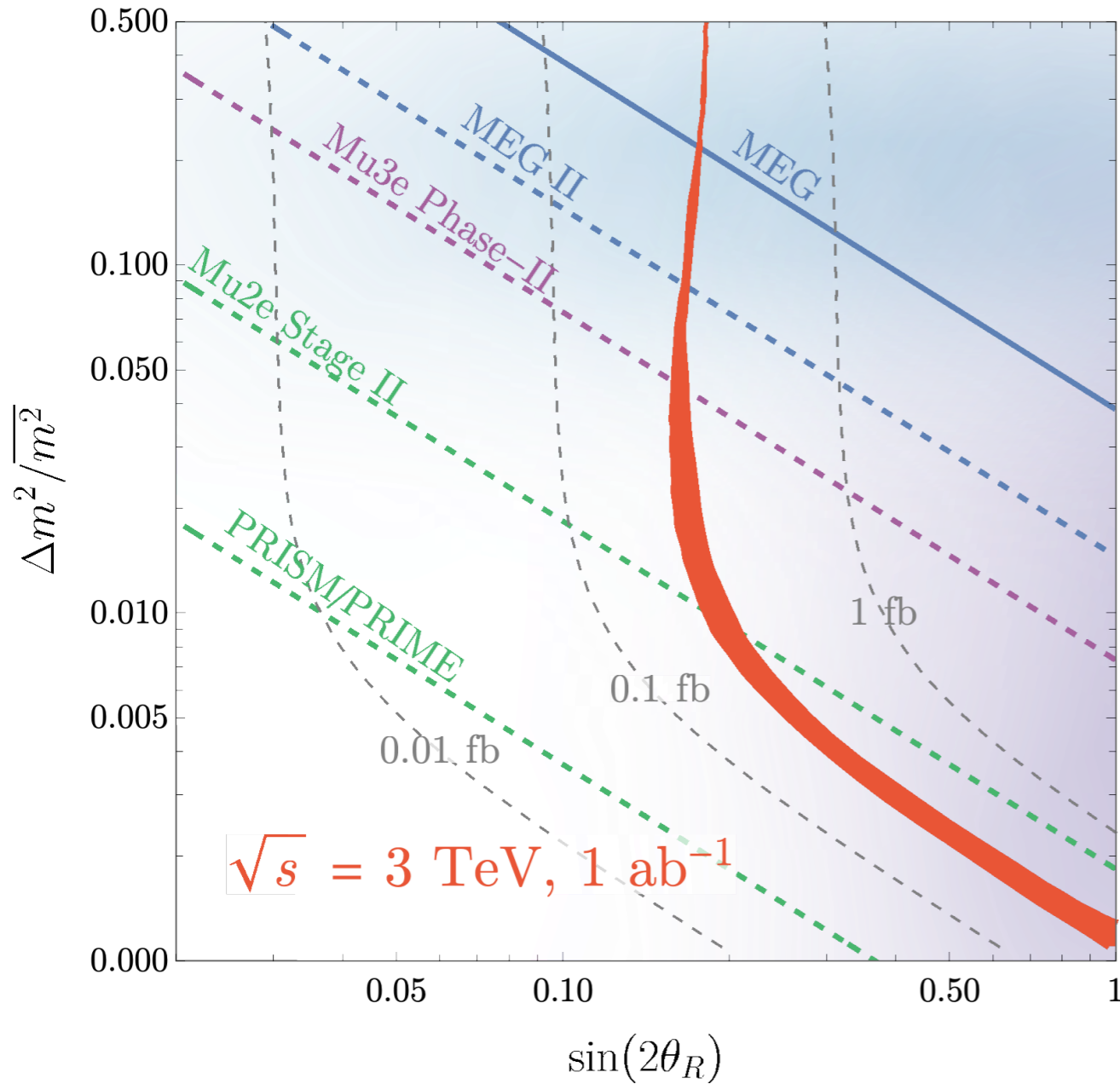
Interference is Important!

Subtitle

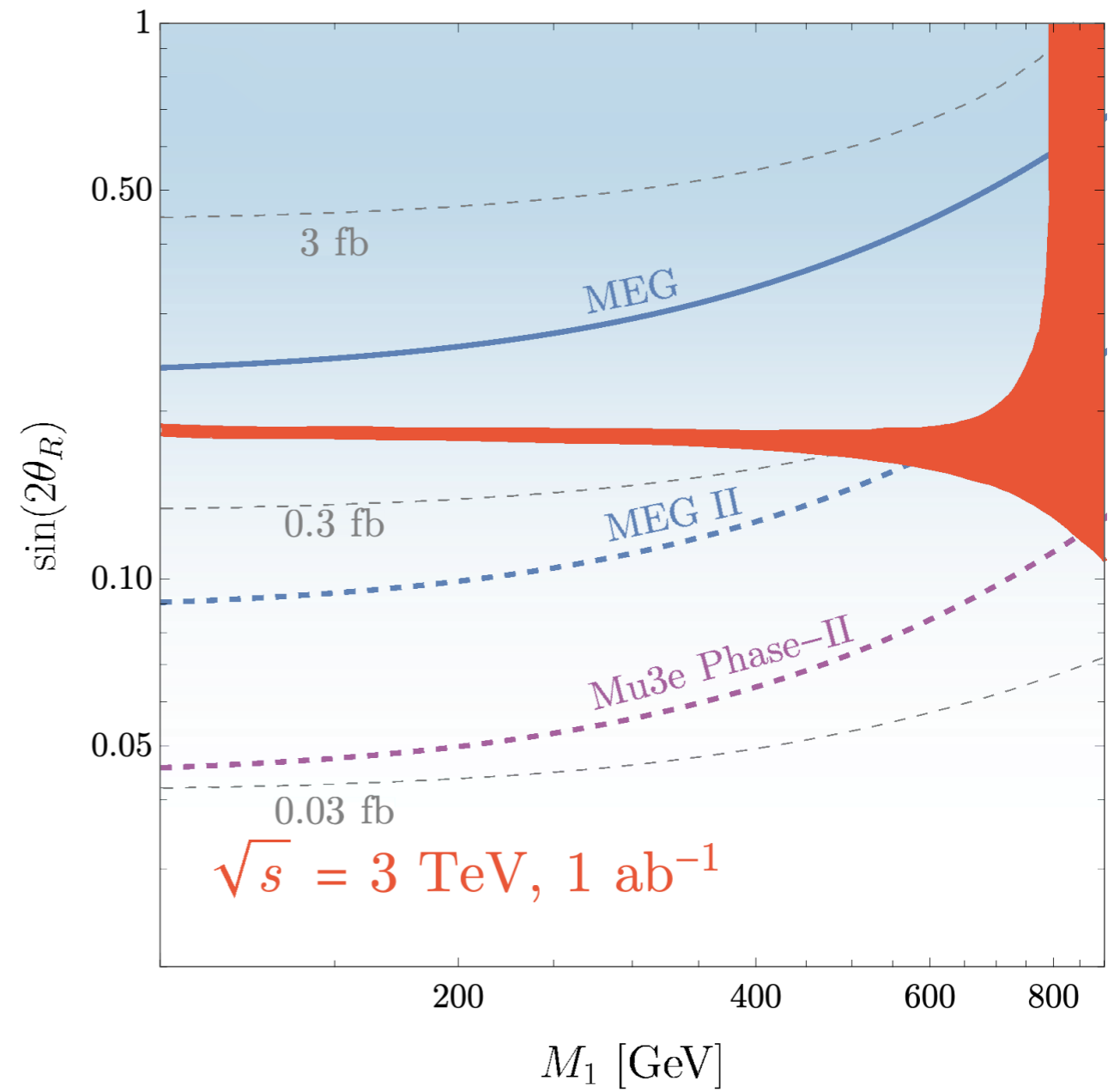


Discovery Reach for LFV Signals

$m_{\tilde{\ell}} = 1 \text{ TeV}, M_1 = 500 \text{ GeV}$

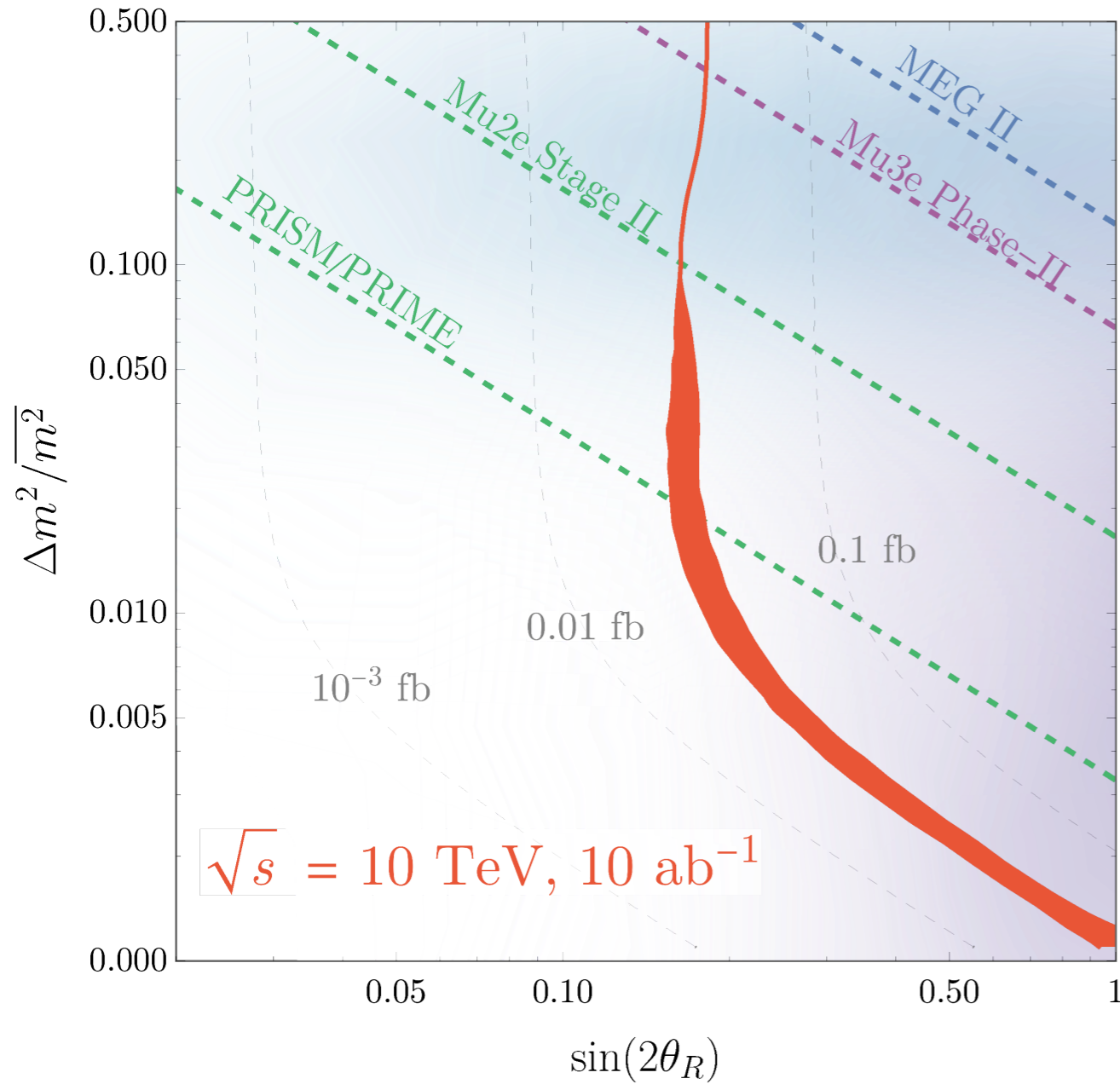


$m_{\tilde{\ell}} = 1 \text{ TeV}, \Delta m^2 / m^2 = 0.1$

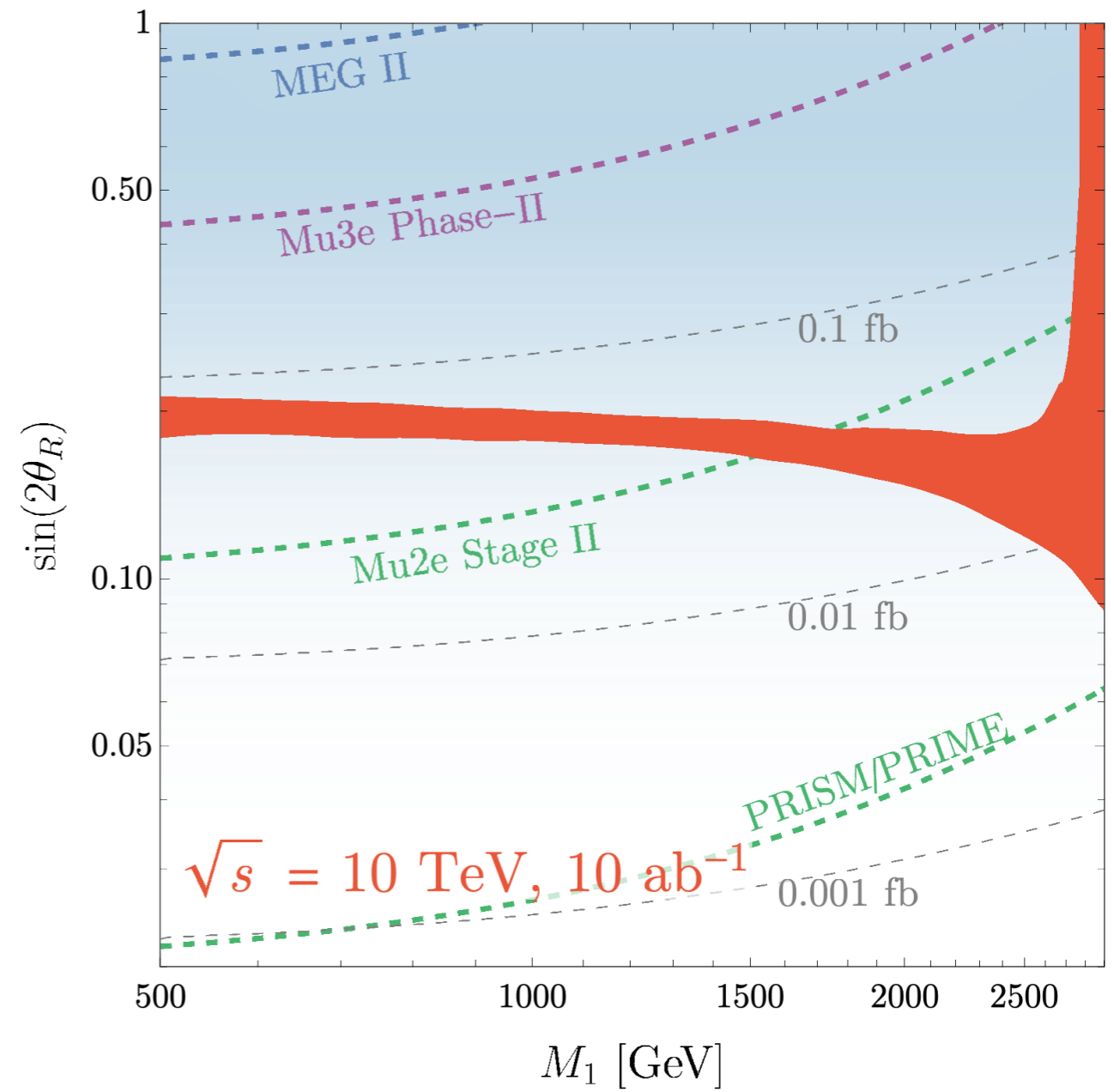


Discovery Reach for LFV Signals

$$m_{\tilde{\ell}} = 3 \text{ TeV}, M_1 = 1.5 \text{ TeV}$$

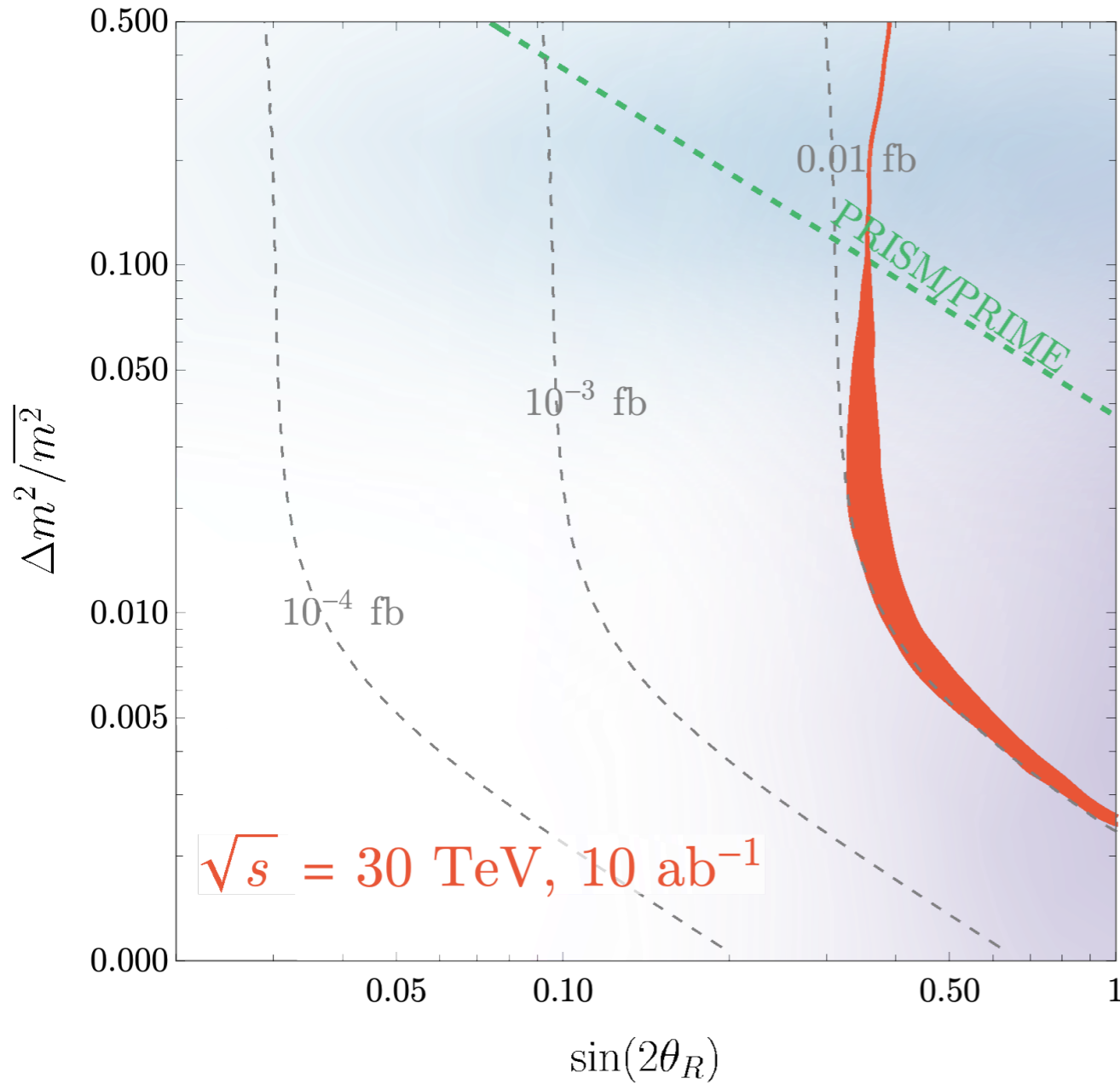


$$m_{\tilde{\ell}} = 3 \text{ TeV}, \Delta m^2 / \overline{m^2} = 0.1$$

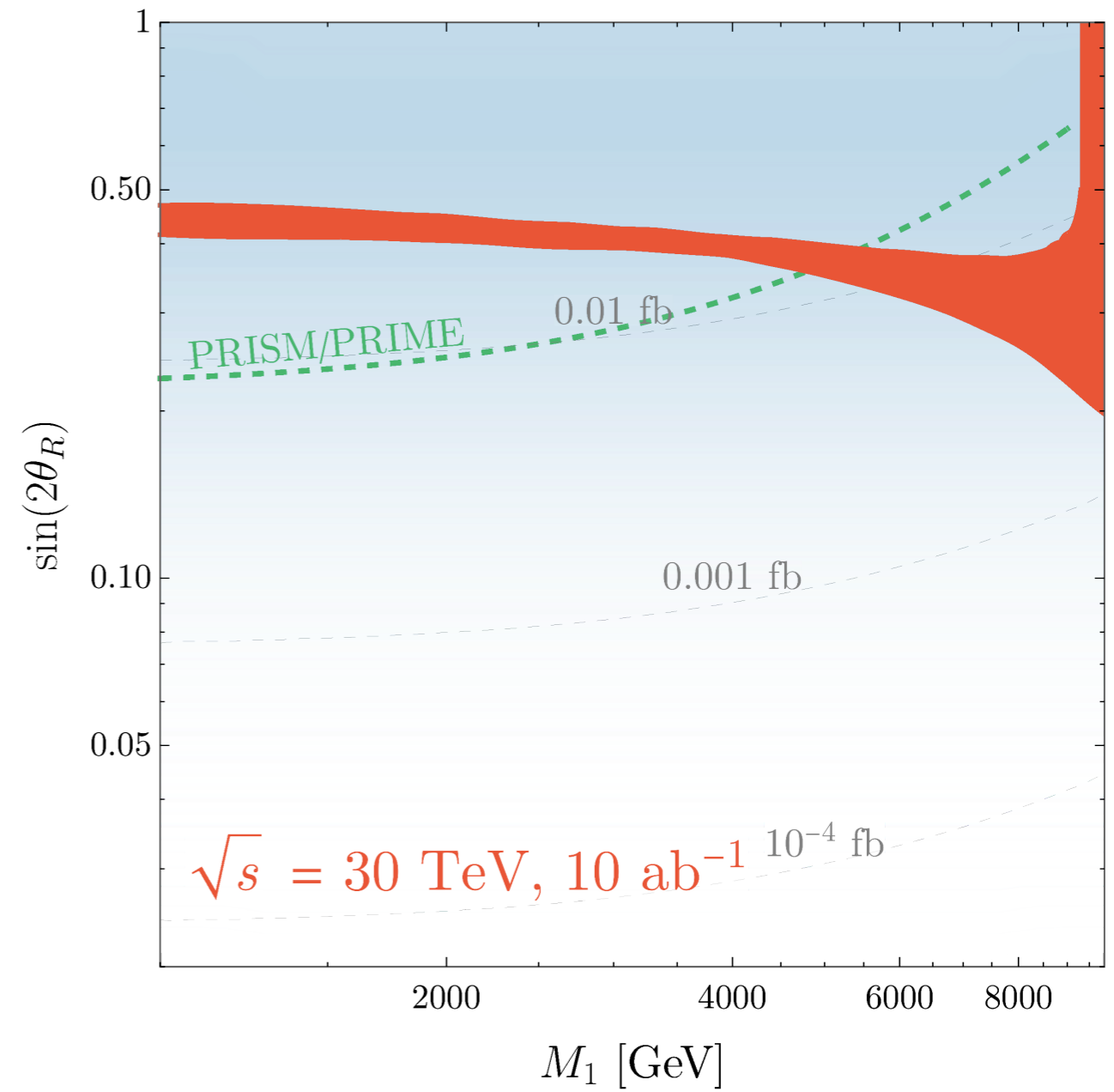


Discovery Reach for LFV Signals

$m_{\tilde{\ell}} = 10 \text{ TeV}, M_1 = 5 \text{ TeV}$



$m_{\tilde{\ell}} = 10 \text{ TeV}, \Delta m^2 / \overline{m^2} = 0.1$



Beyond the Minimal Scenario

Subtitle

Complementarity with eEDM: MFV

Subtitle

Complementarity with eEDM: $\tilde{\tau}$ Mixing

Subtitle

Summary