

# Putting SMEFT Fits to Work

## Lessons from Matching Simple Models

Based on

`arXiv:2007.01296, 2102.02823, 2110.06929, 2205.01561`

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In collaboration with

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**University of Cambridge, December 8, 2021**

# The State of LHC Physics

Have yet to find anything truly unexpected...

## ATLAS Heavy Particle Searches\* - 95% CL Upper Exclusion Limits

Status: July 2021

ATLAS Preliminary

$\int \mathcal{L} dt = (3.6 - 139) \text{ fb}^{-1}$

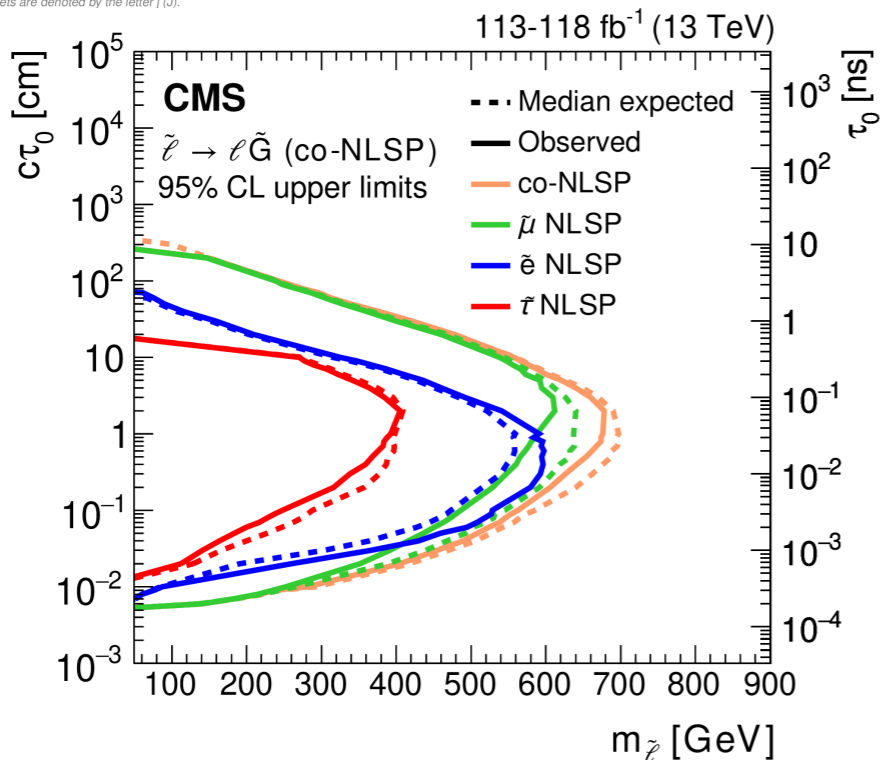
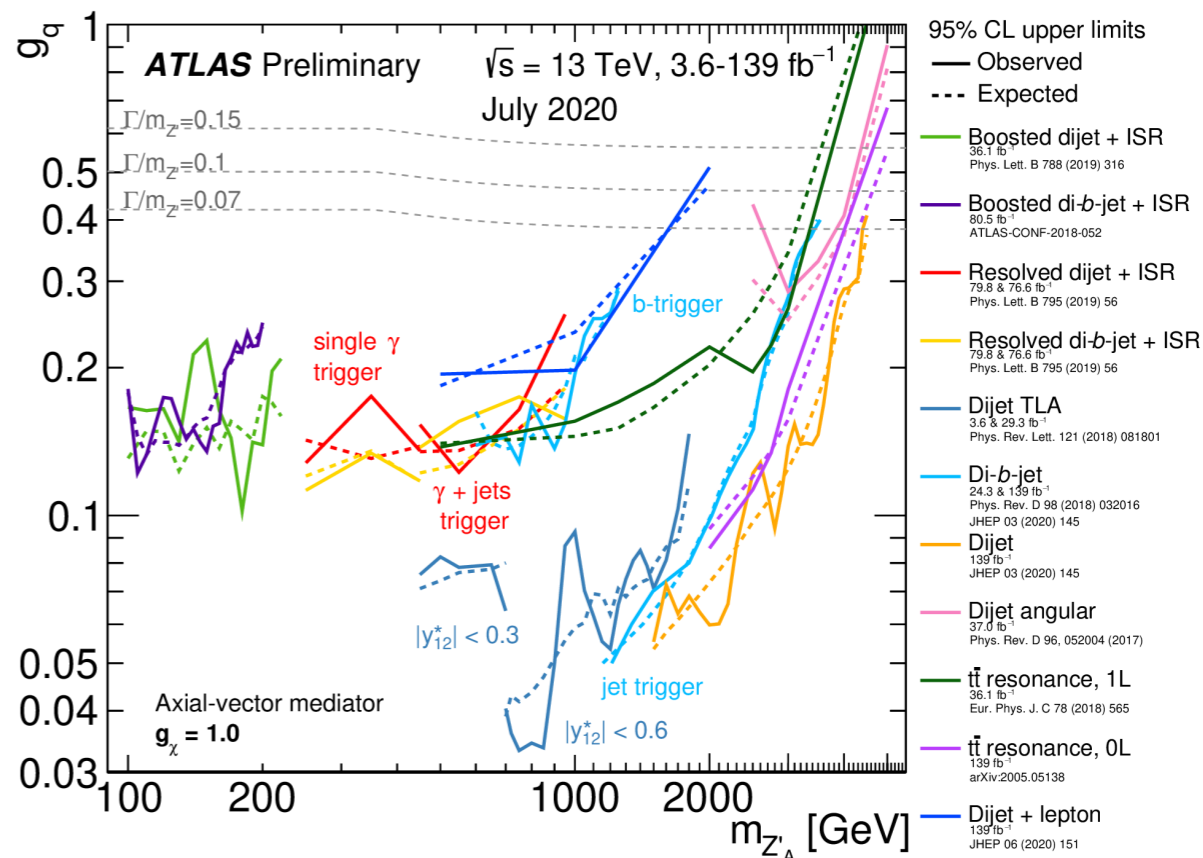
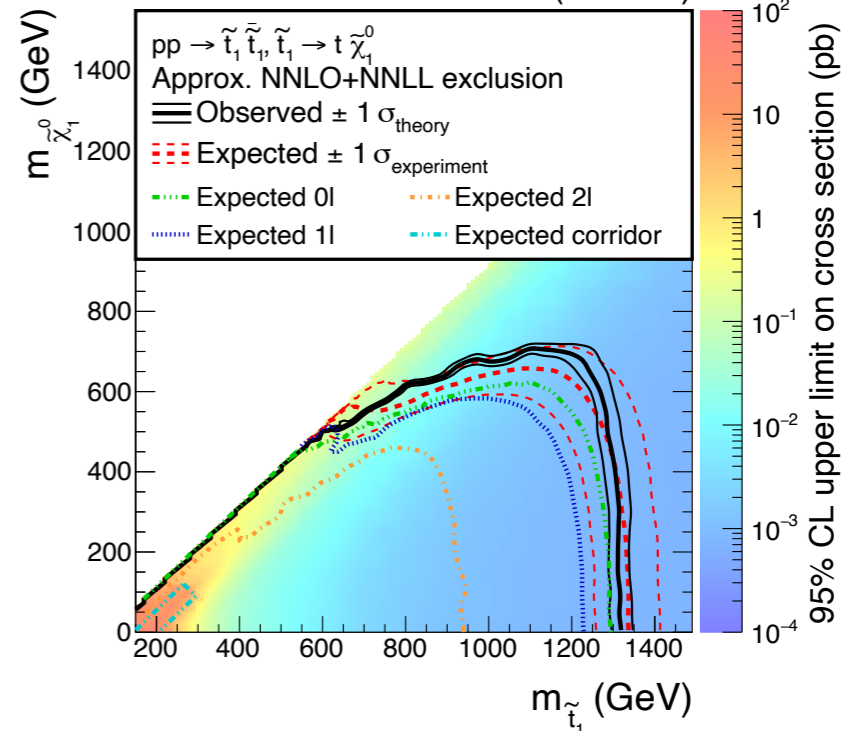
$\sqrt{s} = 8, 13 \text{ TeV}$

Model	$\ell, \gamma$	Jets†	$E_{\text{miss}}^{\dagger}$	$\int \mathcal{L} dt [\text{fb}^{-1}]$	Limit	Reference
<b>Extra dimensions</b>	ADD $G_{KK} + g/g$	$0, e, \mu, \tau, \gamma$	$1-4j$	Yes	139	$M_{\text{Pl}}$ mass
ADD non-resonant $\gamma\gamma$	$2\gamma$	-	-	-	36.7	$M_{\text{Pl}}$ mass
ADD GBH	-	$2j$	-	-	37.0	$M_{\text{Pl}}$ mass
ADD BH multijet	-	$\geq 3j$	-	-	3.6	$M_{\text{Pl}}$ mass
RS1 $G_{KK} \rightarrow \gamma\gamma$	$2\gamma$	-	-	-	139	$G_{KK}$ mass
Bulk RS $G_{KK} \rightarrow WW/ZZ$	multi-channel	-	-	-	36.1	$G_{KK}$ mass
Bulk RS $G_{KK} \rightarrow WW \rightarrow \ell\nu q\bar{q}$	$1, e, \mu$	$\geq 1b, \geq 1j$	Yes	139	$G_{KK}$ mass	
Bulk RS $G_{KK} \rightarrow t\bar{t}$	$1, e, \mu$	$\geq 2b, \geq 2j$	Yes	36.1	$G_{KK}$ mass	
2UED / RPP	$1, e, \mu$	$\geq 2b, \geq 2j$	Yes	36.1	$KK$ mass	
<b>Gauge bosons</b>	SSM $Z' \rightarrow \ell\ell$	$2, e, \mu$	-	-	139	$Z'$ mass
SSM $Z' \rightarrow \tau\tau$	$2, \tau$	-	-	-	36.1	$Z'$ mass
Leptophobic $Z' \rightarrow b\bar{b}$	$0, e, \mu$	$\geq 1b, \geq 2j$	Yes	139	$Z'$ mass	
Leptophobic $Z' \rightarrow t\bar{t}$	$0, e, \mu$	$\geq 1b, \geq 2j$	Yes	139	$Z'$ mass	
SSM $W' \rightarrow \ell\nu$	$1, e, \mu$	-	-	-	139	$W'$ mass
SSM $W' \rightarrow \tau\nu$	$1, \tau$	-	-	-	139	$W'$ mass
SSM $W' \rightarrow b\bar{b}$	$0, e, \mu$	$\geq 1b, \geq 1j$	Yes	139	$W'$ mass	
HVT $W' \rightarrow WZ \rightarrow \ell\nu q\bar{q}$ model B	$1, e, \mu$	$2j/1j$	Yes	139	$W'$ mass	
HVT $Z' \rightarrow ZH$ model B	$0, e, \mu$	$1-2b$	Yes	139	$Z'$ mass	
HVT $W' \rightarrow WH$ model B	$0, e, \mu$	$\geq 1b, \geq 2j$	Yes	139	$W'$ mass	
LRSM $W_{\mu} \rightarrow \mu W_e$	$2, \mu$	$1j$	-	-	80	$W_{\mu}$ mass
<b>CI</b>	CI $qqq$	$2, e, \mu$	-	-	37.0	$A$
CI $\ell\ell q\bar{q}$	$2, e, \mu$	-	-	-	139	$A$
CI $e\bar{e}b\bar{b}$	$2, e$	$1b$	-	-	139	$A$
CI $\mu\bar{\mu}b\bar{b}$	$2, \mu$	$1b$	-	-	139	$A$
CI $t\bar{t}t\bar{t}$	$\geq 1, e, \mu$	$\geq 1b, \geq 1j$	Yes	36.1	$A$	
<b>DM</b>	Axial-vector med. (Dirac DM)	$0, e, \mu, \tau, \gamma$	$1-4j$	Yes	139	$m_{\text{DM}}$
Pseudo-scalar med. (Dirac DM)	$0, e, \mu, \tau, \gamma$	$1-4j$	Yes	139	$m_{\text{DM}}$	
Vector med. $Z'$ -2HDM (Dirac DM)	$0, e, \mu$	$2b$	Yes	139	$m_{\text{DM}}$	
Pseudo-scalar med. 2HDM-a	multi-channel	-	-	-	139	$m_{\text{DM}}$
Scalar reson. $\phi \rightarrow t\bar{t}$ (Dirac DM)	$0-1, e, \mu$	$1b, 0-1j$	Yes	36.1	$m_{\text{DM}}$	
<b>LO</b>	Scalar LQ 1 <sup>st</sup> gen	$2, e, \mu$	$\geq 2j$	Yes	139	$LQ$ mass
Scalar LQ 2 <sup>nd</sup> gen	$2, \mu$	$\geq 2j$	Yes	139	$LQ$ mass	
Scalar LQ 3 <sup>rd</sup> gen	$1, \tau$	$2b$	Yes	139	$LQ$ mass	
Scalar LQ 3 <sup>rd</sup> gen	$0, e, \mu$	$\geq 2j, \geq 2b$	Yes	139	$LQ$ mass	
Scalar LQ 3 <sup>rd</sup> gen	$\geq 2, e, \mu, \tau$	$\geq 1j, \geq 1b$	Yes	139	$LQ$ mass	
Scalar LQ 3 <sup>rd</sup> gen	$0, e, \mu, \tau$	$0-2, 1b, 2j$	Yes	139	$LQ$ mass	
<b>Heavy quarks</b>	VLO $TT \rightarrow Zt + X$	$2e/2\mu/3e, \mu$	$\geq 1b, \geq 1j$	Yes	139	$T$ mass
VLO $BB \rightarrow Wt/Zb + X$	multi-channel	-	-	-	36.1	$T$ mass
VLO $T_{3/2} T_{3/2} \rightarrow Wt + X$	$2(SS) \geq 3, e, \mu$	$\geq 1b, \geq 1j$	Yes	36.1	$T_{3/2}$ mass	
VLO $T \rightarrow Ht/Zt$	$1, e, \mu$	$\geq 1b, \geq 3j$	Yes	139	$T$ mass	
VLO $Y \rightarrow Wb$	$1, e, \mu$	$\geq 1b, \geq 1j$	Yes	36.1	$Y$ mass	
VLO $B \rightarrow Hb$	$0, e, \mu$	$\geq 2b, \geq 1j, \geq 1j$	Yes	139	$B$ mass	
<b>Excited fermions</b>	Excited quark $q^* \rightarrow qg$	-	$2j$	-	139	$q^*$ mass
Excited quark $q^* \rightarrow q\gamma$	$1j$	-	-	-	36.7	$q^*$ mass
Excited quark $b^* \rightarrow bg$	$1, b$	$1j$	-	-	36.1	$b^*$ mass
Excited lepton $\ell^* \rightarrow \ell\gamma$	$3, e, \mu$	-	-	-	20.3	$\ell^*$ mass
Excited lepton $\nu^*$	$3, e, \mu, \tau$	-	-	-	20.3	$\nu^*$ mass
<b>Other</b>	Type III Seesaw	$2, 3, 4, e, \mu$	$\geq 2j$	Yes	139	$N^{\pm}$ mass
LRSM Majorana $\nu$	$2, \mu$	$2j$	-	-	36.1	$N^{\pm}$ mass
Higgs triplet $H^{\pm\pm} \rightarrow W^{\pm}W^{\pm}$	$2, 3, 4, e, \mu$ (SS)	various	Yes	139	$H^{\pm\pm}$ mass	
Higgs triplet $H^{\pm\pm} \rightarrow \ell\ell$	$2, 3, 4, e, \mu$ (SS)	-	-	-	36.1	$H^{\pm\pm}$ mass
Higgs triplet $H^{\pm\pm} \rightarrow \ell\nu$	$3, e, \mu, \tau$	-	-	-	20.3	$H^{\pm\pm}$ mass
Multi-charged particles	-	-	-	-	36.1	multi-charged particle mass
Magnetic monopoles	-	-	-	-	34.4	monopole mass

\*Only a selection of the available mass limits on new states or phenomena is shown.

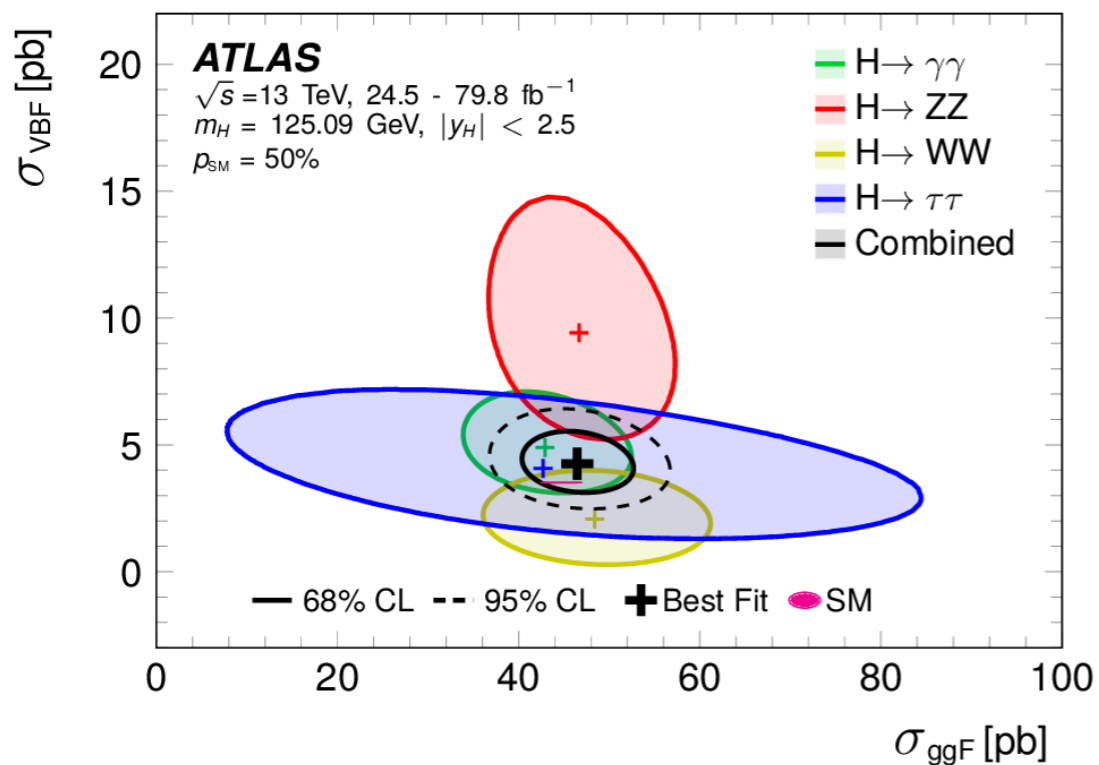
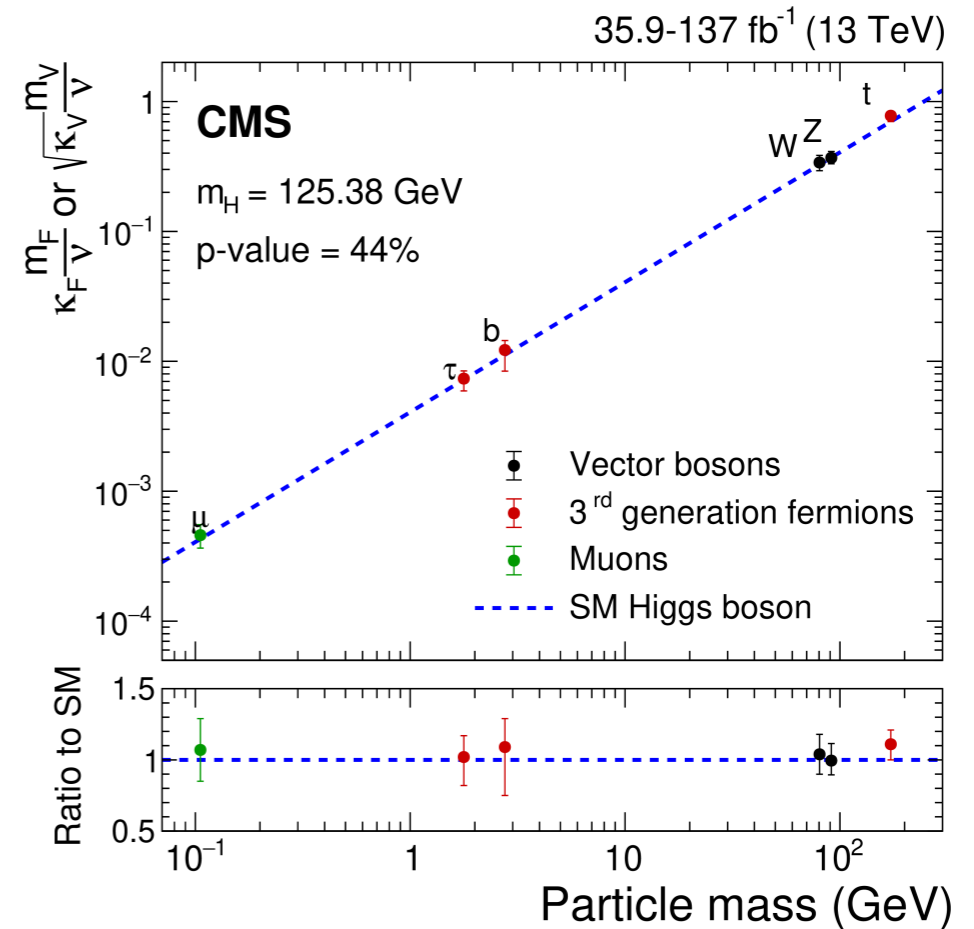
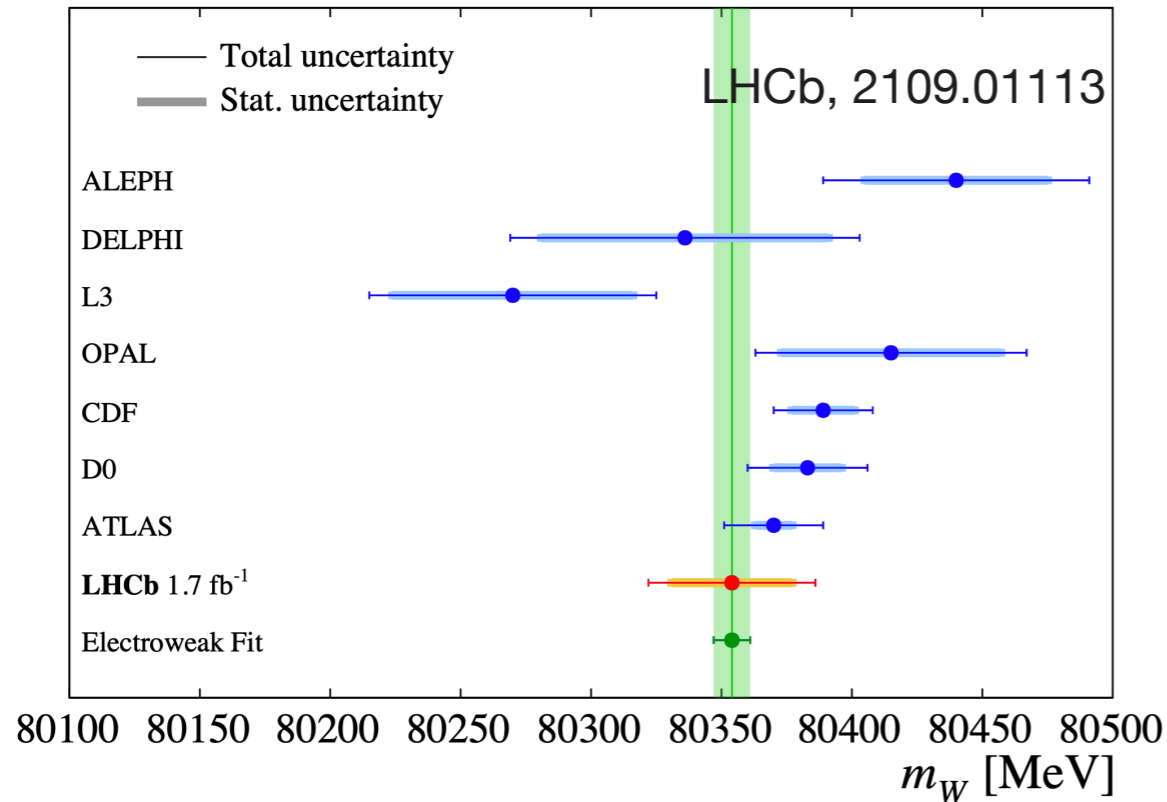
†Small-radius (large-radius) jets are denoted by the letter j (J).

## CMS 137 fb<sup>-1</sup> (13 TeV)



# The State of LHC Physics

But learning a great deal about the SM!



Given the wealth of data, in many different channels, need a framework to search for deviations from the SM...

# Enter the SMEFT

Treat the SM as an effective theory, with new physics at a scale  $\Lambda \gg v, E$

Assuming  $SU(2)_L \times U(1)_Y$  gauge + Lorentz invariance, with the Higgs transforming as a doublet (i.e., EWSB *linearly* realized), expand:

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$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \sum_{d=6,8,\dots} \sum_i \frac{C_i^{(d)}}{\Lambda^{d-2}} \mathcal{O}_i^{(d)}$$

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Coefficients treated as independent parameters, depend on underlying UV theory

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \sum_{d=6,8,\dots} \sum_i \frac{C_i^{(d)}}{\Lambda^{d-2}} \mathcal{O}_i^{(d)}$$

Counting in powers of  $\Lambda$   
(odd-dimension operators violate Lepton number)

Operators of given dimension built out of *only* SM fields

# Enter the SMEFT

arXiv:1008.4884, Grzadkowski, et. al — the Warsaw Basis

Complete (non-redundant) basis of effective operators exists:

$\mathcal{O}_u$	$(\bar{l}_L \gamma_\mu l_L)(\bar{l}_L \gamma^\mu l)_L$	$\mathcal{O}_{HWB}$	$(H^\dagger \tau^a H) W_{\mu\nu}^a B^{\mu\nu}$	$\mathcal{O}_{HD}$	$(H^\dagger D^\mu H)^* (H^\dagger D_\mu H)$
$\mathcal{O}_{He}$	$(H^\dagger i \overleftrightarrow{D}_\mu H)(\bar{e}_R \gamma^\mu e_R)$	$\mathcal{O}_{Hu}$	$(H^\dagger i \overleftrightarrow{D}_\mu H)(\bar{u}_R \gamma^\mu u_R)$	$\mathcal{O}_{Hd}$	$(H^\dagger i \overleftrightarrow{D}_\mu H)(\bar{d}_R \gamma^\mu d_R)$
$\mathcal{O}_{Hq}^{(3)}$	$(H^\dagger i \overleftrightarrow{D}_\mu^a H)(\bar{q}_L \tau^a \gamma^\mu q_L)$	$\mathcal{O}_{Hq}^{(1)}$	$(H^\dagger i \overleftrightarrow{D}_\mu H)(\bar{q}_L \gamma^\mu q_L)$	$\mathcal{O}_{Hl}^{(3)}$	$(H^\dagger i \overleftrightarrow{D}_\mu^a H)(\bar{l}_L \tau^a \gamma^\mu l_L)$
$\mathcal{O}_{Hl}^{(1)}$	$(H^\dagger i \overleftrightarrow{D}_\mu H)(\bar{l}_L \gamma^\mu l_L)$	$\mathcal{O}_{H\Box}$	$(H^\dagger H)\Box(H^\dagger H)$	$\mathcal{O}_{eH}$	$(H^\dagger H)\bar{l}_L \tilde{H} e_R$
$\mathcal{O}_{HG}$	$(H^\dagger H)G_{\mu\nu}^A G^{\mu\nu,A}$	$\mathcal{O}_{uH}$	$(H^\dagger H)(\bar{q}_L \tilde{H} u_R)$	$\mathcal{O}_{dH}$	$(H^\dagger H)(\bar{q}_L H d_R)$
$\mathcal{O}_{HB}$	$(H^\dagger H)B_{\mu\nu} B^{\mu\nu}$	$\mathcal{O}_{HW}$	$(H^\dagger H)W_{\mu\nu}^a W^{\mu\nu,a}$	$\mathcal{O}_W$	$\epsilon_{abc} W_\mu^{\nu,a} W_\nu^{\rho,b} W_\rho^{\mu,c}$
$\mathcal{O}_H$	$(H^\dagger H)^3$	(Note: not the full set here — lots of flavor / model-based assumptions to limit the ~3000 operators in the full EFT!)			

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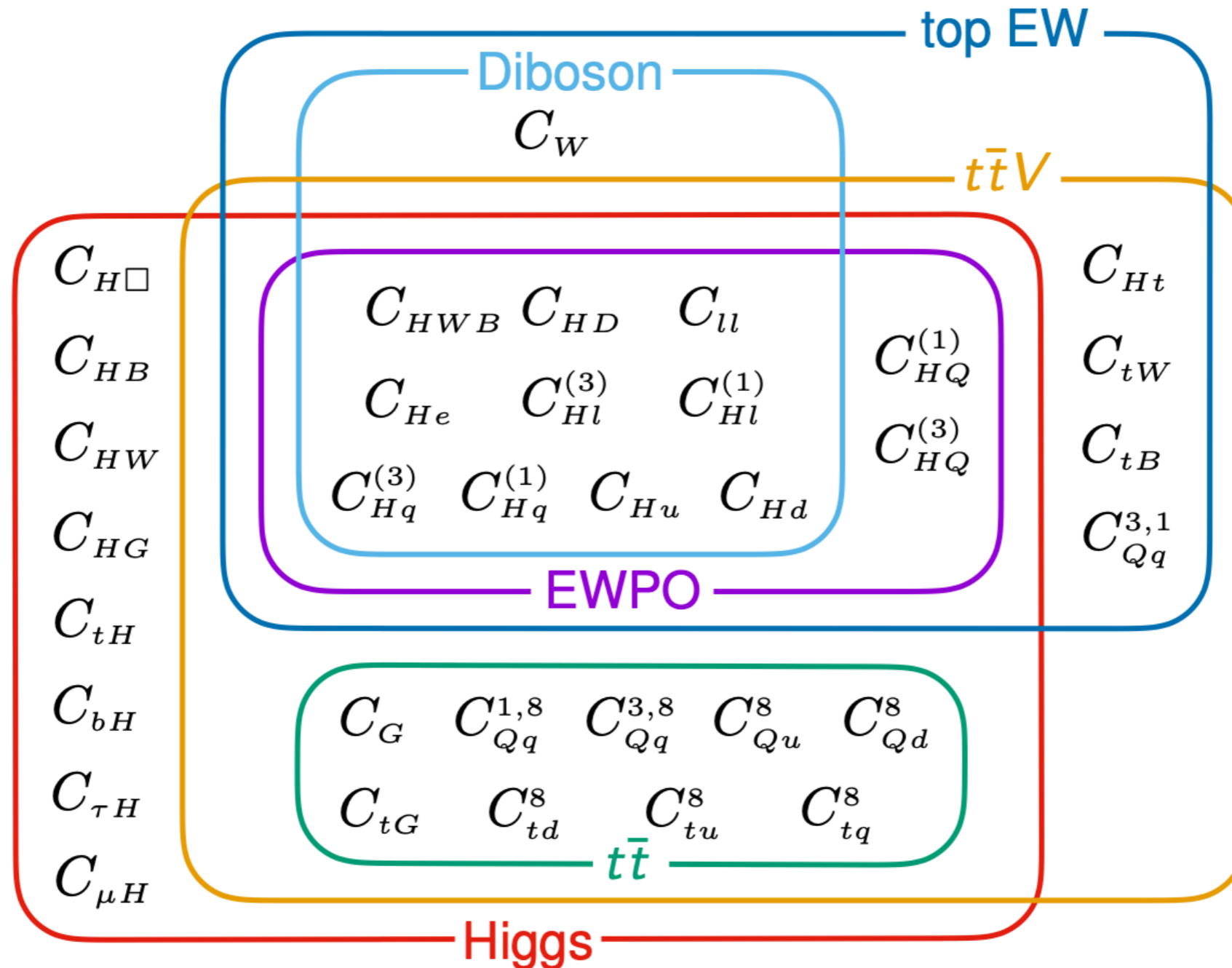
Recently enumerated at dimension-8 as well:

Li et al [2005.00008] + Murphy [2005.00059]



# Enter the SMEFT

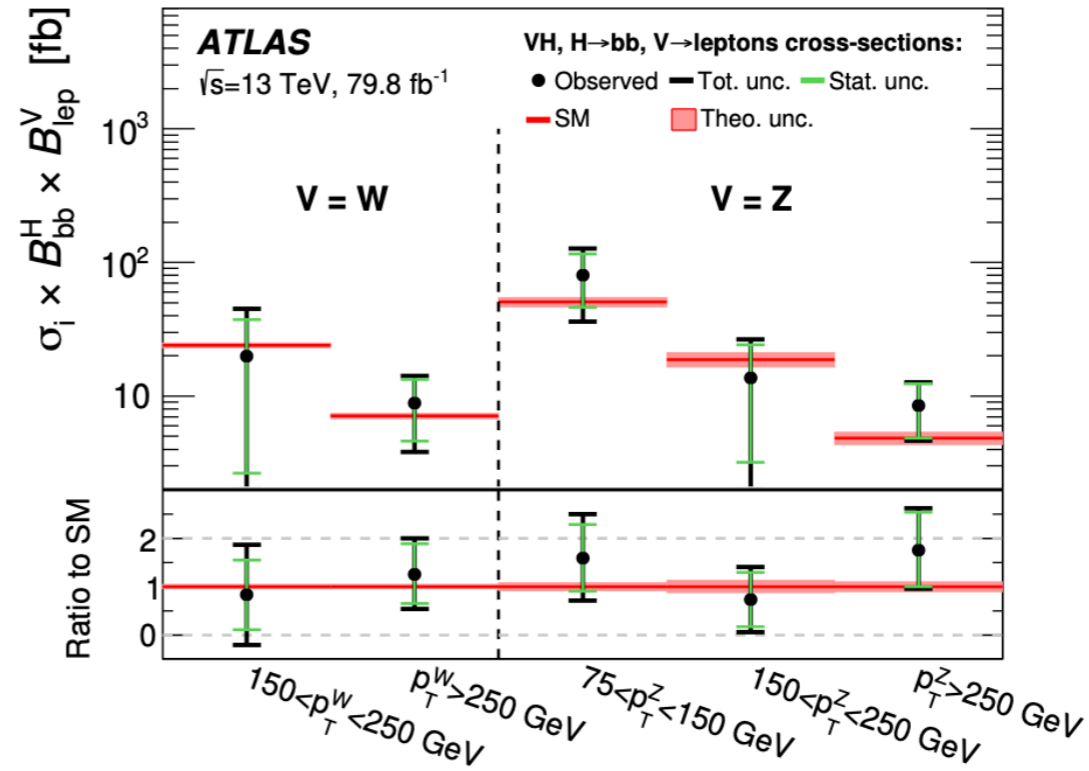
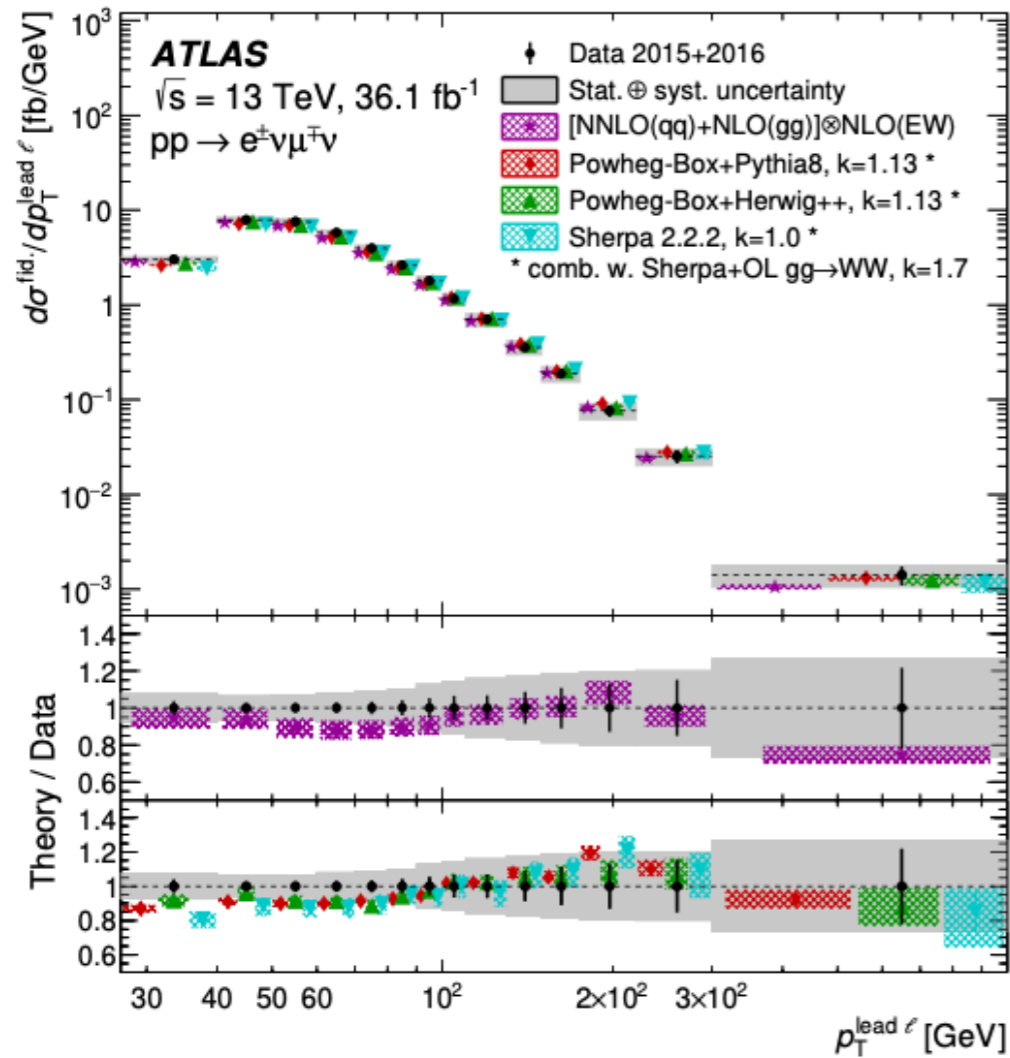
Effective operators allow for consistent combination of measurements



Ellis, Madigan, Mimasu, Sanz, You [2012.02779]

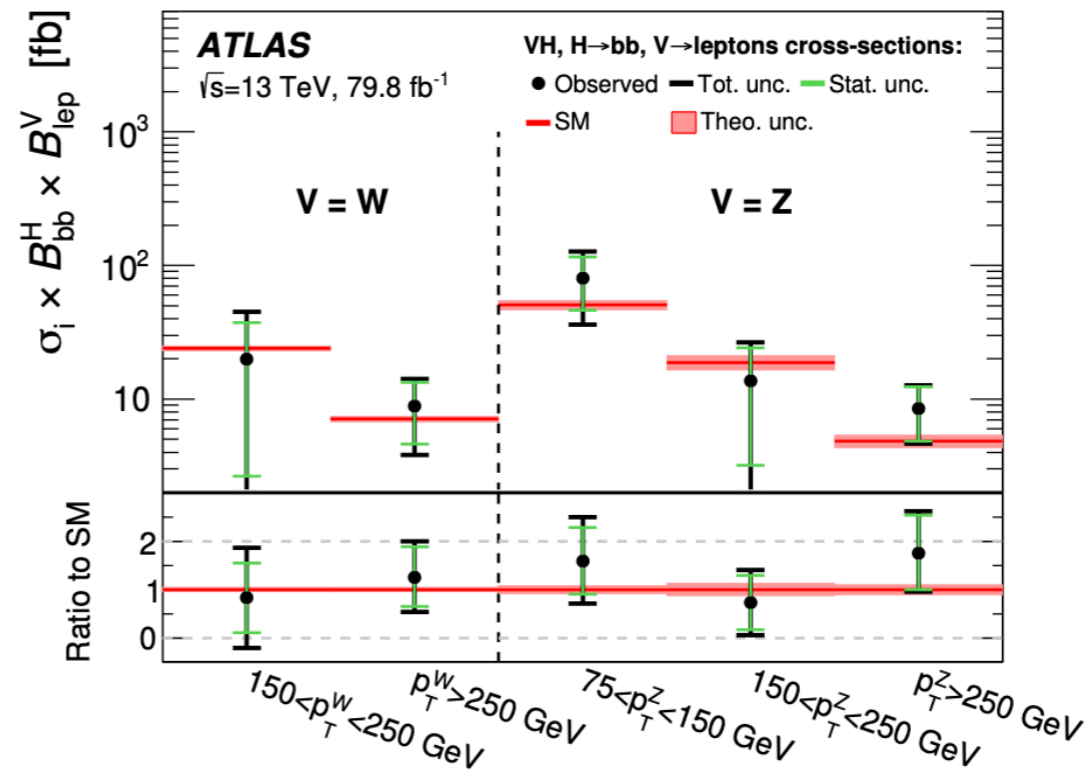
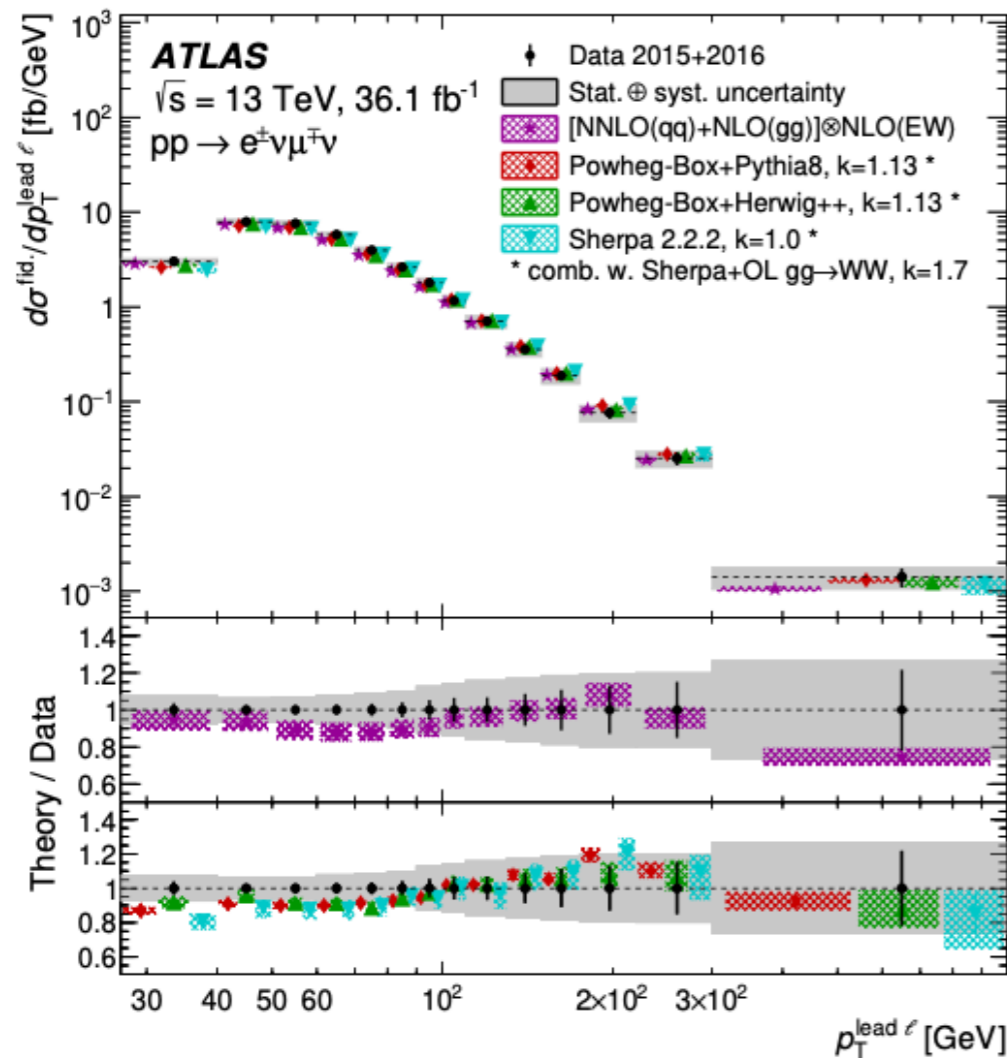
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... and can also parameterize deviations in kinematic distributions!

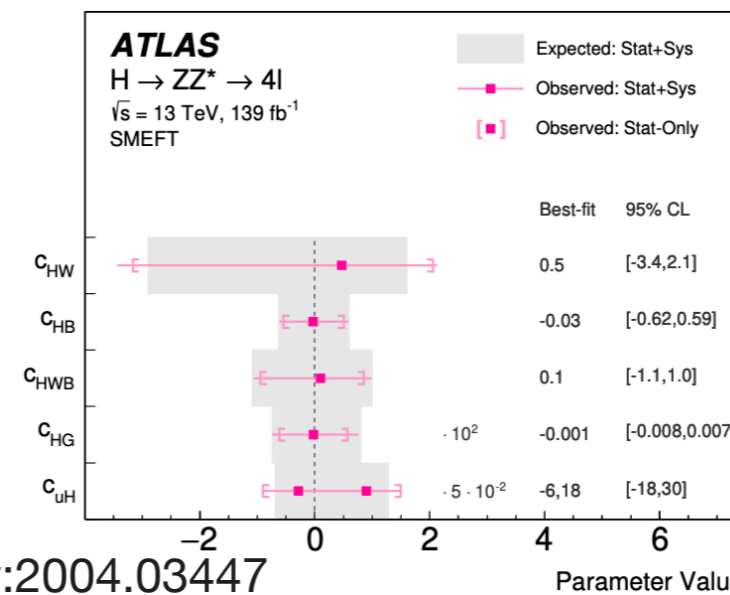


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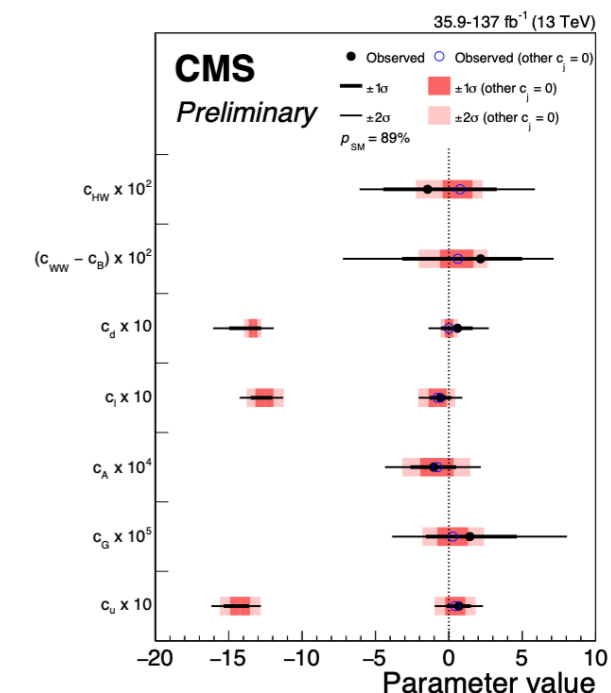
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Experiments starting to present limits in this framework:



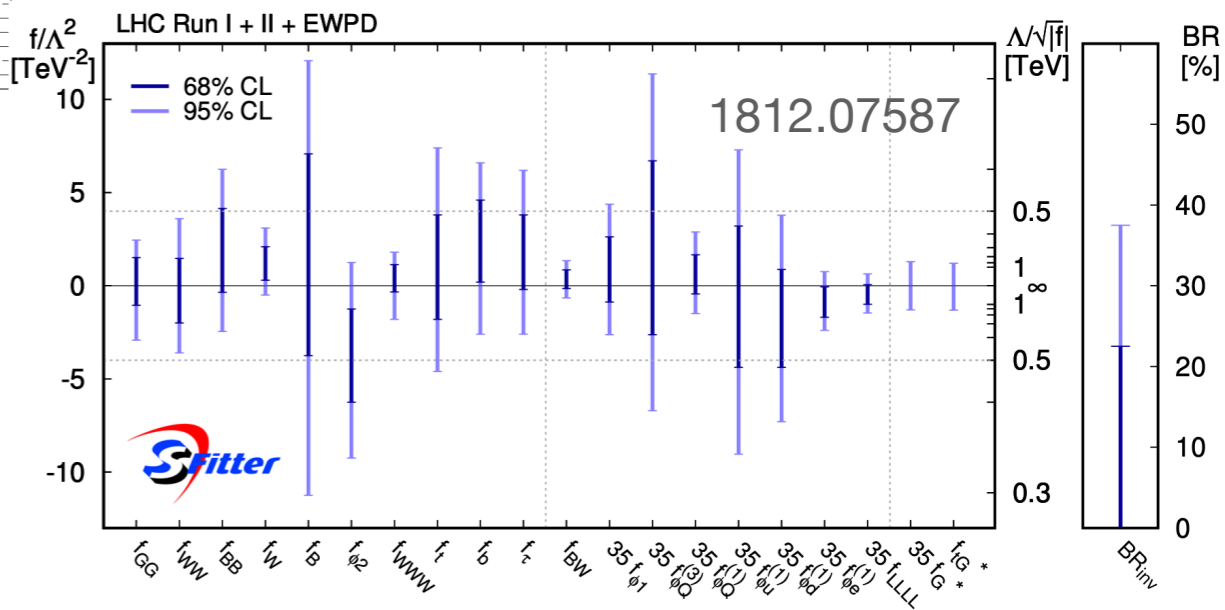
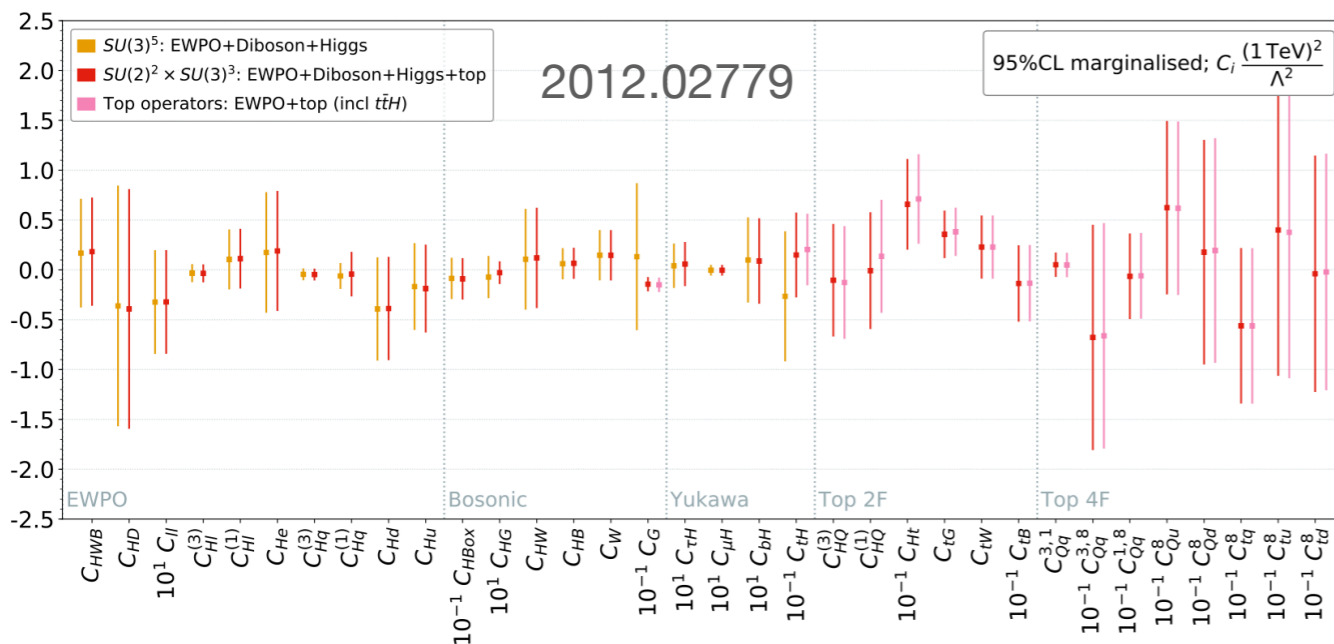
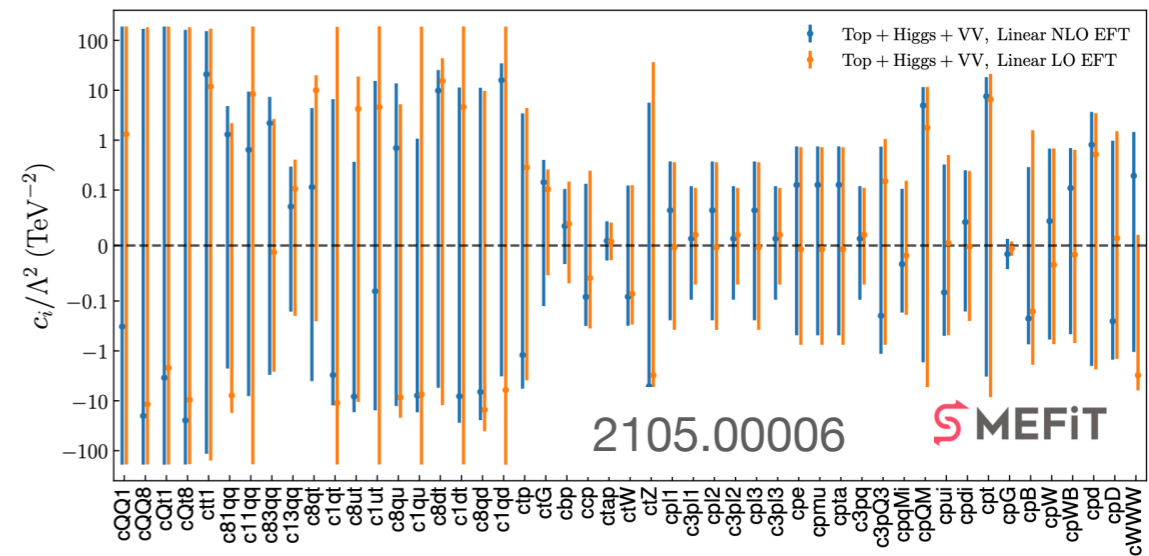
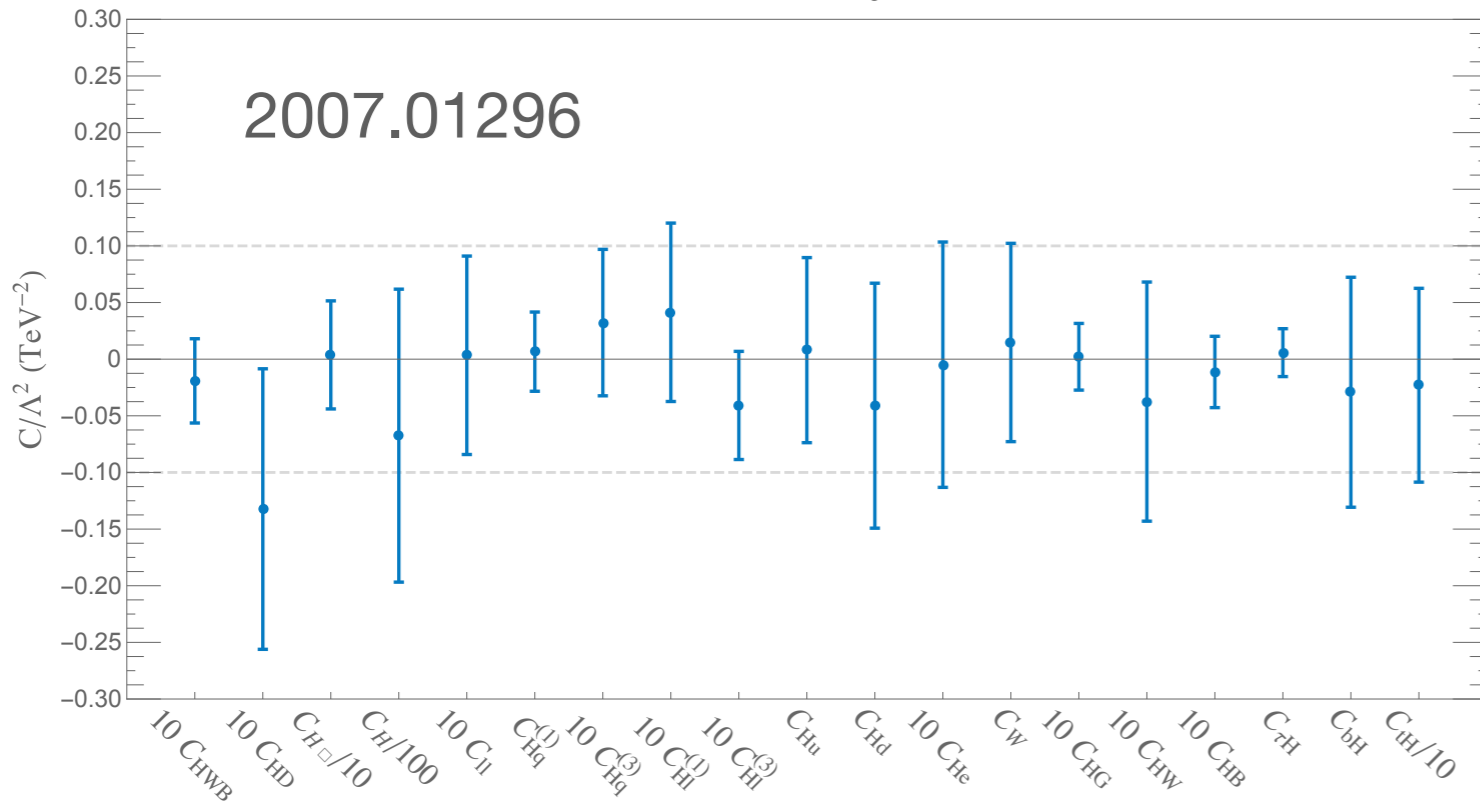
arXiv:2004.03447



CMS-PAS-HIG-19-005

# Lots of effort on SMEFT Global Fits:

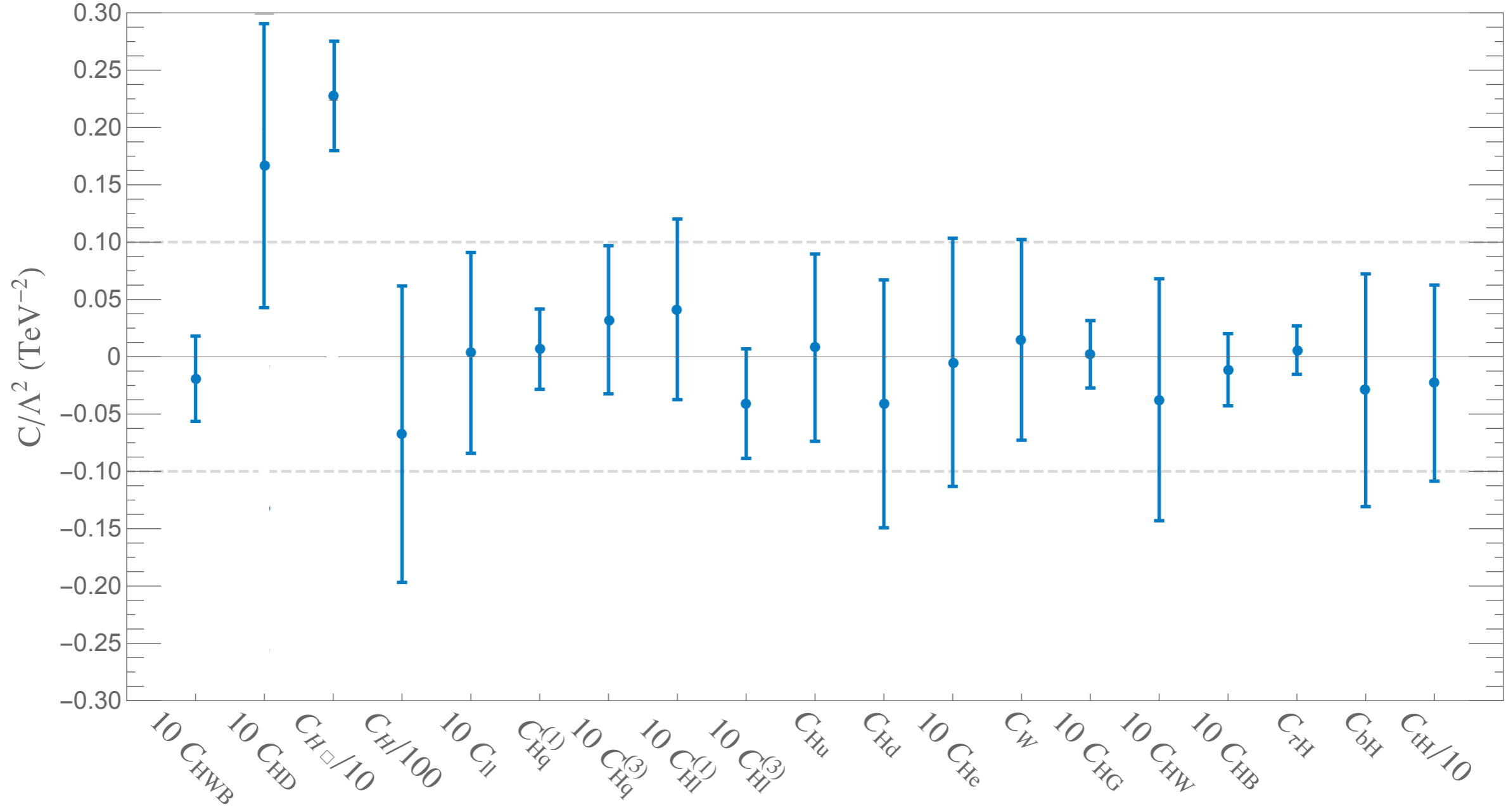
95% Limits, Projected



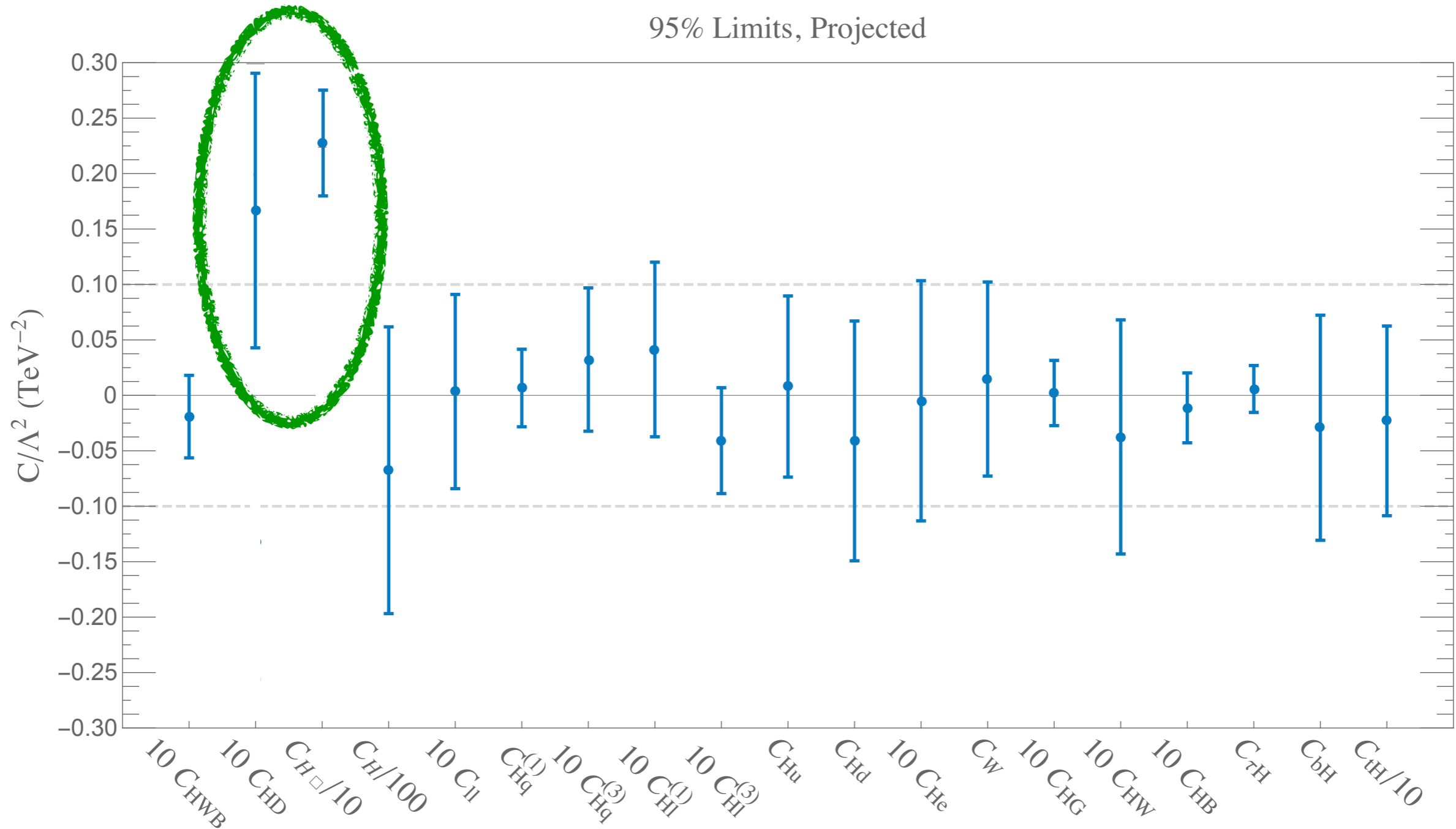
See also 1803.03252, 1812.01009, 1910.14012, 1911.07866, ...

# The Dream:

95% Limits, Projected



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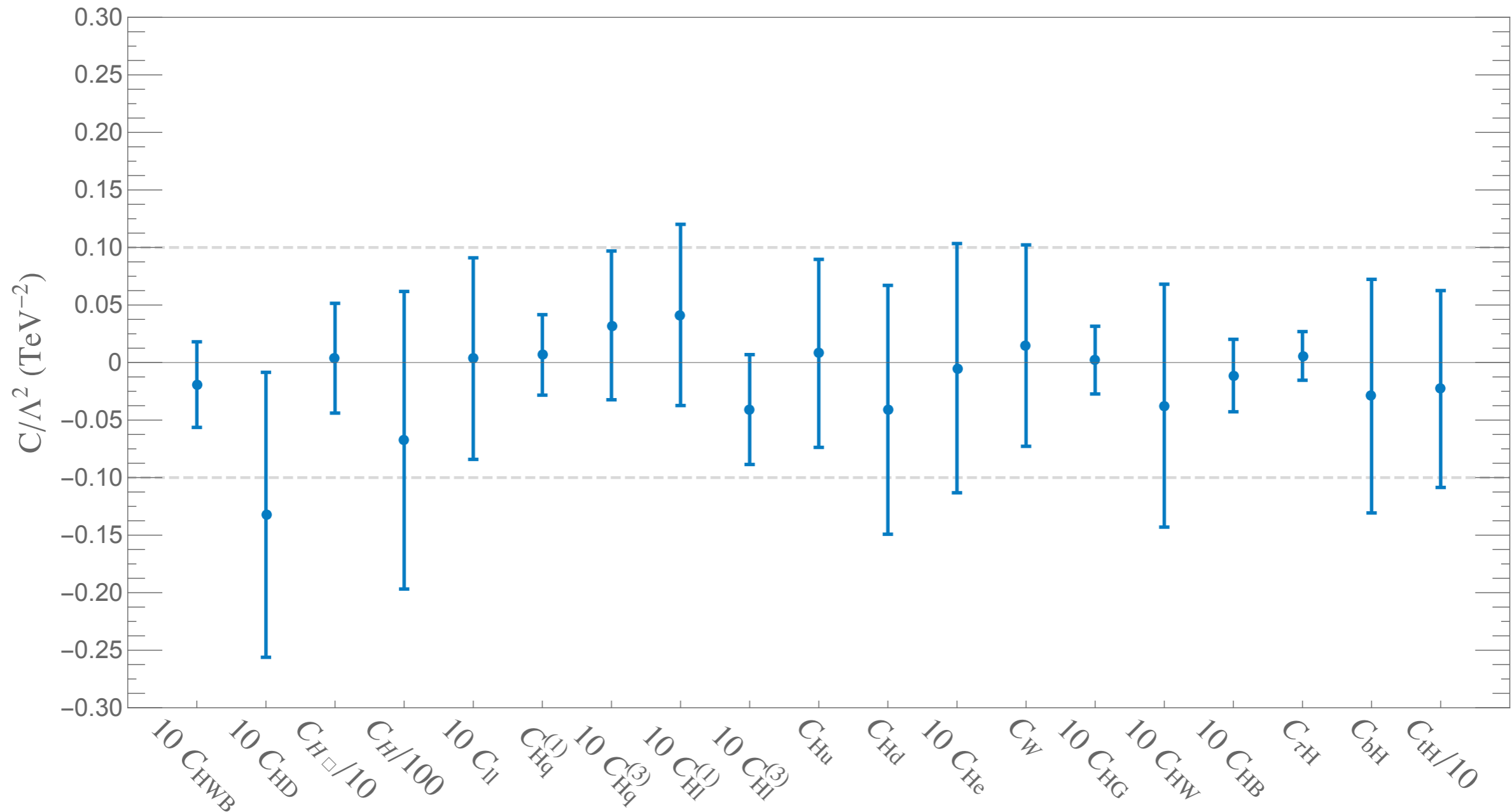


⇒ Start model building! Focussed searches, make sure we understand the SM, ...

# Alas...

(Though CDF may have different ideas...)

95% Limits, Projected



We are still learning a lot about the Standard Model!

# Beyond Tree Level Matching:

Lots of “higher-order” effects to consider:

- RG Evolution of Wilson Coefficients
- Linear vs. Quadratic Effects in  $(1 / \Lambda^2)$
- One-Loop Matching Effects
- Importance of Dimension-8 Operators
- Higher Order QCD / EW Corrections in the EFT  
See, e.g, Baglio, Dawson, SH, [arXiv:1909.11576](https://arxiv.org/abs/1909.11576),  
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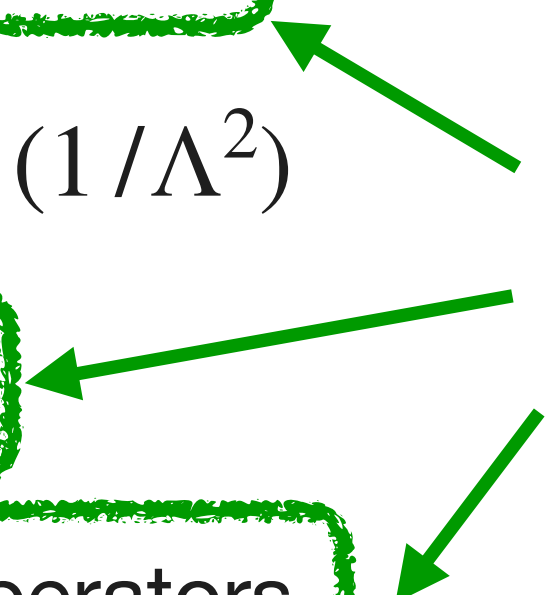
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One way to assess the importance of these effects is by evaluating them in the context of *concrete models*.

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Lots of interesting / challenging methodological questions:

- At what order do we truncate the amplitude / Lagrangian?
- What assumptions about flavor should we make to get a manageable set of operators?
- How should we account for EFT validity issues?
- ...

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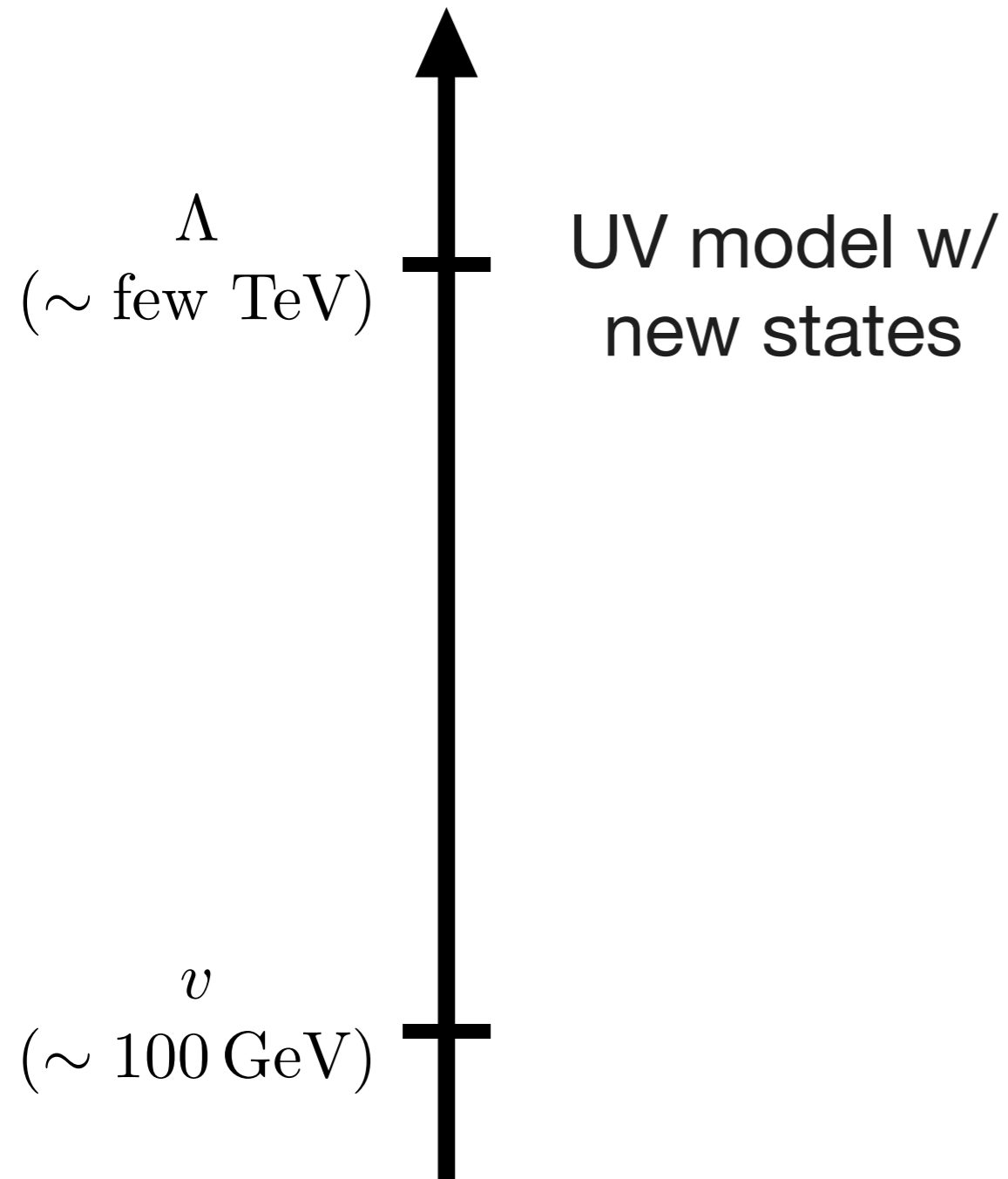
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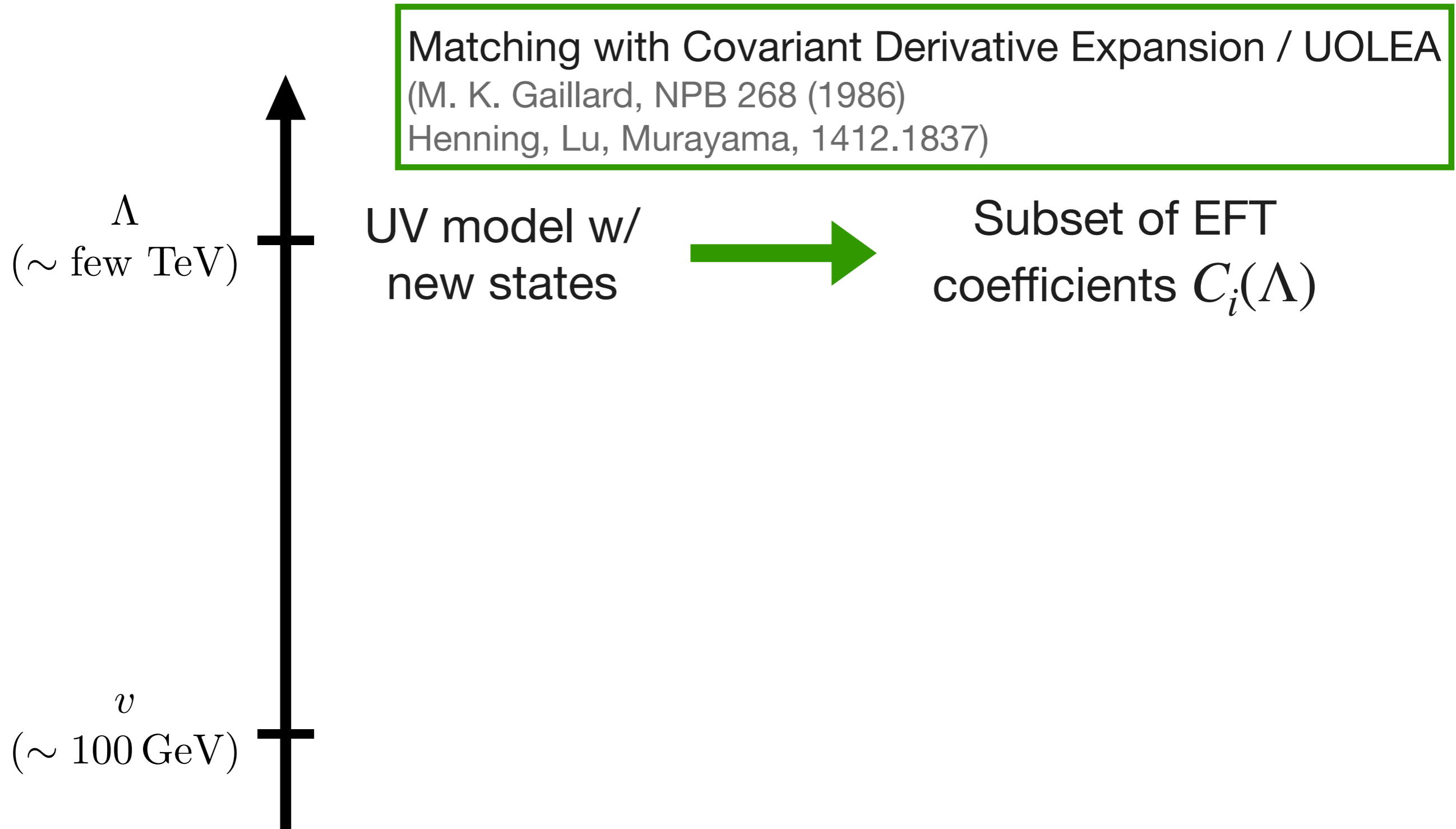
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- ...

No completely “model independent” answer to some of these questions... but they are easy to investigate in examples!

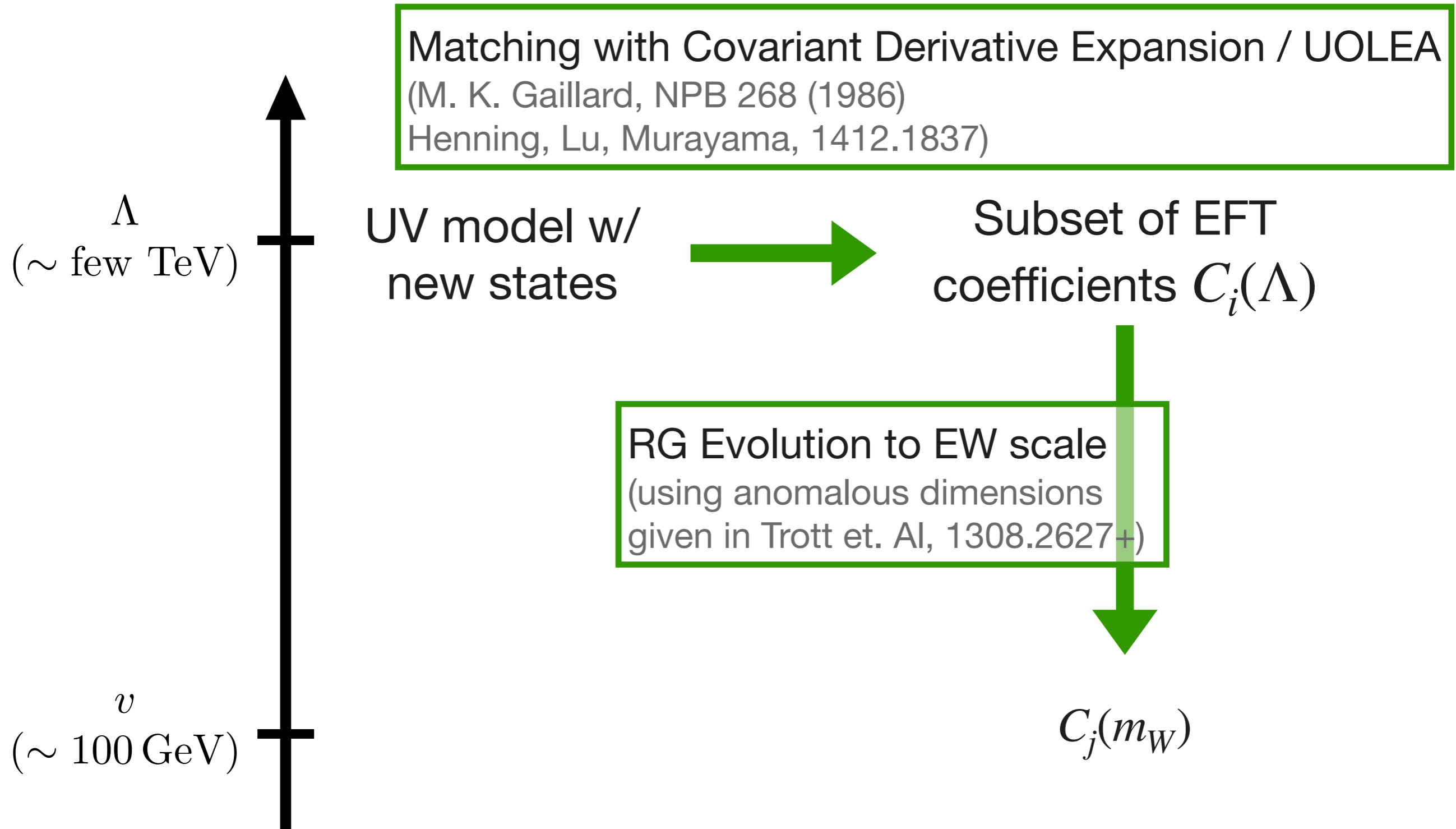
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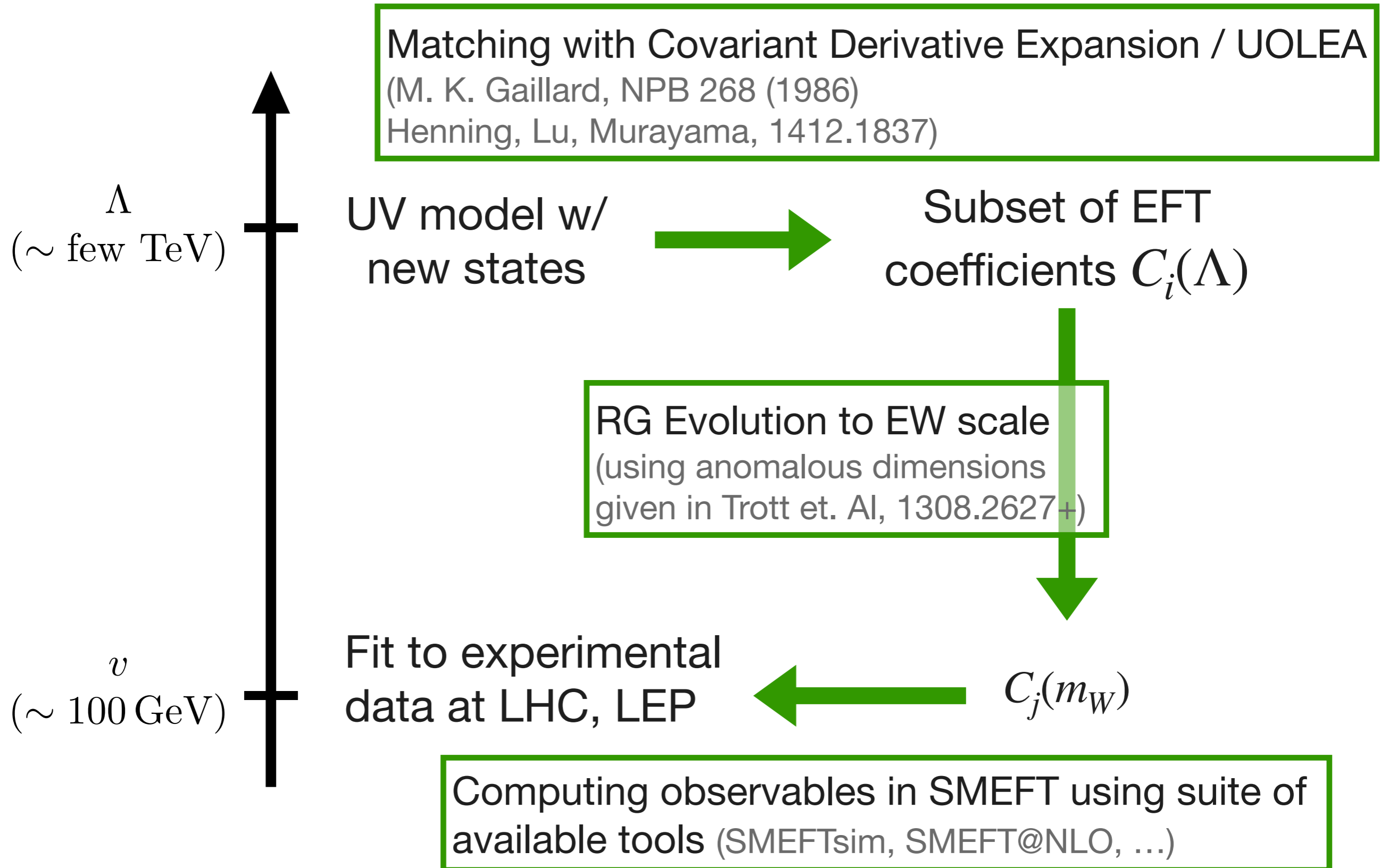


# Interpreting Models in the SMEFT





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# Example 1: the T VLQ Model

Extend the SM with a pair of SU(2) singlet,  $Q = 2/3$ , vector-like quarks (VLQs):

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Denoting the SM third generation as:

$$\psi_L = \begin{pmatrix} \mathcal{T}_L^1 \\ b_L \end{pmatrix}, \quad \mathcal{T}_R^1, \quad b_R$$

The most general Lagrangian can be written:

$$\begin{aligned} -\mathcal{L} = & \lambda_b \bar{\psi}_L H b_R + \lambda_t \bar{\psi} H^c \mathcal{T}_R^1 \\ & + m_{12} \bar{\mathcal{T}}_L^2 \mathcal{T}_R^1 + \lambda_T \bar{\psi}_L H^c \mathcal{T}_R^2 + m_T \bar{\mathcal{T}}_L^2 \mathcal{T}_R^2 + \text{h.c.} \end{aligned}$$

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Extend the SM with a pair of SU(2) singlet,  $Q = 2/3$ , vector-like quarks (VLQs):

$$\mathcal{T}_L^2, \quad \mathcal{T}_R^2$$

Denoting the SM third generation as:

$$\psi_L = \begin{pmatrix} \mathcal{T}_L^1 \\ b_L \end{pmatrix}, \quad \mathcal{T}_R^1, \quad b_R$$

The most general Lagrangian can be written:

$$-\mathcal{L} = \lambda_b \bar{\psi}_L H b_R + \lambda_t \bar{\psi} H^c \mathcal{T}_R^1 \quad \text{Heavy Dirac mass} \\ + \cancel{m_{12} \bar{\mathcal{T}}_L^2 \mathcal{T}_R^1} + \underbrace{\lambda_T \bar{\psi}_L H^c \mathcal{T}_R^2}_{\text{New Yukawa coupling}} + \underbrace{m_T \bar{\mathcal{T}}_L^2 \mathcal{T}_R^2}_{\text{Heavy Dirac mass}} + \text{h.c.}$$

Can be rotated away by  
redefinition of  $\mathcal{T}_R^{1,2}$

New Yukawa coupling  
(leads to mixing w/ SM top)

# Example 1: the T VLQ Model

Diagonalize the left- and right-handed tops to find physical eigenstates with masses  $m_t$  ( $= 173 \text{ GeV}$ ),  $M_T$

$$\begin{pmatrix} t \\ T \end{pmatrix}_{L,R} = \begin{pmatrix} \cos \theta_{L,R} & -\sin \theta_{L,R} \\ \sin \theta_{L,R} & \cos \theta_{L,R} \end{pmatrix} \begin{pmatrix} \mathcal{T}^1 \\ \mathcal{T}^2 \end{pmatrix}_{L,R}$$

Three physical parameters:  $m_t, M_T, \sin \theta_L$   $\tan \theta_R = \frac{m_t}{M_T} \tan \theta_L$   
(Alternatively,  $\lambda_t, \lambda_T, m_{\mathcal{T}}$ )

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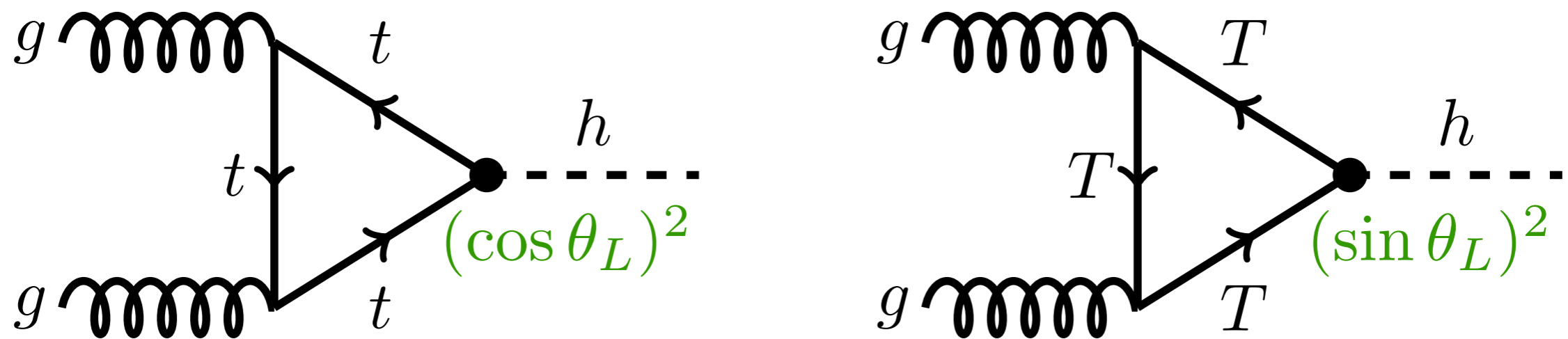
Note: expansions in  $M_T$  and  $m_{\mathcal{T}}$  have different counting in inverse mass dimension for fixed  $\sin \theta_L$

$$\frac{1}{m_{\mathcal{T}}^2} = \frac{1}{M_T^2} + \frac{s_L^2}{M_T^2} \left( 1 - \frac{m_t^2}{M_T^2} \right)$$

We match at  $m_{\mathcal{T}}$ , see however Brehmer, Freitas, Lopez-Val, Plehn [1510.03443]

# T VLQ Pheno: Higgs Production

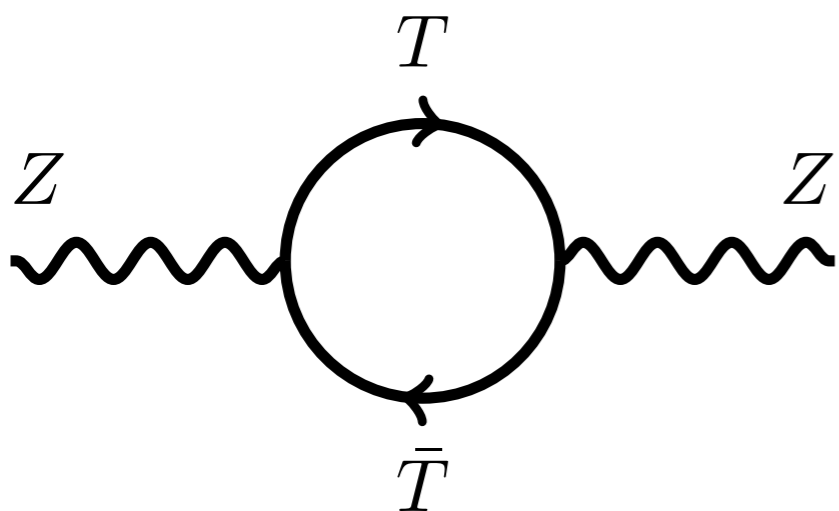
Chiral fourth generation is completely excluded by Higgs production, but what about vector-like pairs?



In the limit  $m_H \ll m_t, M_T$  the ggh amplitude is unchanged!

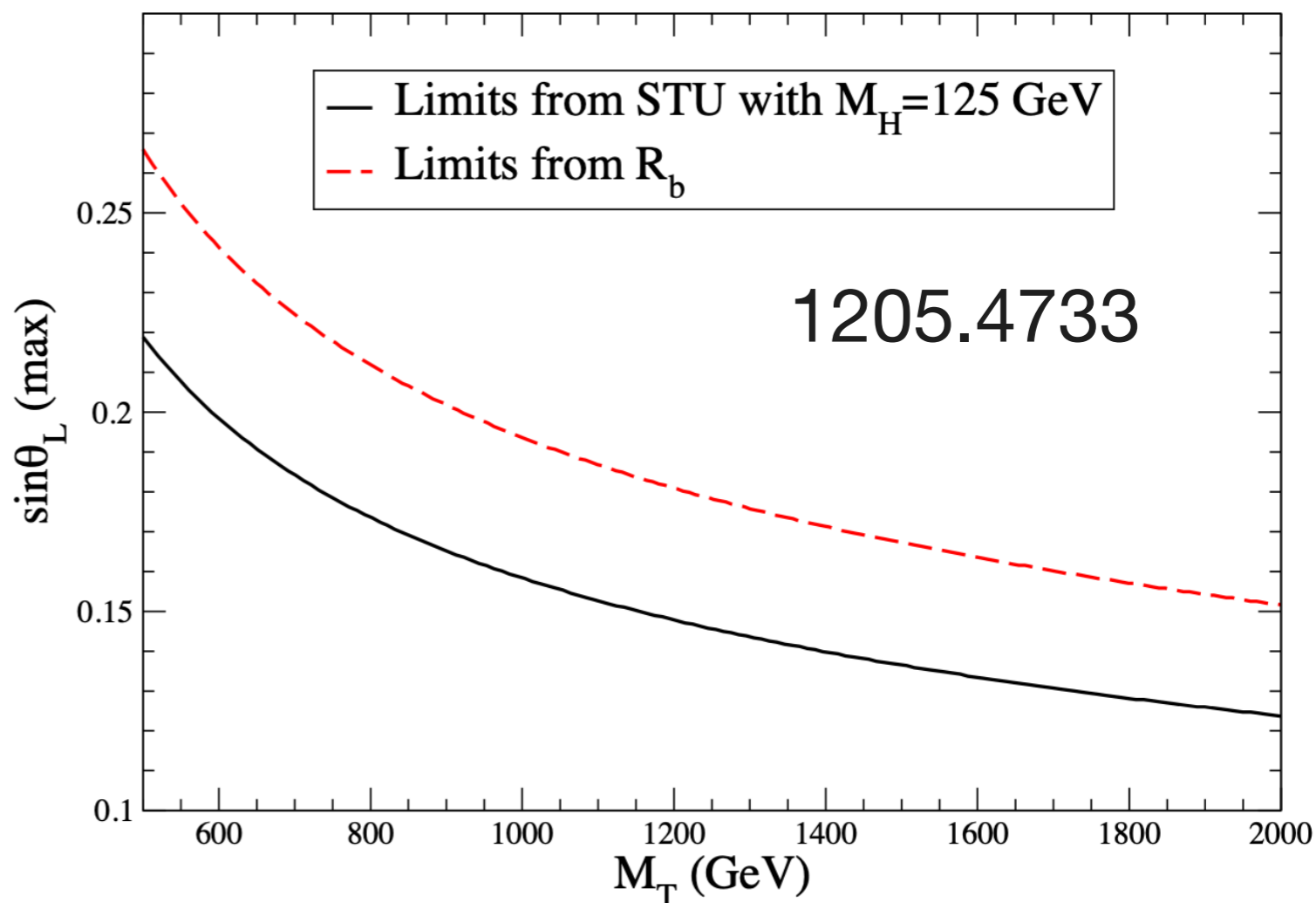
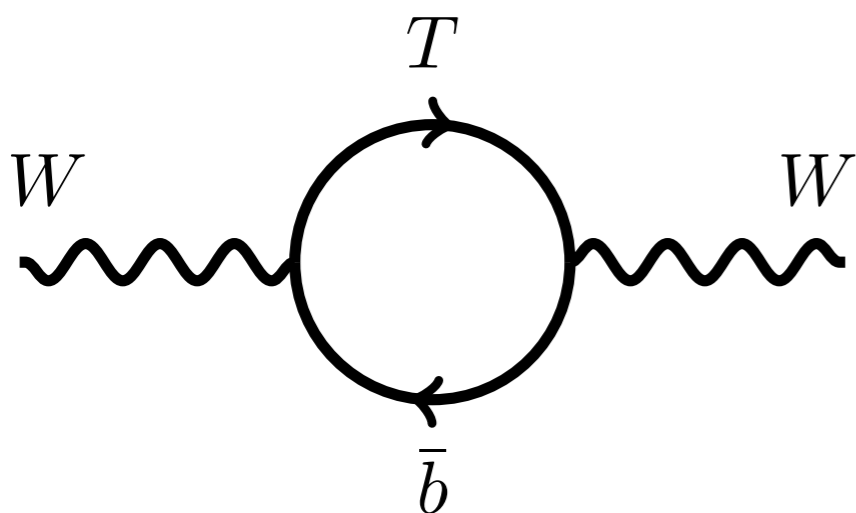
(this is a reasonably good approximation, compare to e.g.,  $m_t \rightarrow \infty$  limit for Higgs production...)

# T VLQ Pheno: EW Precision



$$\Delta T = s_L^2 \left[ - (1 + c_L^2) + s_L^2 \frac{M_T^2}{m_t^2} + 2c_L^2 \log \left( \frac{M_T^2}{m_t^2} \right) \right] T_{\text{SM}}$$

$$\Delta S = -\frac{s_L^2}{6\pi} \left[ 5c_L^2 + (1 - 3c_L^2) \log \left( \frac{M_T^2}{m_t^2} \right) \right] S_{\text{SM}}$$



Also limits from unitarity,  
perturbativity of  $\lambda_T$

see e.g., Dawson, Furlan [1205.4733],  
Dawson, Furlan, Chen [1703.06134]

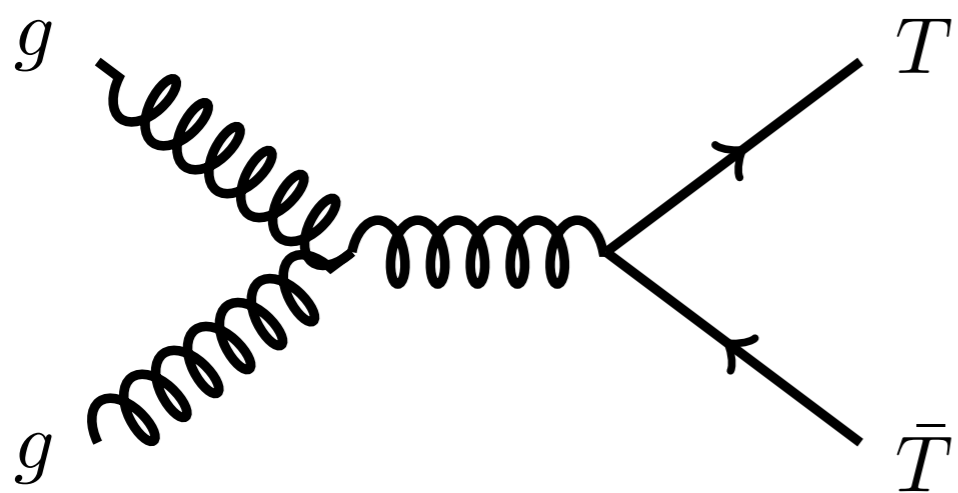


# T VLQ Pheno: Direct Searches

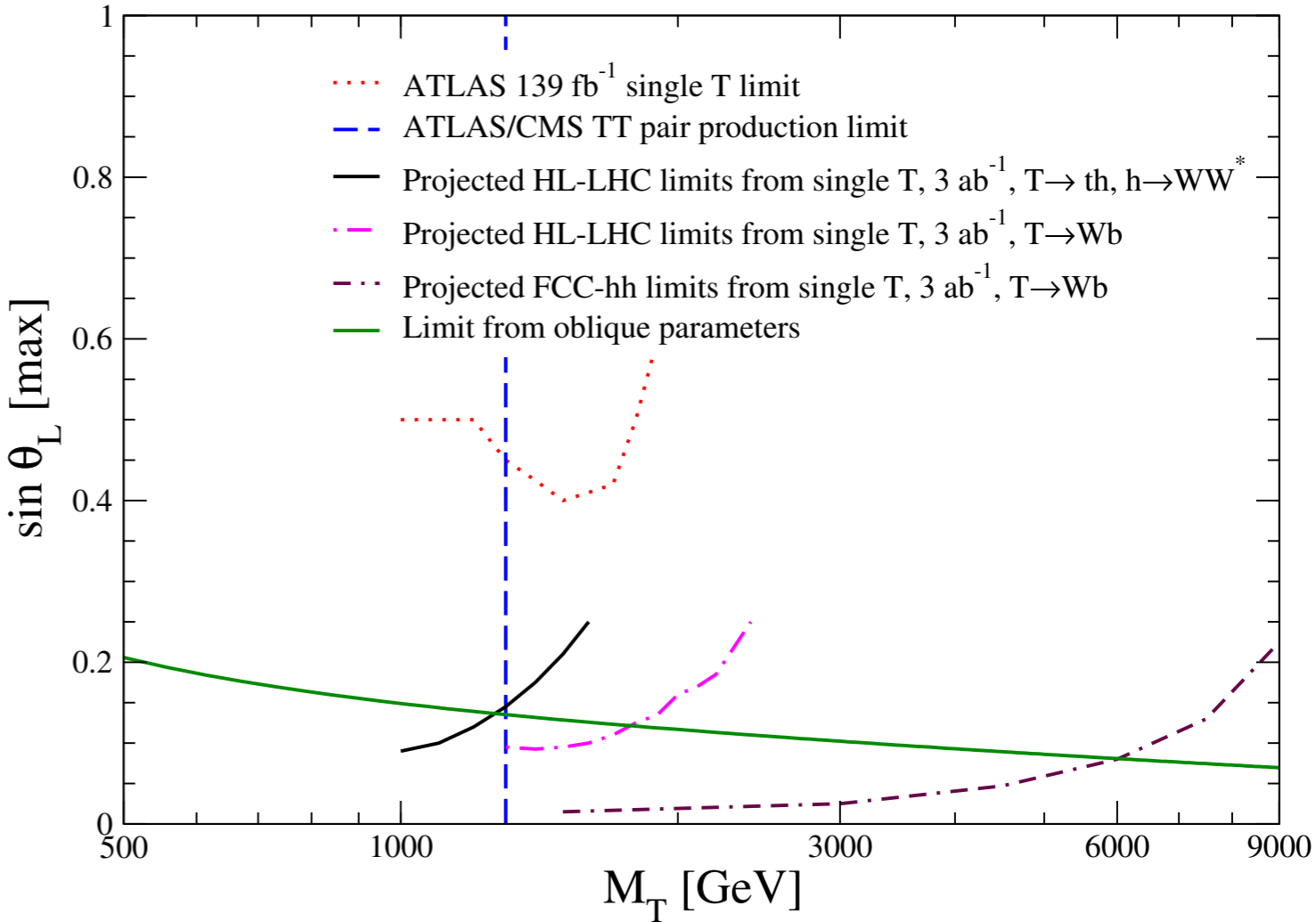
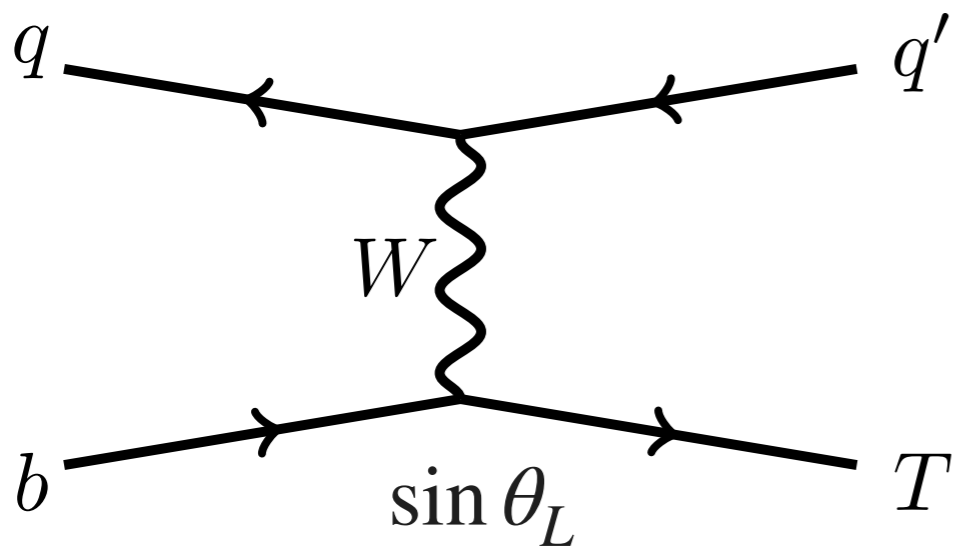
TVLQ Model

95% C.L. limits

Pair production:



Single-production:



VLQs must be heavier than  $\sim 1.7$  TeV, independent of mixing angle!

$\implies$  Ideal candidate for SMEFT!

# T VLQ in the SMEFT

## Dimension-6 Matching

Using Eqns. of motion (CDE) to integrate out the heavy Top, we have at dimension-6:

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \frac{i}{2} \frac{\lambda_T^2}{m_T^2} \bar{\psi}_L H^c \not{D} (H^{c\dagger} \psi_L) + \text{h.c.} + \dots$$

New interactions + non-canonical kinetic term

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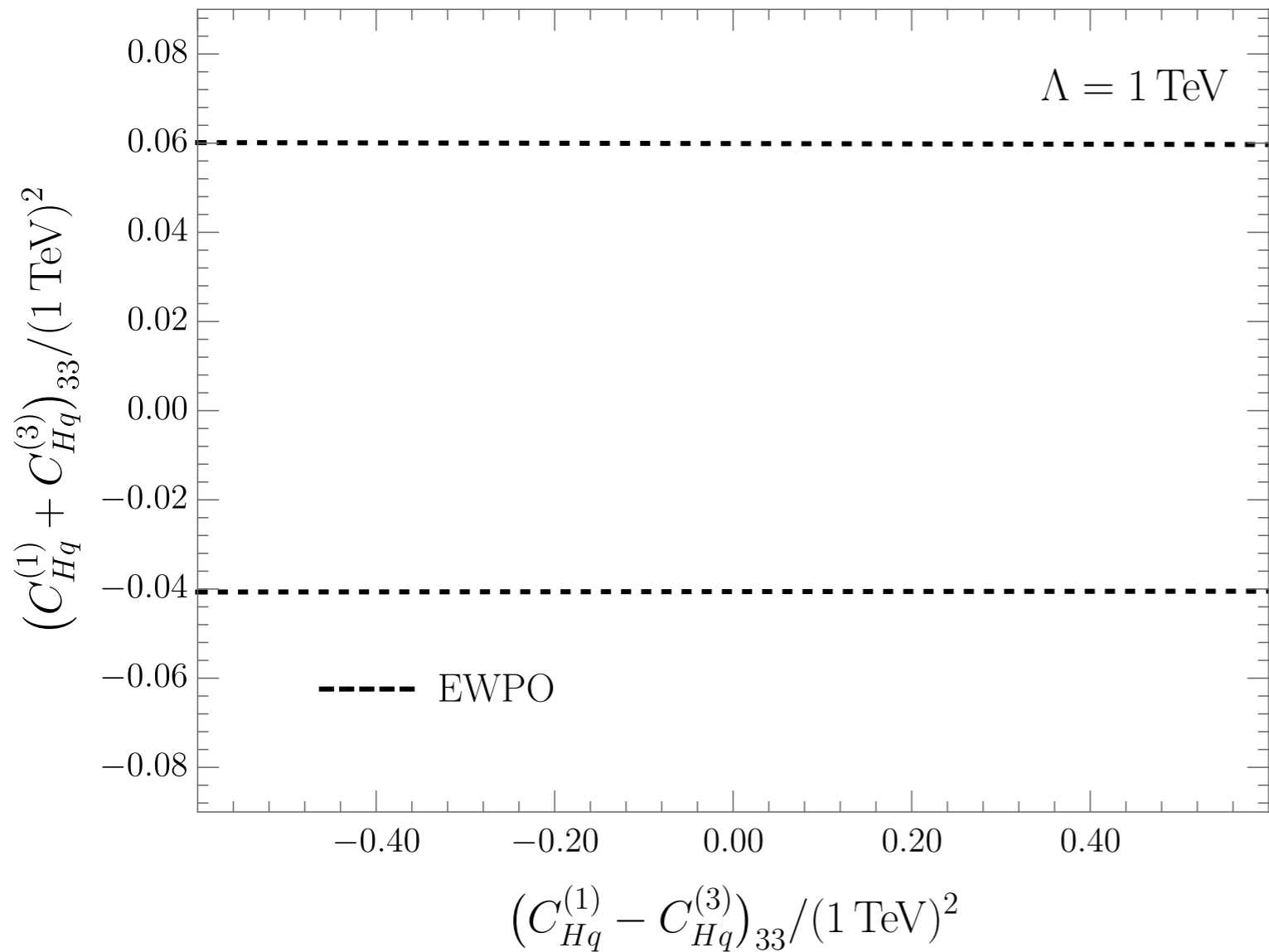
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Note: all dim-6 corrections scale like  $(\lambda_T/m_{\mathcal{T}})^2$ !

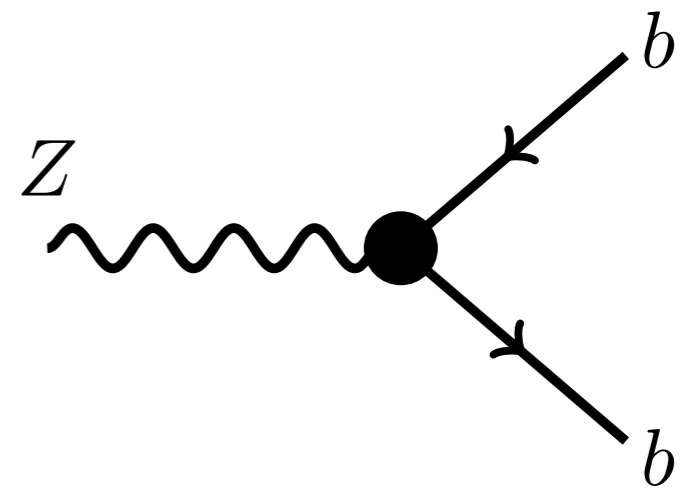
# T VLQ in the SMEFT

## LEP Constraints: Tree Level



At tree level, only one way to measure operators

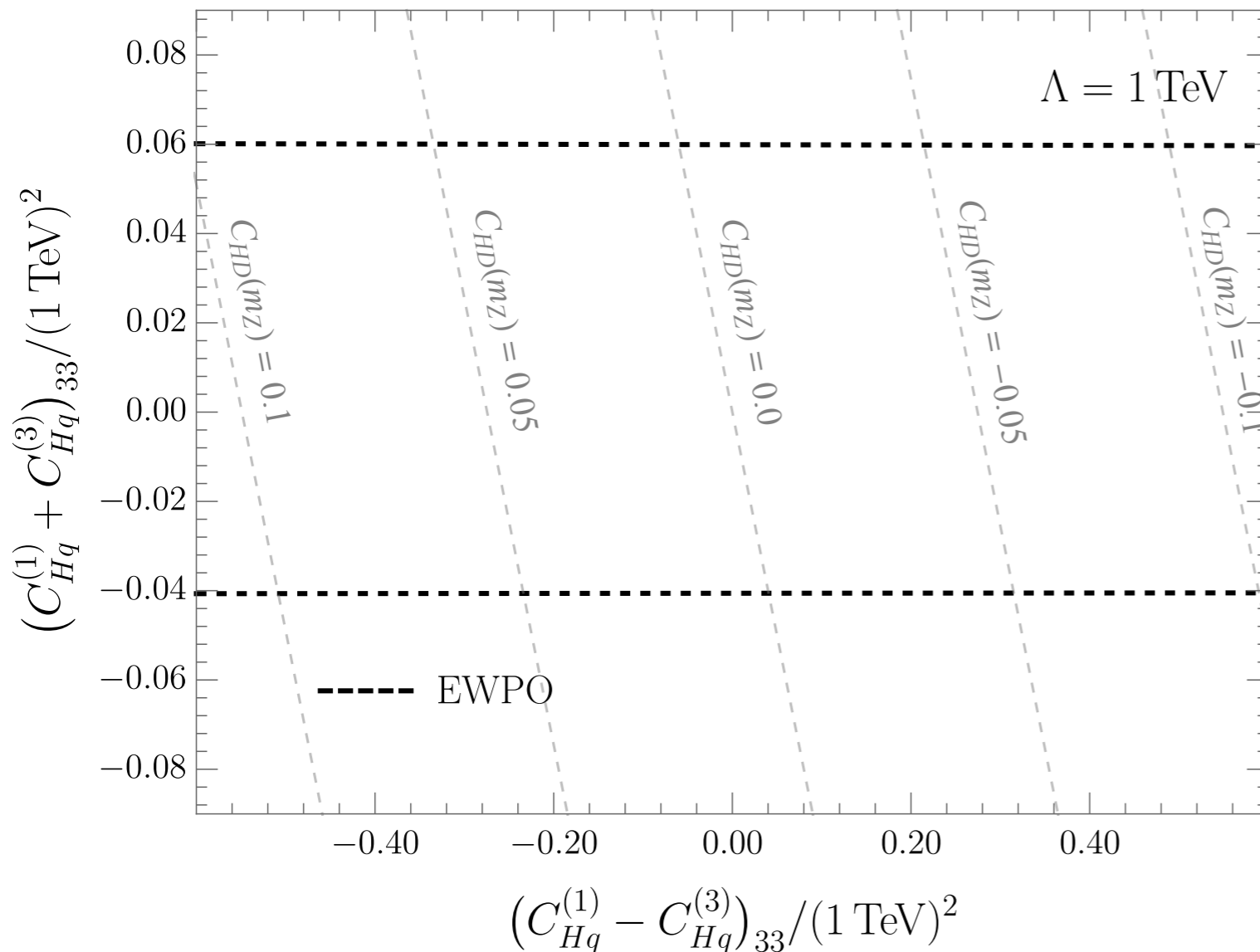
$$C_{Hq,33}^{(1)}, C_{Hq,33}^{(3)}$$



$Z \rightarrow b\bar{b}$  branching ratio  
constrains **one** combination  
of operators.

# T VLQ in the SMEFT

LEP Constraints: RGE-Induced

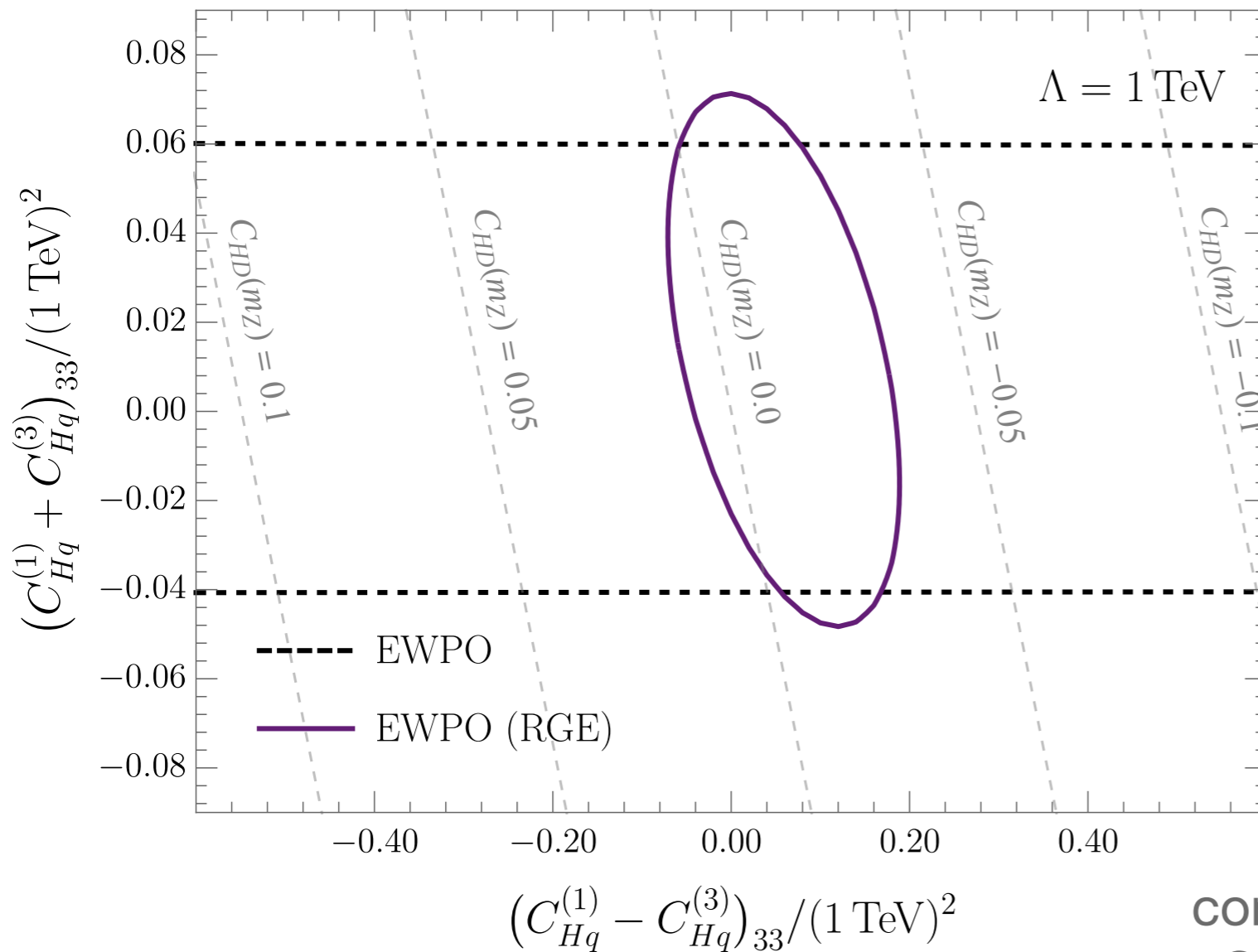


But if we evolve the operators down to the weak scale...

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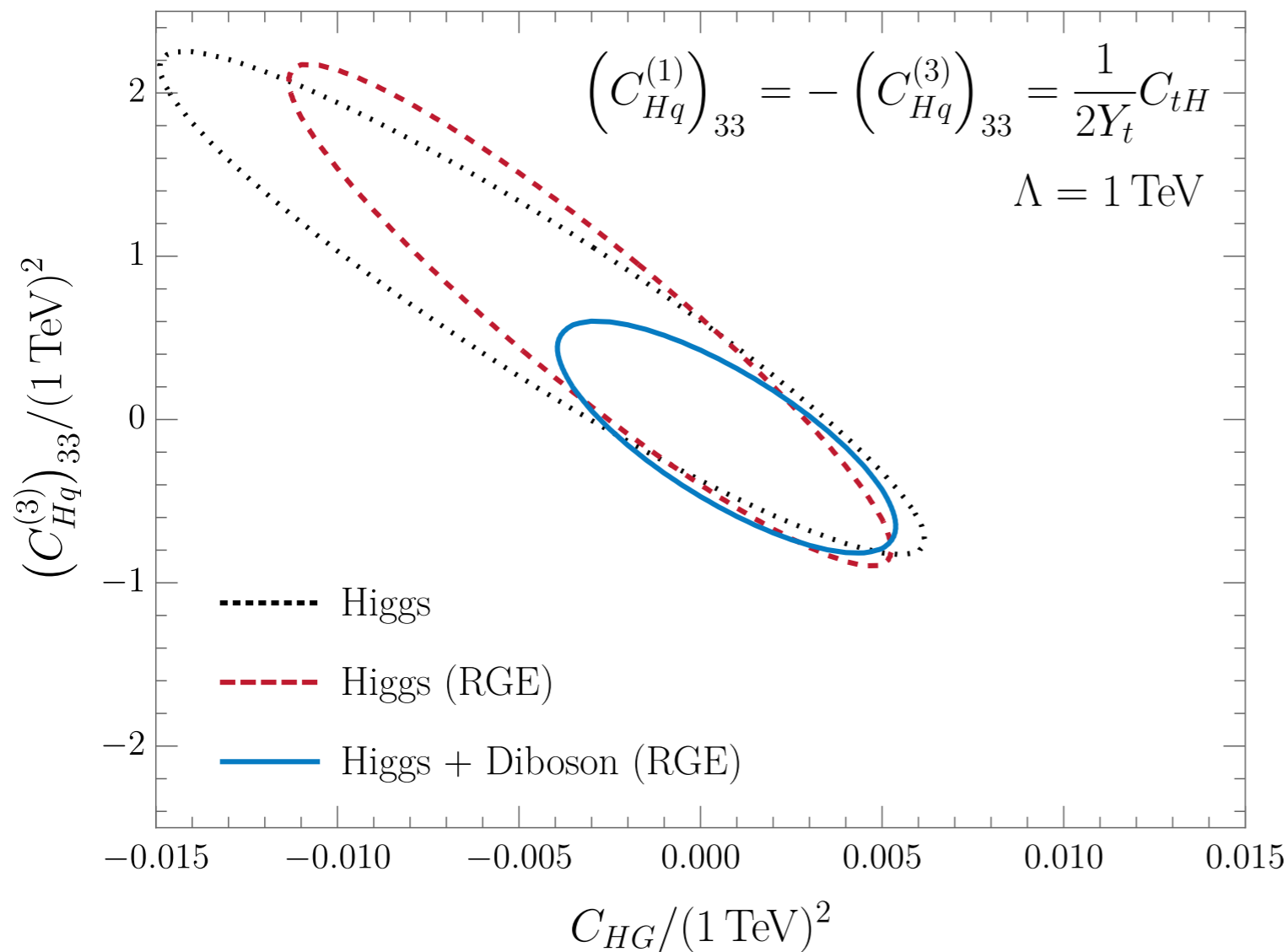
(Well understood in UV theory — constraints from oblique parameters, e.g., Chen, Dawson, Furlan, [arXiv:1406.3349](https://arxiv.org/abs/1406.3349))



# T VLQ in the SMEFT

LHC Constraints: Tree-Level + RGEs

Similar lessons apply to LHC bounds:



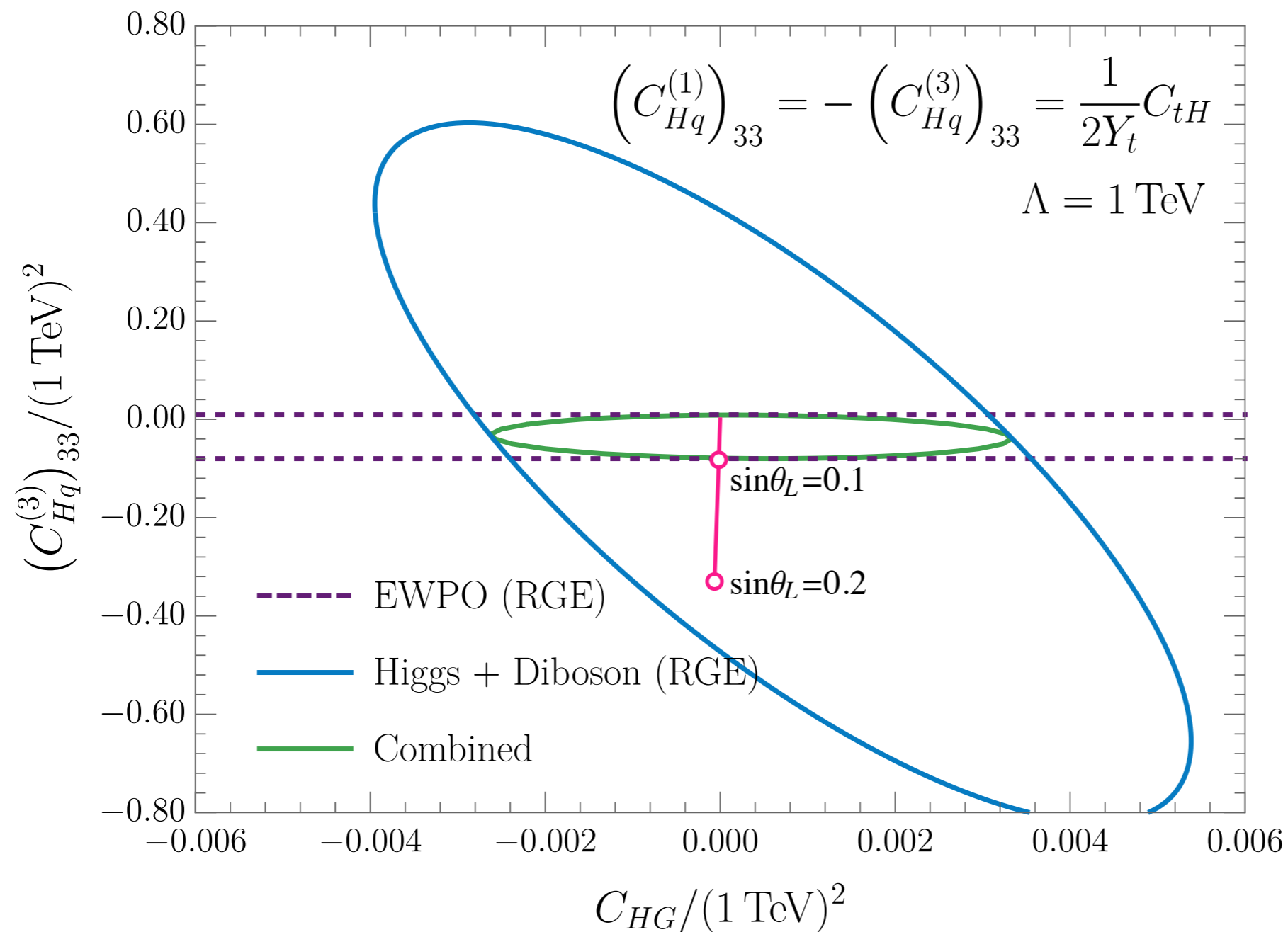
But RG evolution also generates *new* operators measured at the LHC in  $WW$ ,  $WZ$ ,  $WH$ ,  $ZH$  production!

Strongest LHC constraint from RGEs!

Note: NLO-QCD effects are *very* important for diboson limits (see [arXiv:1909.11576](https://arxiv.org/abs/1909.11576), [arXiv:2003.07862](https://arxiv.org/abs/2003.07862))

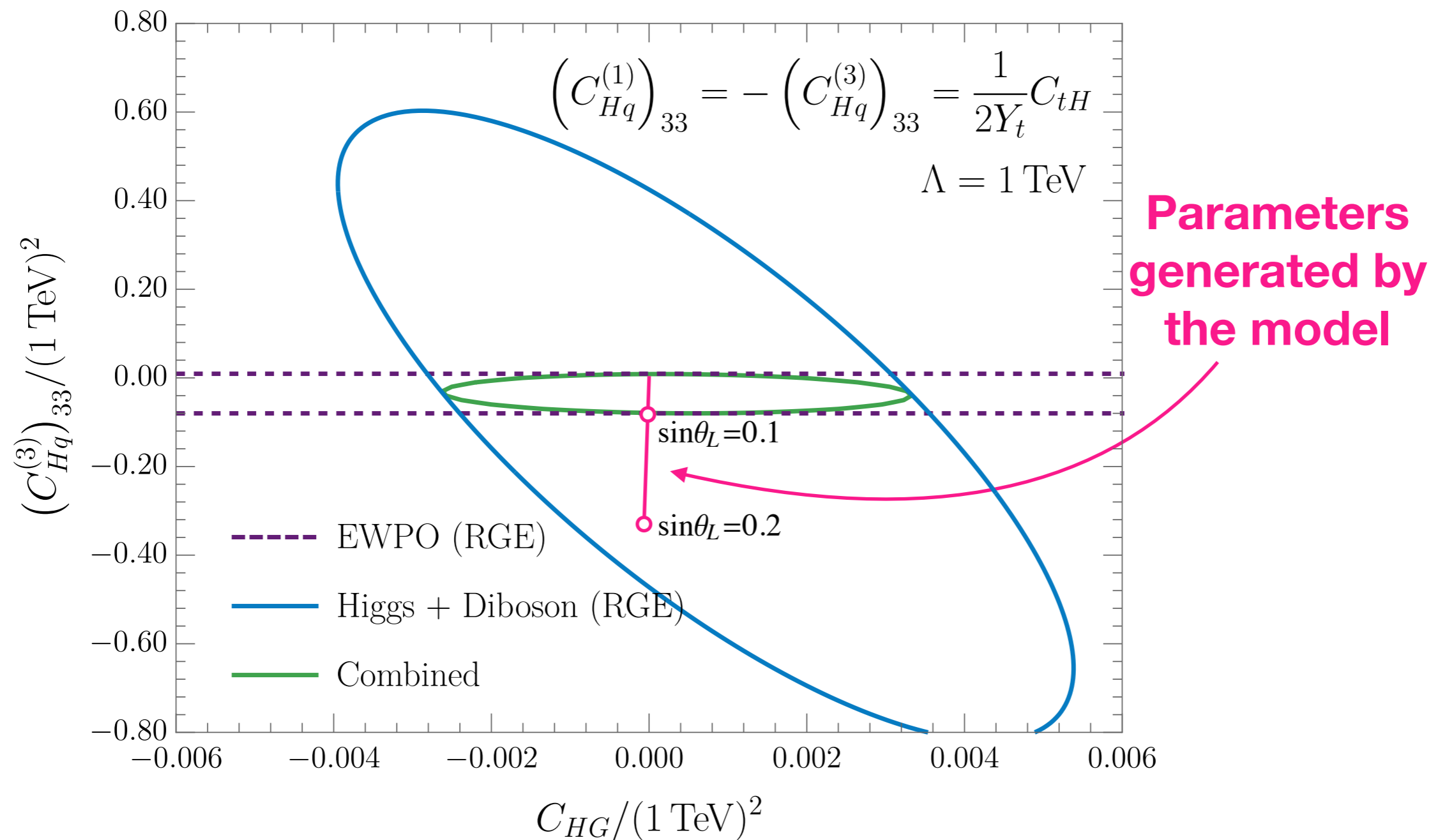
# T VLQ in the SMEFT

Combined Constraints: a Constrained SMEFT Fit



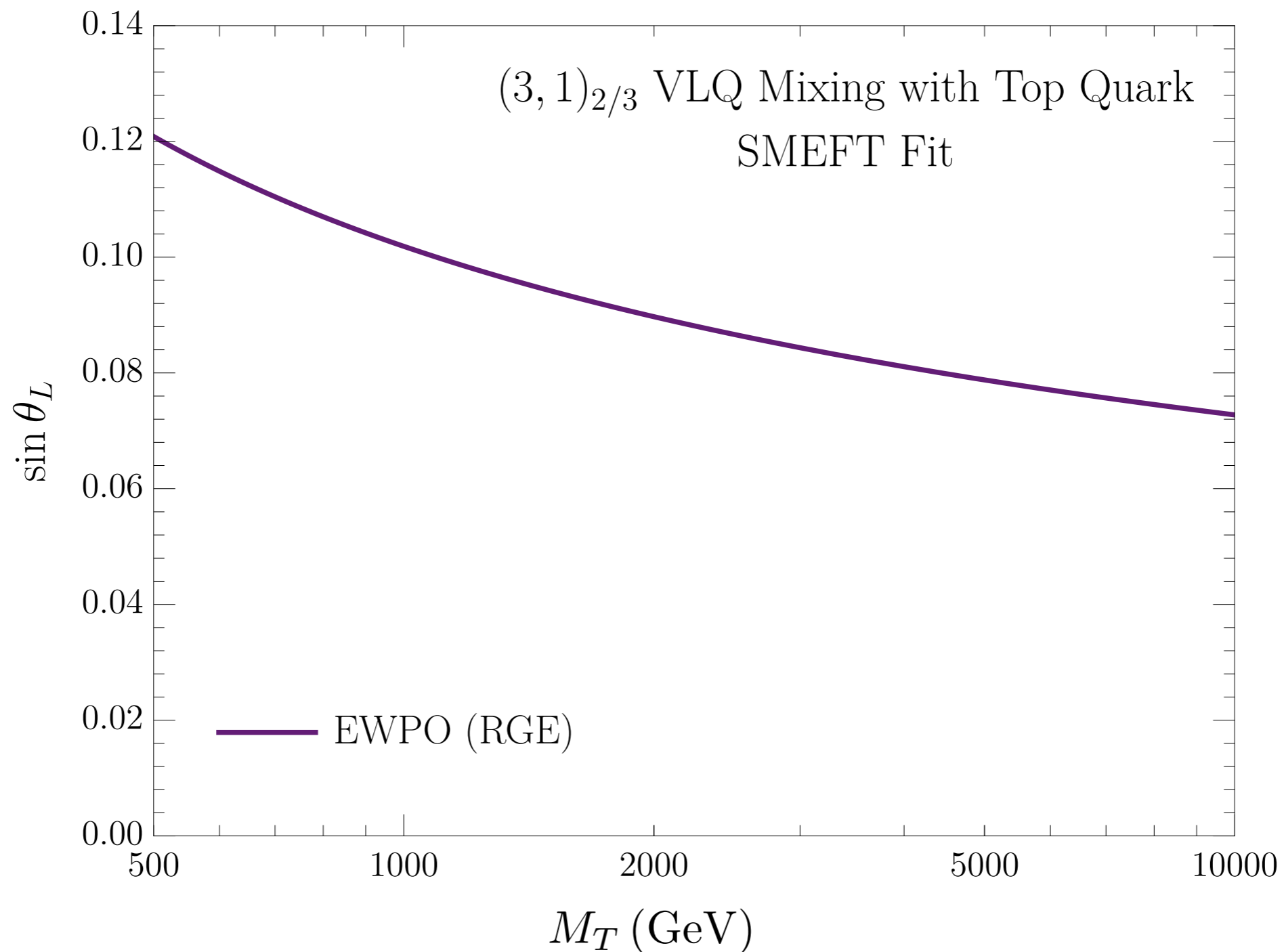
# T VLQ in the SMEFT

Combined Constraints: a Constrained SMEFT Fit



# T VLQ in the SMEFT

Re-Interpretation in terms of model parameters



# Is Dimension-6 Fit Sufficient?

Expanding an arbitrary observable in powers of  $1/\Lambda^2$ :

$$\begin{aligned} d\sigma &\sim \left| \mathcal{A}_{\text{SM}} + \frac{1}{\Lambda^2} \mathcal{A}_6 + \frac{1}{\Lambda^4} \mathcal{A}_8 + \dots \right|^2 \\ &\sim |\mathcal{A}_{\text{SM}}|^2 + \frac{2}{\Lambda^2} \text{Re}|\mathcal{A}_{\text{SM}}^* \mathcal{A}_6| + \frac{1}{\Lambda^4} |\mathcal{A}_6|^2 + \frac{2}{\Lambda^4} \text{Re}|\mathcal{A}_{\text{SM}}^* \mathcal{A}_8| + \dots \end{aligned}$$

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But if we keep the dim-6 squared terms, linear terms at dim-8 are of the same order....

Several pheno studies including dim-8 terms, finding sometimes significant effects:

- Hays, Martin, Sanz, Setford ( $WH$  production) [1808.00442]
- Grazzini et al, Battaglia et al, ( $H + \text{jet}$  production) [1612.00283, 2109.02987]
- Corbett, Helset, Martin, Trott (EWPO) [2102.02819]

# T VLQ Matched to Dimension-8

arXiv:2110.06948, Dawson, SH, Sullivan

Perform the matching by continuing the CDE:

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \frac{i}{2} \frac{\lambda_T^2}{m_{\mathcal{T}}^2} \bar{\psi}_L H^c \not{D} (H^{c\dagger} \psi_L) + \text{h.c.} + \dots$$

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The necessary field redefinition is unchanged,

$$\psi_{L,i} \rightarrow \psi_{L,i} - \frac{\lambda_T^2}{2m_{\mathcal{T}}^2} (H_i^c H_j^{c\dagger}) \psi_{L,j} + \dots$$

... but now must be included in the dim-6 operators as well.

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After repeated use of the EOMs:

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \mathcal{L}_6 + \frac{\lambda_t \lambda_T^2}{8m_{\mathcal{T}}^4} (4\lambda_t^2 - 3\lambda_T^2) \underbrace{(H^\dagger H)^2 \bar{\psi}_L H^c t_R}_{\mathcal{O}_{quH^5}^{(8)}} + \dots$$

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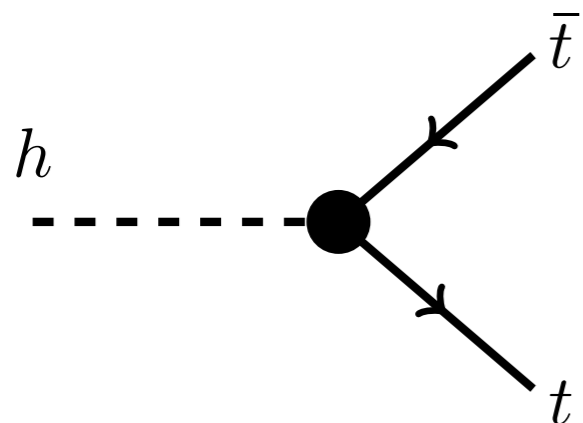
Also additional momentum-dependent interactions, and interactions with gluons:

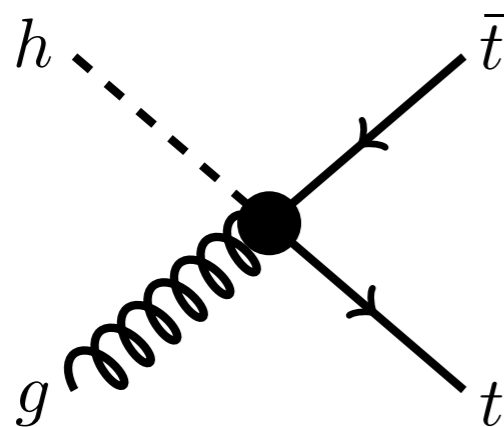
$$\begin{aligned} &+ i \frac{\lambda_T^2}{m_{\mathcal{T}}^4} (\bar{\psi}_L D^\mu H^c) \gamma_\mu (D^\nu H^{c\dagger} D_\nu \psi_L) + i \frac{\lambda_T^2}{m_{\mathcal{T}}^4} (\bar{\psi}_L H^c) \gamma_\mu (D^\mu D^\nu H^{c\dagger} D_\nu \psi_L) \\ &- i \frac{\lambda_T^2}{m_{\mathcal{T}}^4} (\bar{\psi}_L H^c) \gamma_\mu (D^\nu D^\mu H^{c\dagger} D_\nu \psi_L) - \frac{\lambda_t \lambda_T^2}{m_{\mathcal{T}}^4} (H^\dagger H) \bar{t}_R (D^\mu H^{c\dagger} D_\mu \psi_L) + \text{h.c.} + \dots \end{aligned}$$

# T VLQ Matched to Dimension-8

arXiv:2110.06948, Dawson, SH, Sullivan

New, momentum-dependent interactions:


$$= -i \frac{Y_t^{(8)}}{\sqrt{2}} + i \frac{\lambda_T^2 v m_t}{4m_{\mathcal{T}}^4} (p_t - p_{\bar{t}}) \cdot p_h (P_L - P_R)$$


$$= i g_s T^A \frac{\lambda_T^2 v m_t}{2m_{\mathcal{T}}^4} p_h^\mu (P_L - P_R)$$

Also new  $tbW$ ,  $tbWh$ , interactions, and interactions with more Higgses...

Complete set of interactions implemented in FeynRules model.



# T VLQ Matched to Dimension-8

arXiv:2110.06948, Dawson, SH, Sullivan

Clearest effect at dim-8 is the change in the top Yukawa:

$$Y_t^{(8)} = \frac{m_t \sqrt{2}}{v} \left( 1 - \frac{\lambda_T^2 v^2}{2m_T^2} - \frac{m_t^2 v^2 \lambda_T^2}{m_T^4} + \frac{\lambda_T^4 v^4}{4m_T^4} \right)$$

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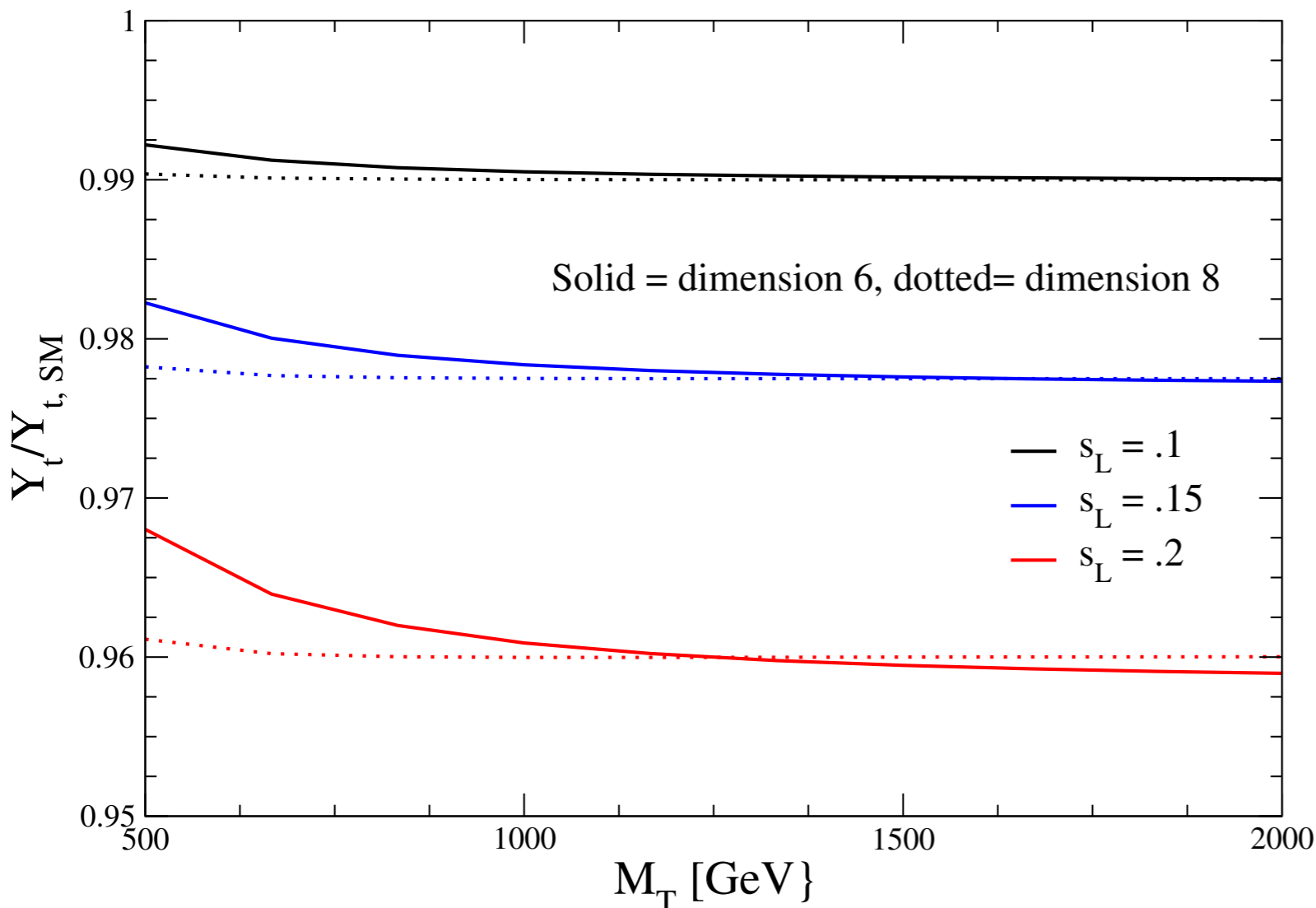
Again see the difference  
in counting in  $\lambda_T/m_\tau$

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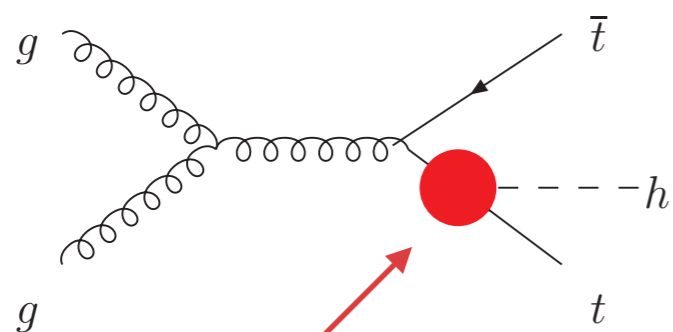
# Impact of Dim-8 Terms: $t\bar{t}h$ Production

arXiv:2110.06948, Dawson, SH, Sullivan

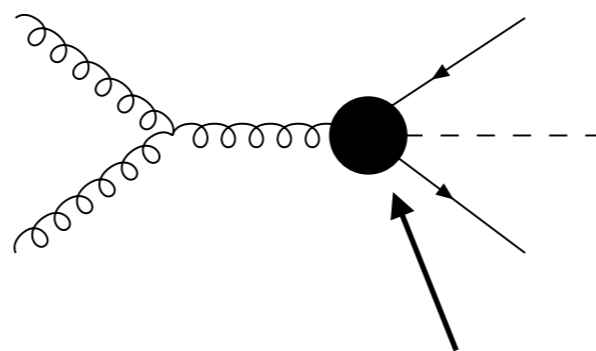
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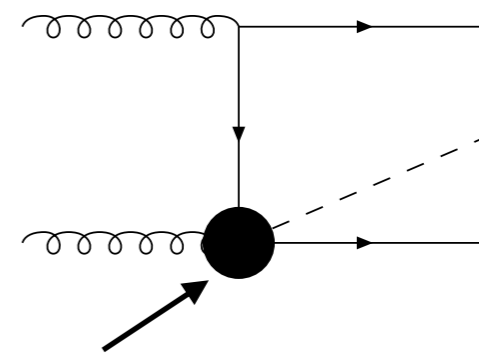
Implement full set of interactions in FeynRules, simulate  $t\bar{t}h$  production in MadGraph:



Insertion of dim-6 or dim-8



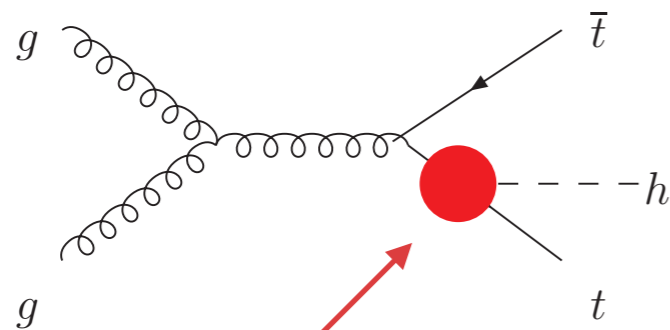
Appear only at dim-8 —  $s$ -enhanced!



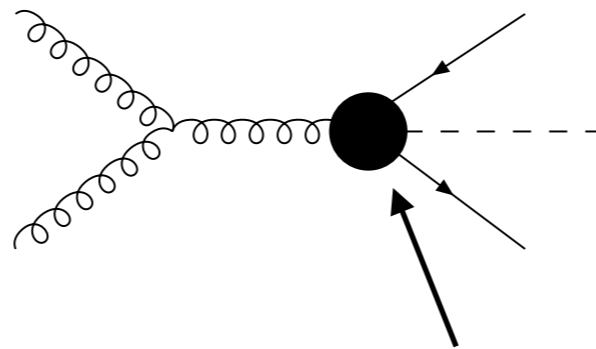
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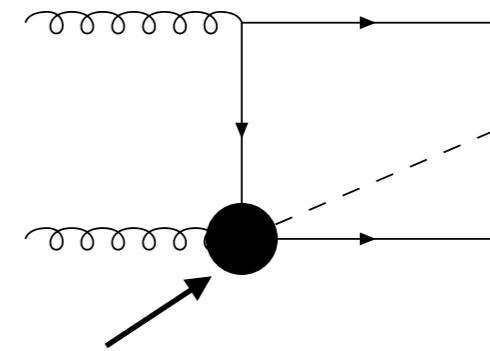
Implement full set of interactions in FeynRules, simulate  $t\bar{t}h$  production in MadGraph:



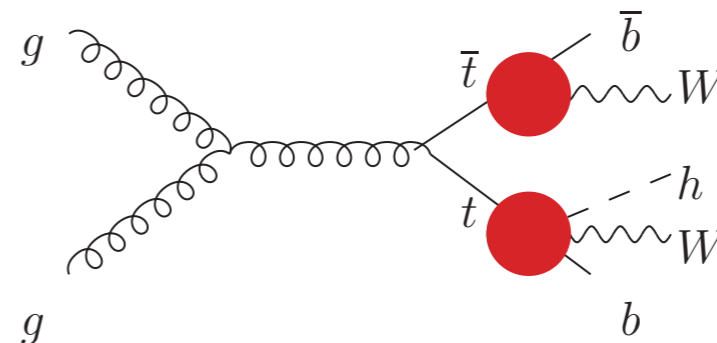
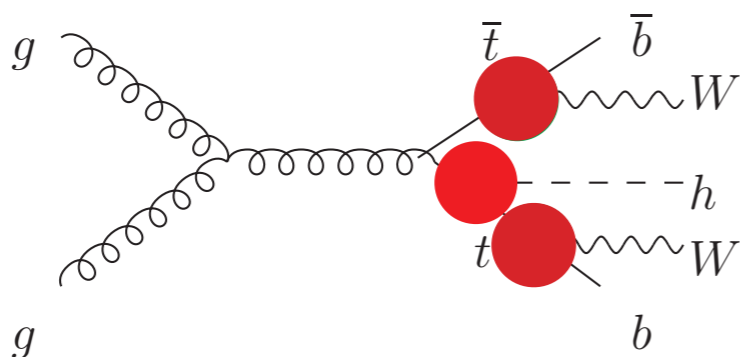
Insertion of dim-6 or dim-8



Appear only at dim-8 —  $s$ -enhanced!

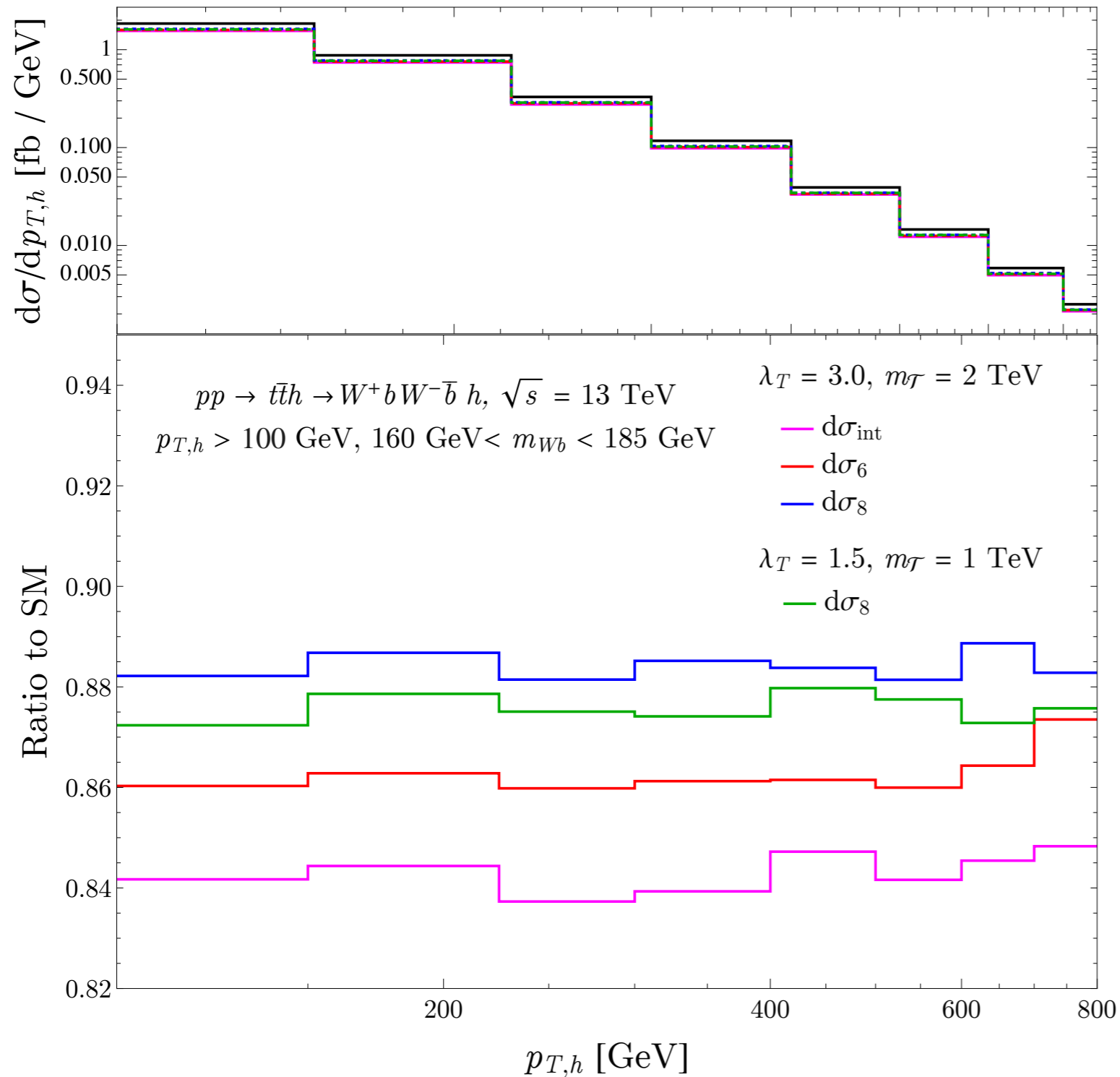


Important to also include decays, including corrections to  $tbWh$  vertex:



# Impact of Dim-8 Terms: $t\bar{t}h$ Production

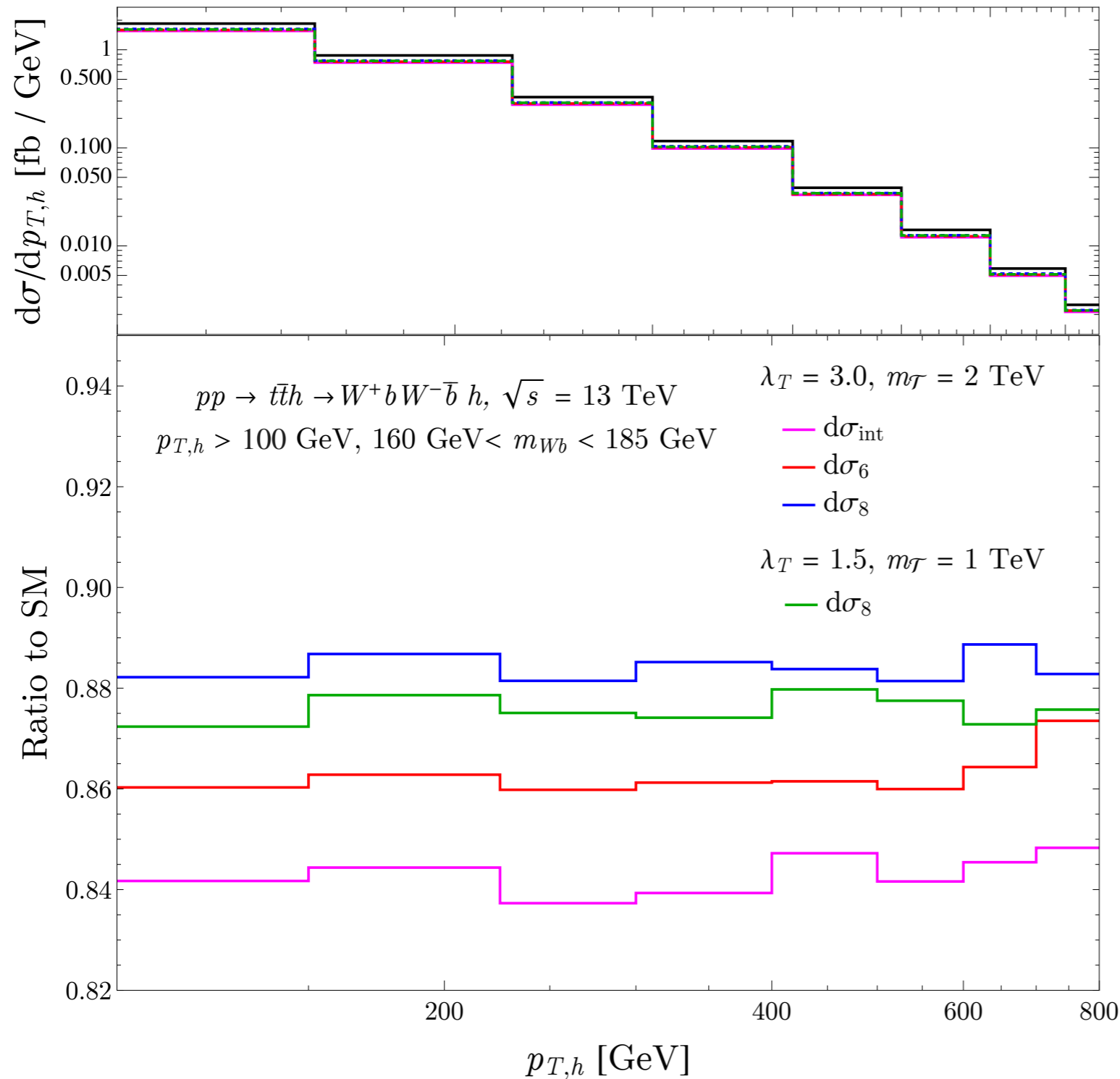
arXiv:2110.06948, Dawson, SH, Sullivan



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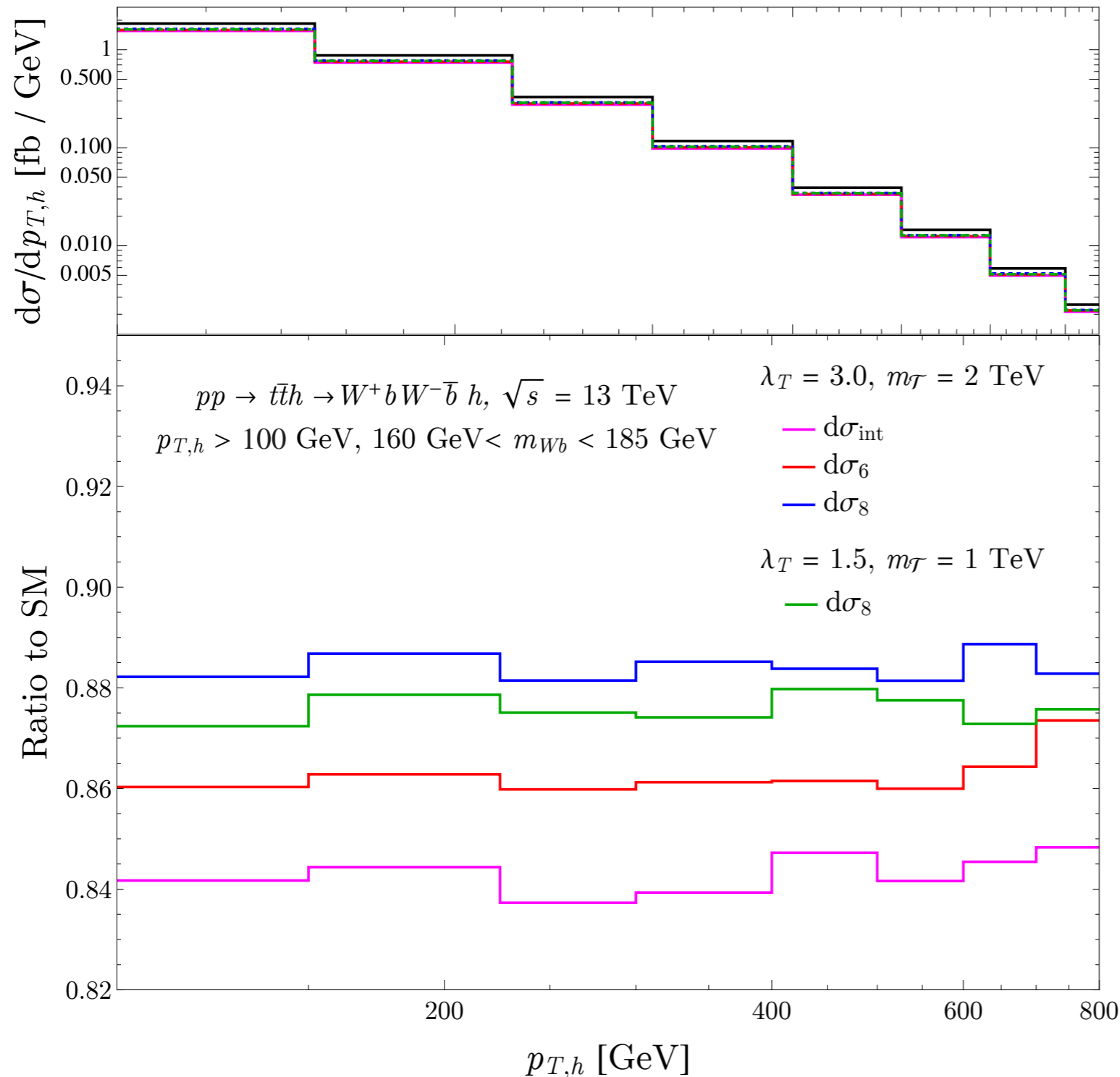
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Momentum-dependent effects from non-factorizable contributions — somewhat washed out at dim-8



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arXiv:2110.06948, Dawson, SH, Sullivan



Most significant effect is rescaling of top Yukawa (but *not* a universal effect!)

Momentum-dependent effects from non-factorizable contributions — somewhat washed out at dim-8

Dim-8 Effects sensitive to mass, independently of coupling (mixing angle!)

# Dim-8 Terms in $t\bar{t}h$ production: Summary

arXiv:2110.06948, Dawson, SH, Sullivan

Several apparent effects from matching up to dimension-8 in this model:

- Higher order terms can have different scalings in coupling/mass — interesting interplay with decoupling limit
- New vertices with different particles, momentum structure that didn't exist at dimension-6 — can lead to kinematic effects
- Effects are *small* —  $\mathcal{O}(1\%)$  for allowed parameters — but this model is too simple!

More complicated models may lead to larger effects, particularly if there is interplay with the EW input parameters?  
(see e.g., 2102.02819 in context of EWPO)

# Example 2: The 2HDM

arXiv:2205.01561, Dawson, Fontes, SH, Sullivan

Assume two scalar doublets,  $\Phi_1$ ,  $\Phi_2$  distinguished by a softly broken  $Z_2$  symmetry,  $\Phi_2 \rightarrow -\Phi_2$ .

Extend to fermions to avoid FCNCs, leads four types of 2HDMs (I, II, L, and F)

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Extend to fermions to avoid FCNCs, leads four types of 2HDMs (I, II, L, and F)

Useful to work in the *Higgs basis*, denoted  $H_1$ ,  $H_2$  defined by  $\langle H_1 \rangle = v/\sqrt{2}$ ,  $\langle H_2 \rangle = 0$

$$\begin{pmatrix} H_1 \\ H_2 \end{pmatrix} = \begin{pmatrix} \cos \beta & \sin \beta \\ -\sin \beta & \cos \beta \end{pmatrix} \begin{pmatrix} \Phi_1 \\ \Phi_2 \end{pmatrix}$$

A second mixing angle  $\alpha$ , puts  $h_{125}$  into  $H_1$

# Example 2: The 2HDM

arXiv:2205.01561, Dawson, Fontes, SH, Sullivan

For each type, Higgs coupling deviations can be written in terms of  $\tan \beta$ ,  $\cos(\beta - \alpha)$ . E.g., for Type-II:

$$\kappa_u = \sin(\beta - \alpha) + \frac{\cos(\beta - \alpha)}{\tan \beta}$$

$$\kappa_d = \sin(\beta - \alpha) - \tan \beta \cos(\beta - \alpha)$$

$$\kappa_\ell = \sin(\beta - \alpha) - \tan \beta \cos(\beta - \alpha)$$

$$\kappa_V = \sin(\beta - \alpha)$$

$\implies$  all approach 1 as  $\cos(\beta - \alpha) \rightarrow 0$

Alignment parameter tells us how “SM-like” the 125-GeV Higgs is

# Matching to Dimension-6

The matching at dimension-6 is well known. Ignoring light flavor, there are four operators generated:

$$\mathcal{O}_H = (H^\dagger H)^3, \quad \frac{v^2}{\Lambda^2} C_H = \frac{\Lambda^2}{v^2} \cos^2(\beta - \alpha)$$

$$\mathcal{O}_{bH} = (H^\dagger H)(\bar{Q}_3 b_R H), \quad \frac{v^2}{\Lambda^2} C_{bH} = -y_b \eta_b \frac{\cos(\beta - \alpha)}{\tan \beta}$$

$$\mathcal{O}_{tH} = (H^\dagger H)(\bar{Q}_3 t_R \tilde{H}), \quad \frac{v^2}{\Lambda^2} C_{bH} = -y_t \eta_t \frac{\cos(\beta - \alpha)}{\tan \beta}$$

$$\mathcal{O}_{\tau H} = (H^\dagger H)(\bar{L}_3 \tau_R \tilde{H}), \quad \frac{v^2}{\Lambda^2} C_{\tau H} = -y_\tau \eta_\tau \frac{\cos(\beta - \alpha)}{\tan \beta}$$

	$\eta_t$	$\eta_b$	$\eta_\tau$
Type-I	1	1	1
Type-II	1	$-\tan^2 \beta$	$-\tan^2 \beta$
Lepton-specific	1	1	$-\tan^2 \beta$
Flipped	1	$-\tan^2 \beta$	1

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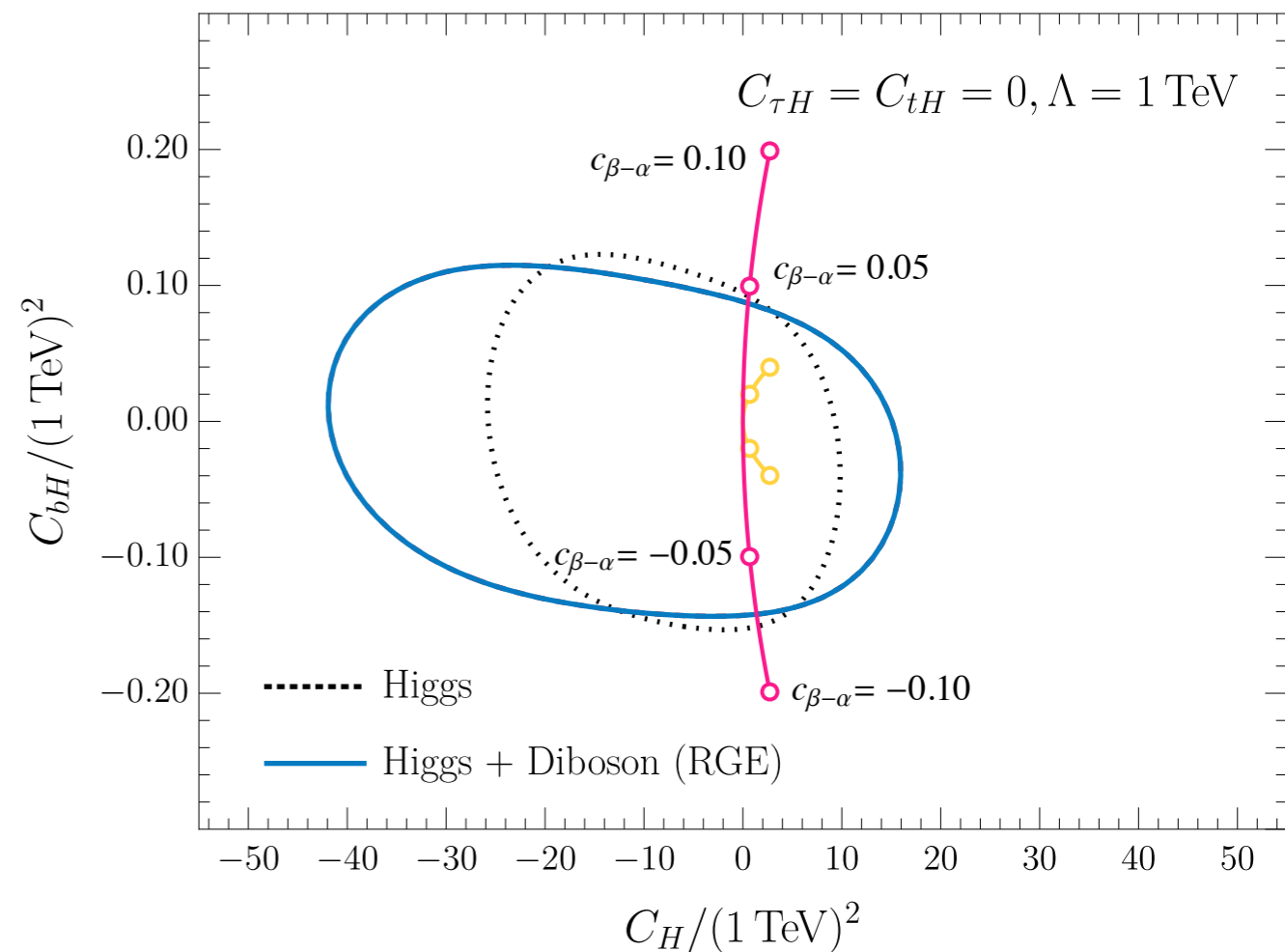
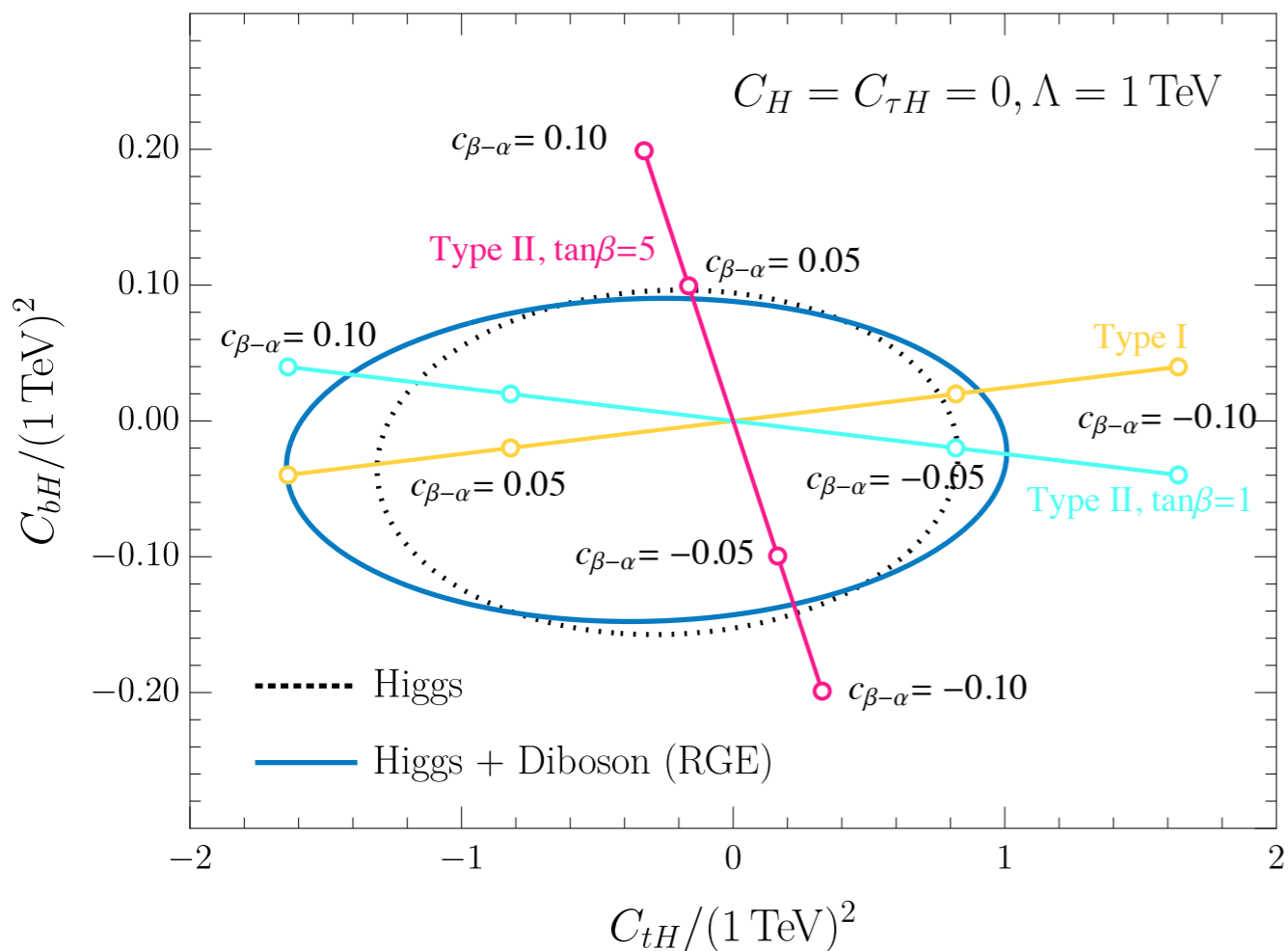
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Requiring all the additional states to lie at a common high scale enforces the “decoupling limit”:

$$\cos(\beta - \alpha) \sim \frac{v^2}{\Lambda^2} \ll 1$$

# Matching to Dimension-6

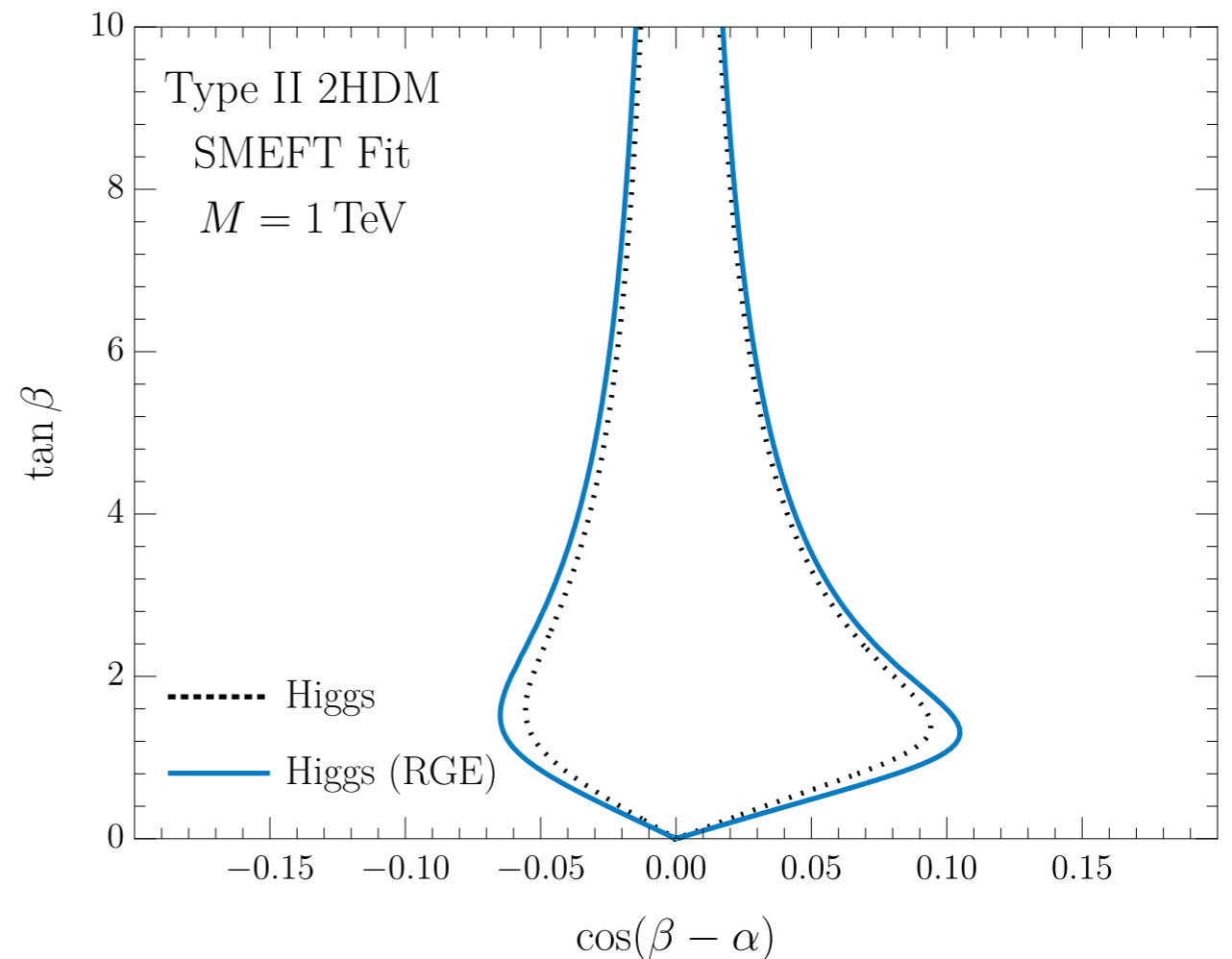
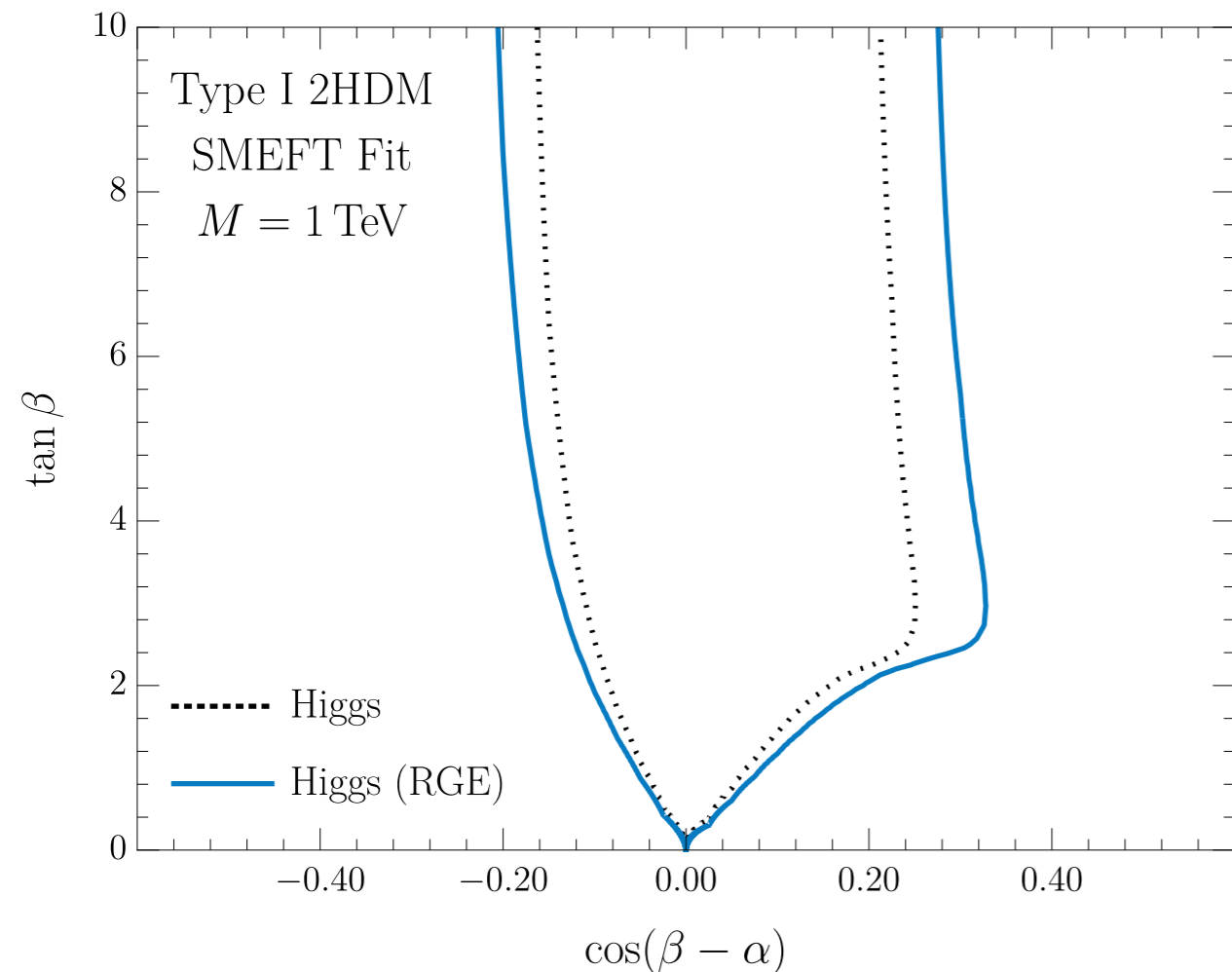


Different types of 2HDM sweep out different ranges of allowed coefficients



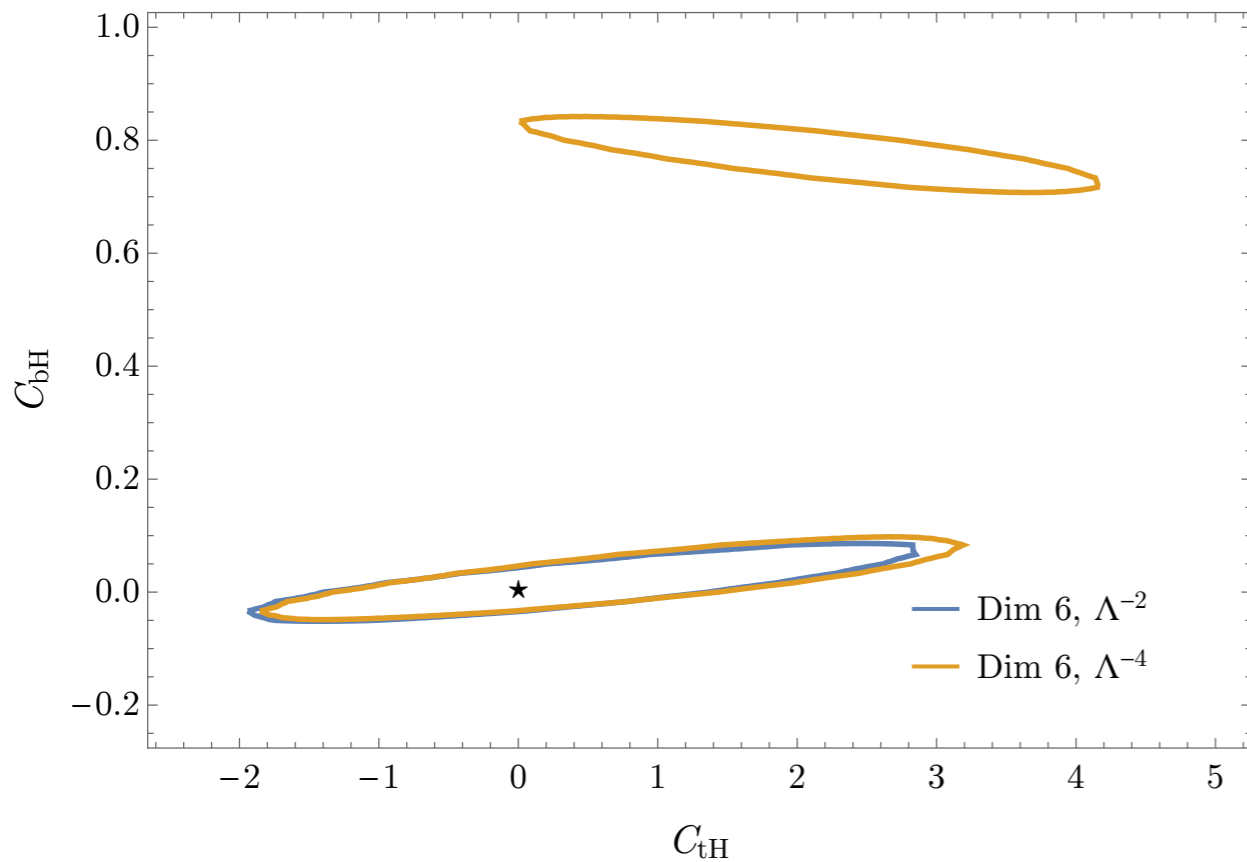
# Matching to Dimension-6

For a given type of 2HDM, easy to translate into the  $\tan \beta, \cos(\beta - \alpha)$  plane



Effects of RGE are relatively small  
(logarithmic effects on Higgs couplings)

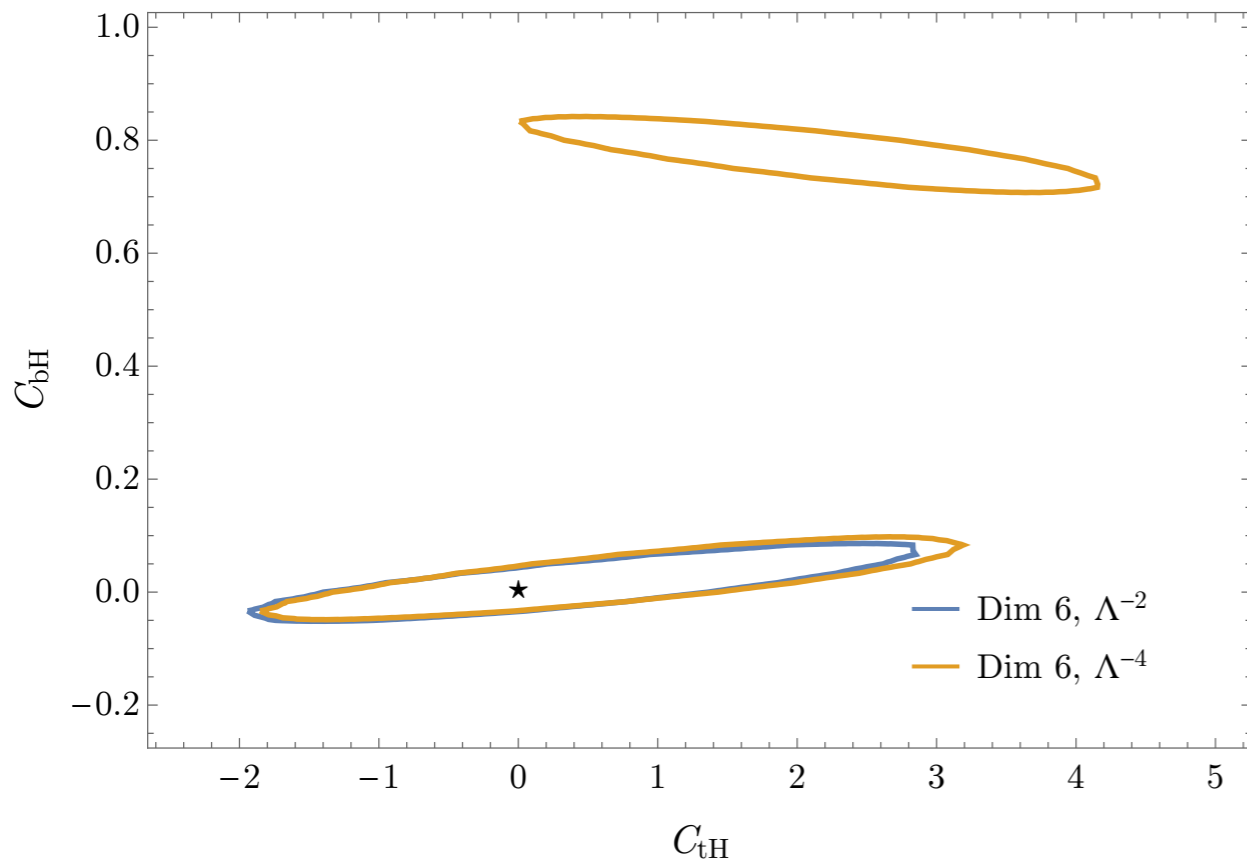
# Effects at Large $\tan \beta$



There is a second minimum where the bottom Yukawa has the opposite sign

The well-known “wrong-sign” region of the Type-II 2HDM

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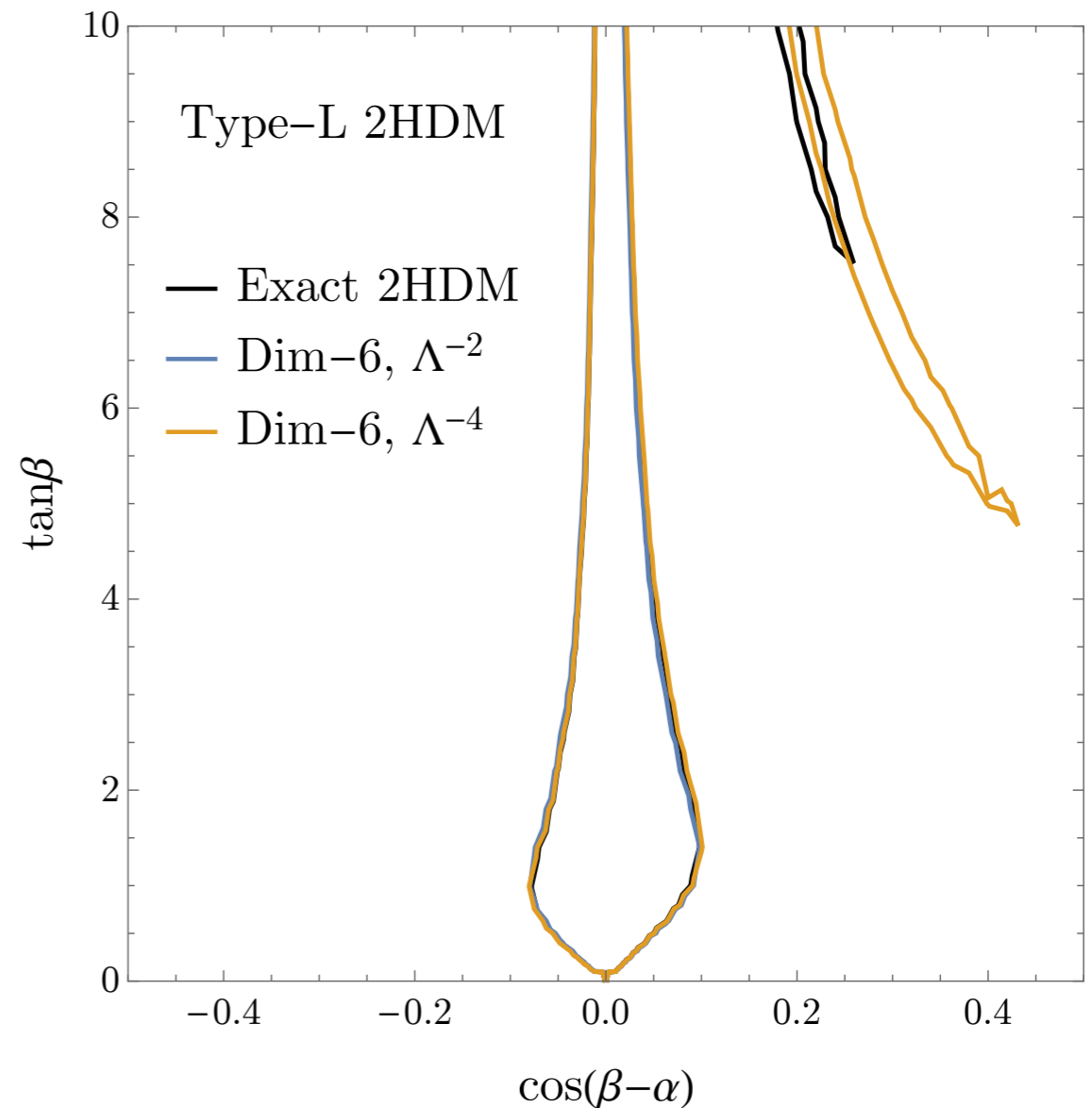


Actually ruled out for Type-II by latest Higgs data, but appears still in e.g., Type-L:

But only if we include  $\mathcal{O}(\Lambda^{-4})$  terms!

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The well-known “wrong-sign” region of the Type-II 2HDM



# Effects at Large $\tan \beta$

In the type-I 2HDM, all of the fermionic operators scale like:

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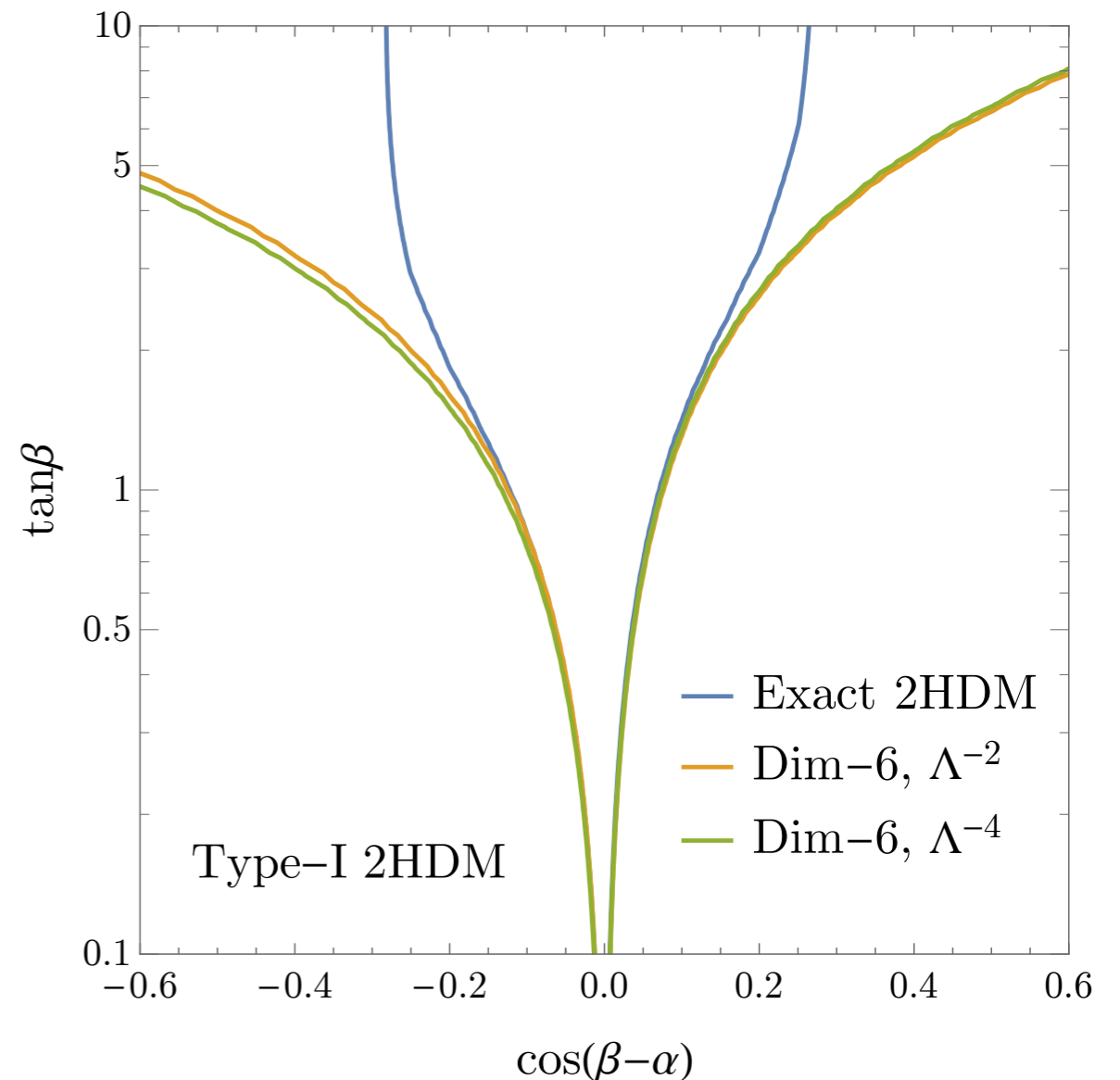
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Ignoring the constraints on  $C_H$ , we see the dimension-6 description fails (see e.g., [1611.01112])

⇒ need to include gauge couplings! (Dimension-8)

For large  $\tan \beta$ , approaches the SM!



# $\lambda_{hhh}$ Constraints are Important!

At dimension-6, the leading constraints for large  $\tan \beta$  come from information about the Higgs self coupling encoded in  $C_H$

Use indirect bounds from single-Higgs measurements based on [arXiv:1607.04251]

(Degrassi, Di Micco, Giardino, Rossi).

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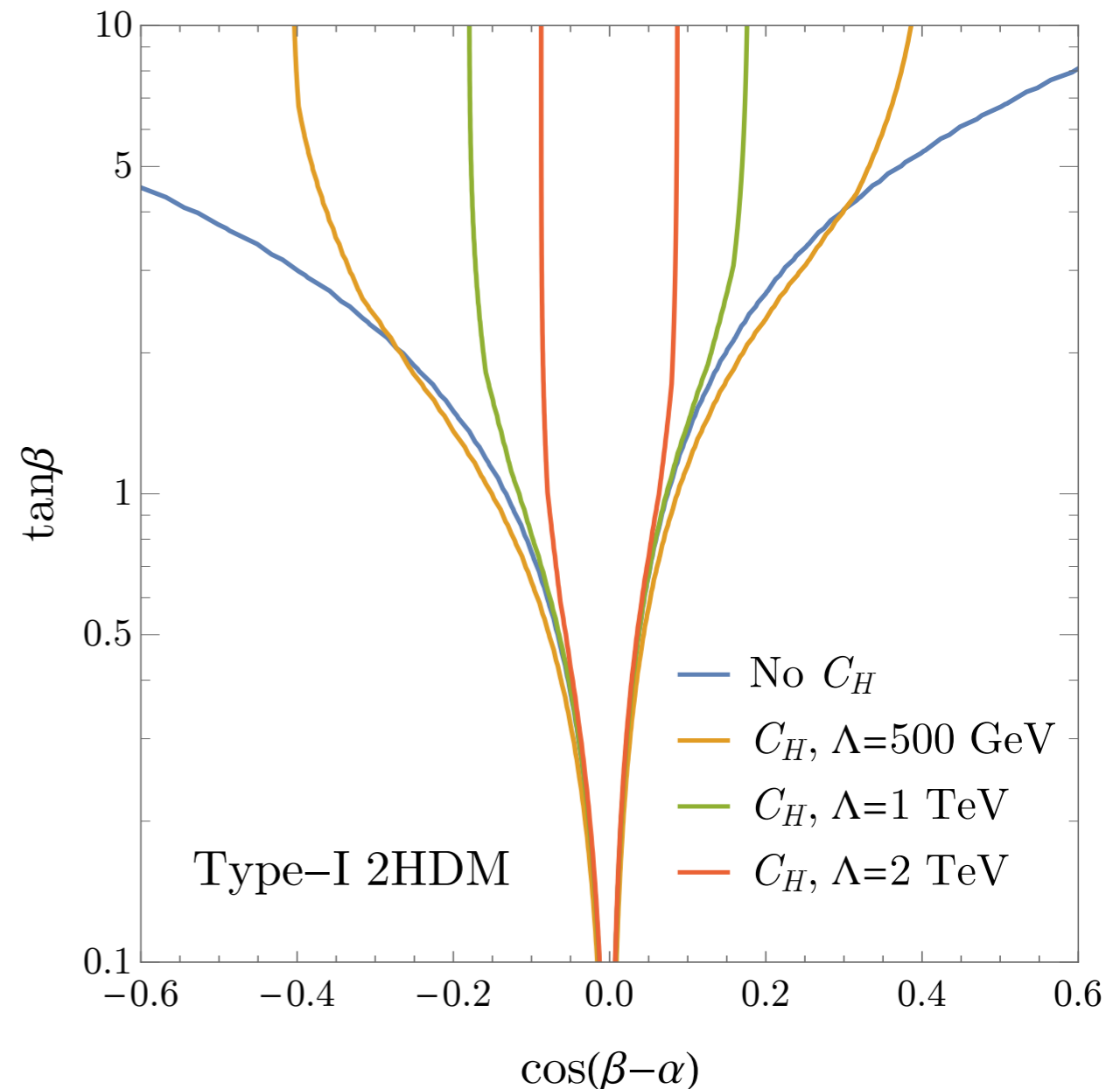
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Gauge coupling modifications make it clear matching to dimension-8 is important.

Perform complete matching of the 2HDM to dimension-8, and write operators in terms of “Murphy basis” in [2005.00059]

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$$(D_\mu H^\dagger D^\mu H)(\bar{q}u\tilde{H}), \quad (D_\mu H^\dagger \tau^I D^\mu H)(\bar{q}u\tau^I \tilde{H}), \quad (D_\mu H^\dagger H)(\bar{q}uD^\mu \tilde{H})$$
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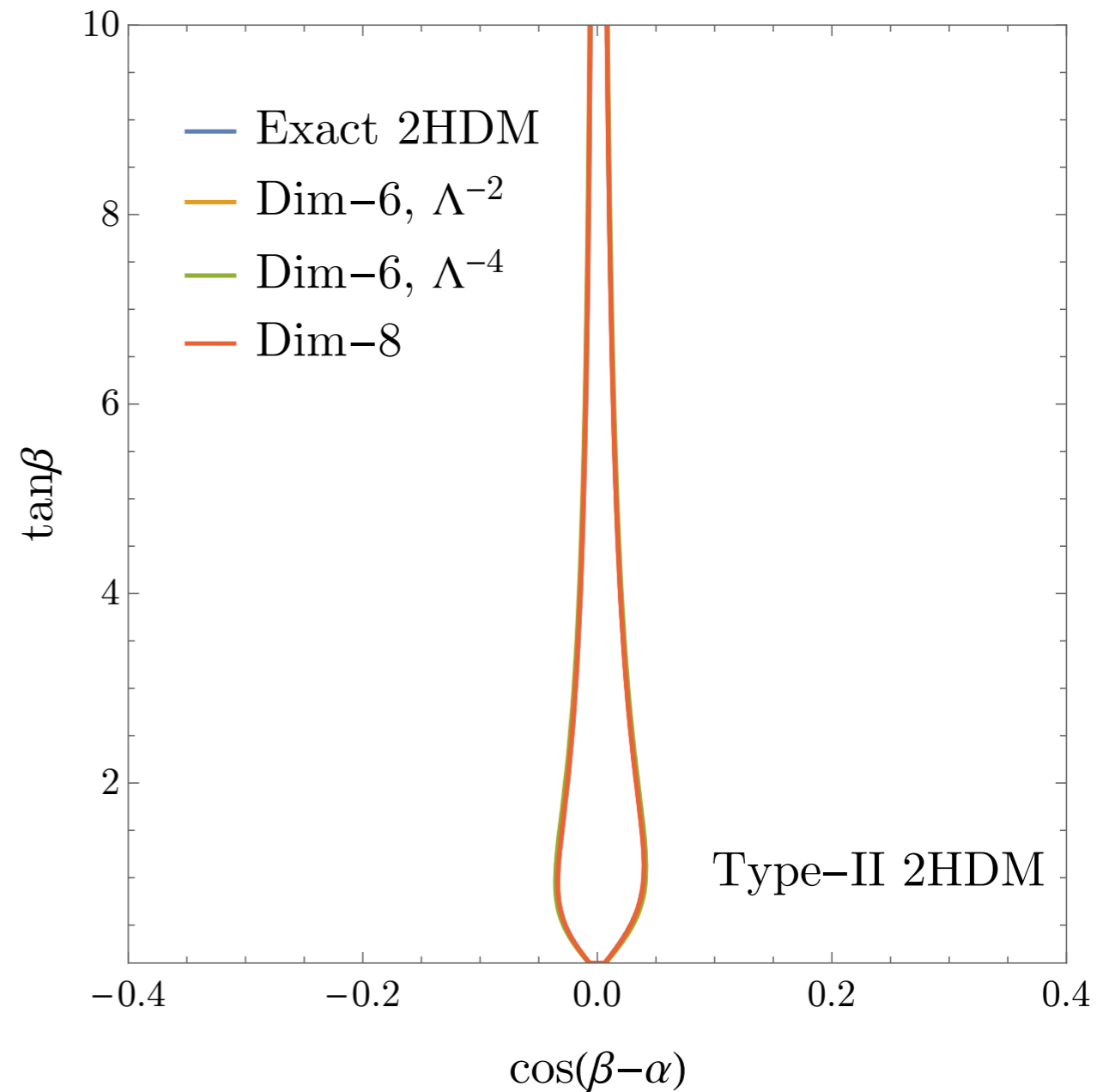
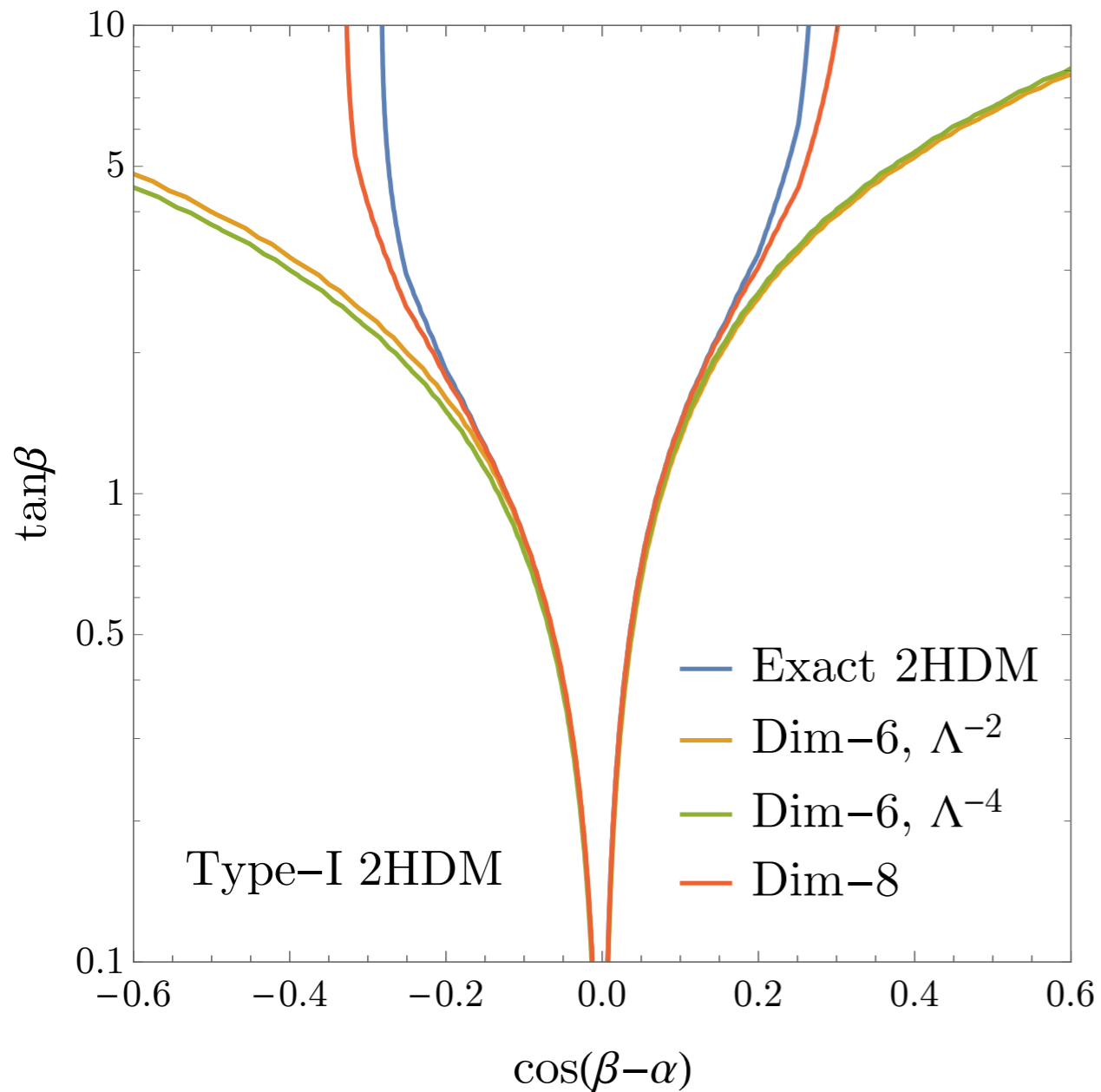
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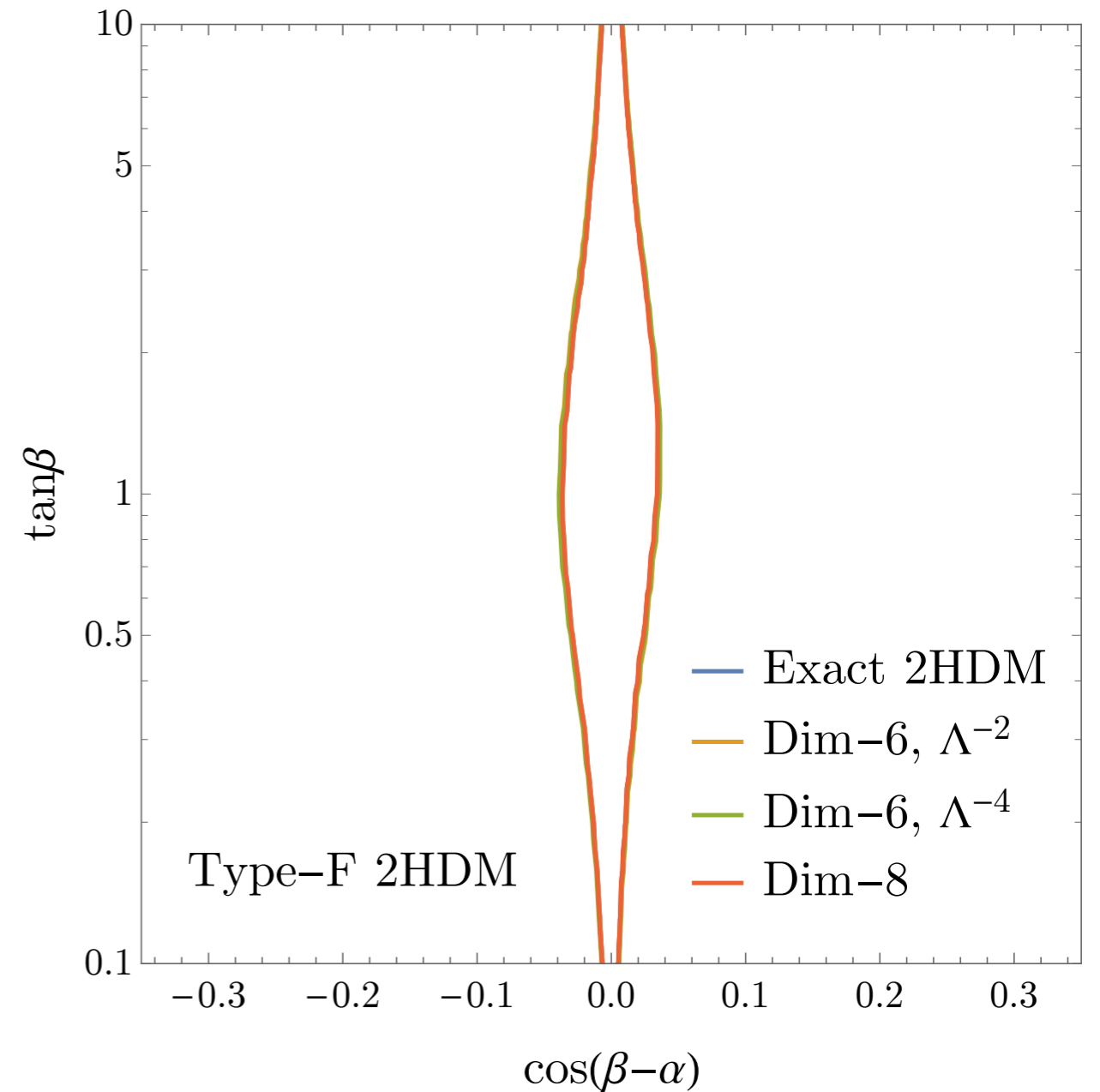
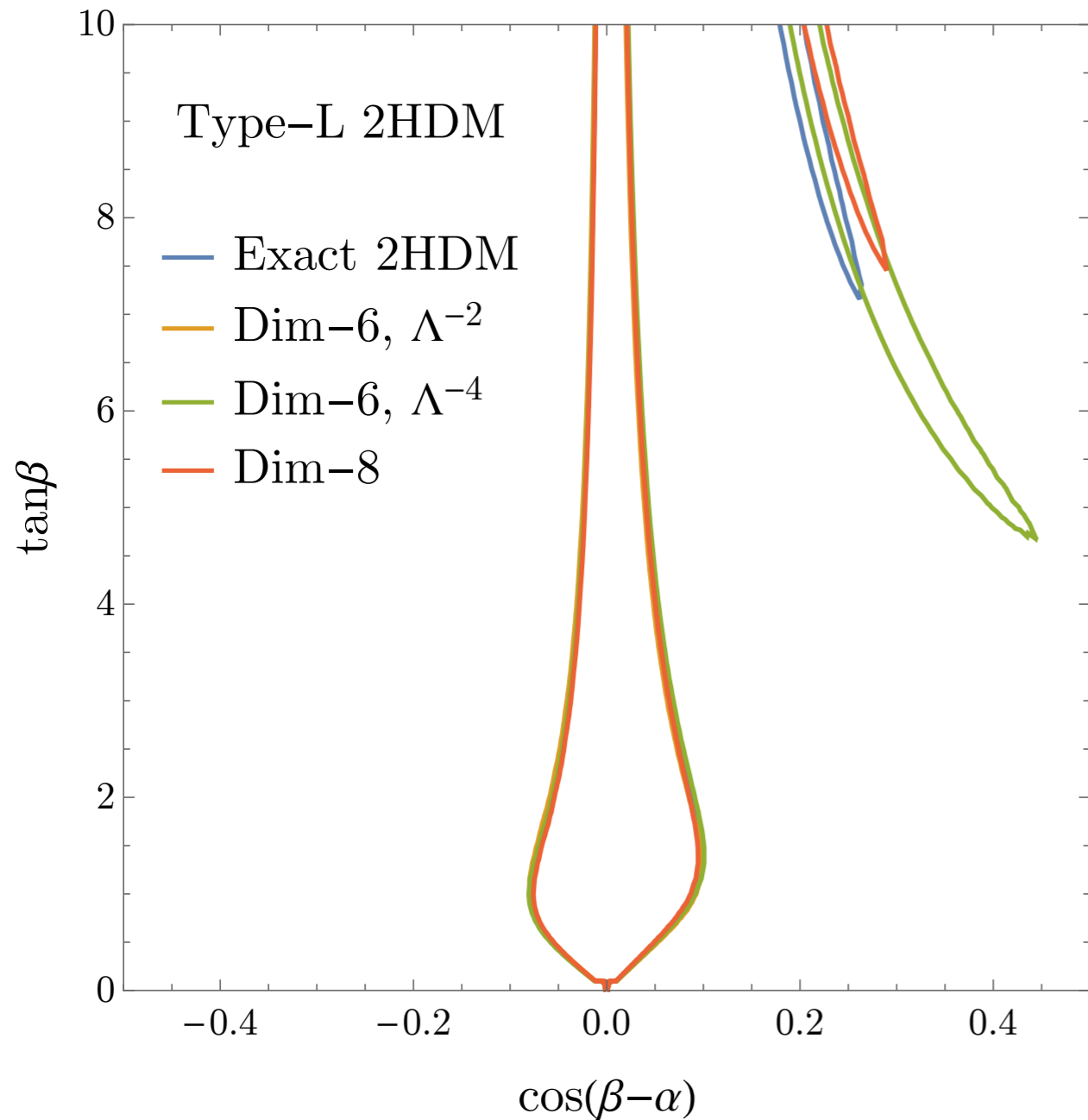
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$$\mathcal{O}_{H^6}^{(1)} = (H^\dagger H)^2 (D_\mu H)^\dagger (D^\mu H), \quad C_{H^6}^{(1)} = -\frac{\Lambda^4}{v^4} \cos(\beta - \alpha)^2$$

# Fit Results Including Dimension-8



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# EFT of the 2HDM Summary

arXiv:2205.01561, Dawson, Fontes, SH, Sullivan

Rich structure of the 2HDM leads to interesting effects when interpreting SMEFT results:

- SMEFT formally valid only in the “alignment-limit”, requires light scales for large mixing angles
- “Wrong-sign” regions require going beyond  $\mathcal{O}(\Lambda^{-2})$
- Gauge couplings only appear at dimension-8
- Self-coupling effects introduce a dependence on the heavy scale

# Example 3: The Singlet Model

arXiv:2102.02823, Dawson, Giardino, SH



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Simplest extension to the SM — only one additional state

Ideal test case for investigating details of matching procedure

- theoretical constraints well understood
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(Jiang et al., 1811.08878, Haisch et al., 2003.05936)

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(Jiang et al., 1811.08878, Haisch et al., 2003.05936)

$$C_i(\mu_R) = c_i(M) + \frac{1}{16\pi^2} d_i(M) + \frac{1}{32\pi^2} \gamma_{ij} c_j(M) \log \left( \frac{\mu_R^2}{M^2} \right)$$

Goal: understand numerical importance of 1-loop matching effects in the context of the singlet model

# The Singlet Model

$$V(\Phi, S) = -\mu_H^2 \Phi^\dagger \Phi + \lambda_H (\Phi^\dagger \Phi)^2 + \frac{1}{2} m_\xi \Phi^\dagger \Phi S + \frac{1}{2} \kappa \Phi^\dagger \Phi S^2 \\ + t_S S + \frac{1}{2} M^2 S^2 + \frac{1}{3} m_\zeta S^3 + \frac{1}{4} \lambda_S S^4$$

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In  $Z_2$  non-symmetric case, use shift symmetry to set  $v_S \rightarrow 0$

Physical states:

Masses  $m_h = 125$  GeV,  $M_H$

$$h = \cos \theta \Phi_0 + \sin \theta S$$

Other physical parameters:

$$H = -\sin \theta \Phi_0 + \cos \theta S$$

$$\sin \theta, \kappa, m_\zeta, \lambda_S$$

Higgs couplings universally suppressed by  $\cos \theta$

# Unitarity and Vacuum Stability

The physical parameters are not entirely arbitrary!

Unitarity of the  $hh$ ,  $hH$ ,  $HH$  amplitudes requires:

$$M_H^2 \sin^2 \theta \lesssim \frac{16\pi}{3} v^2 - m_h^2 \cos^2 \theta$$

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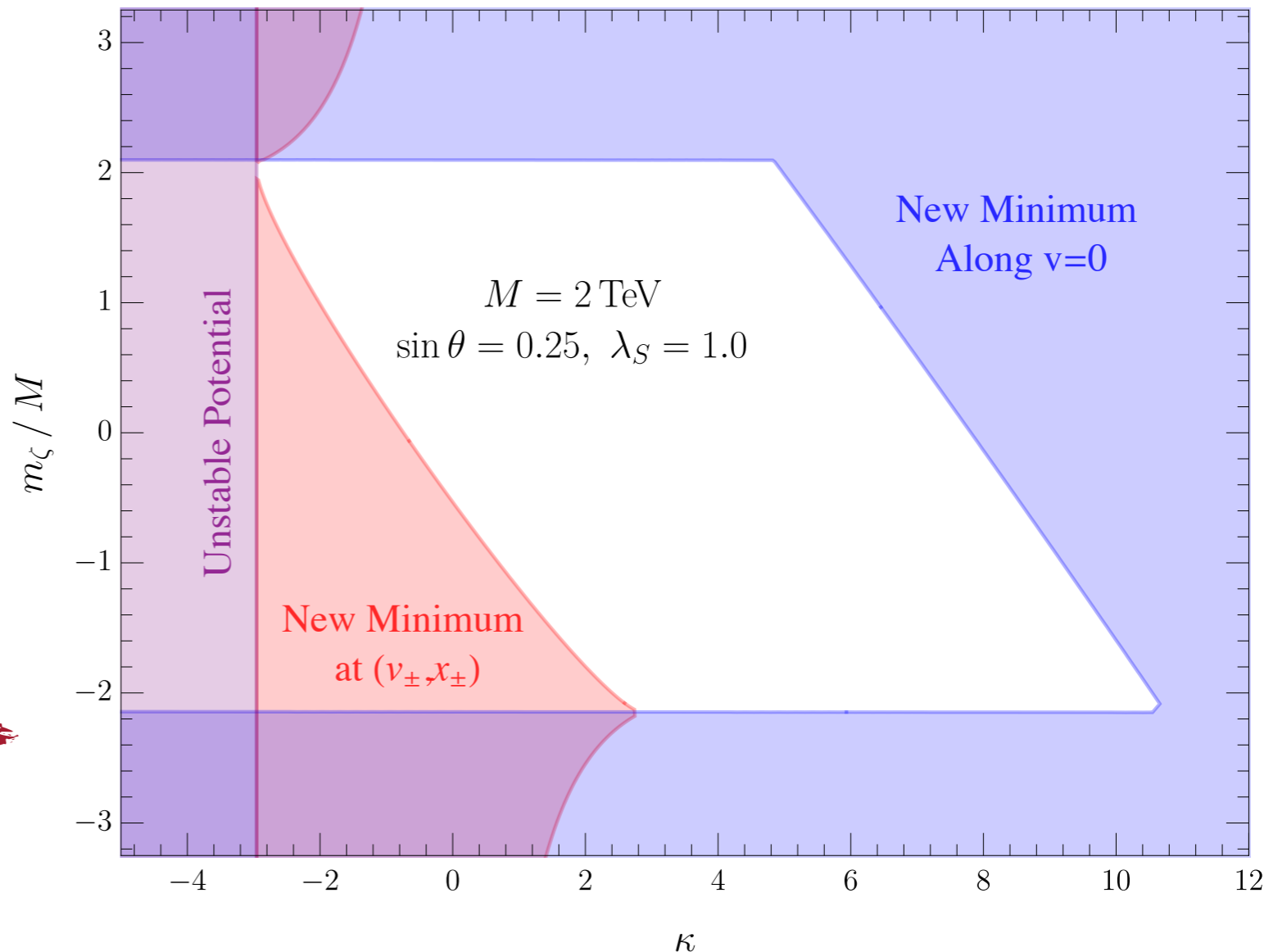
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$$|\kappa| \lesssim 8\pi$$

Furthermore, have to demand that the EWSB minimum be the global minimum of the potential



# Singlet Matching to SMEFT

Two coefficients are generated at tree-level:

$$c_{H\Box} = -\frac{m_\xi^2}{8M^2}$$

$$c_H = \frac{m_\xi^2}{8M^2} \left( \frac{m_\xi m_\zeta}{3M^2} - \kappa \right)$$

Perform matching at the scale  $M$ , related to the physical mass via

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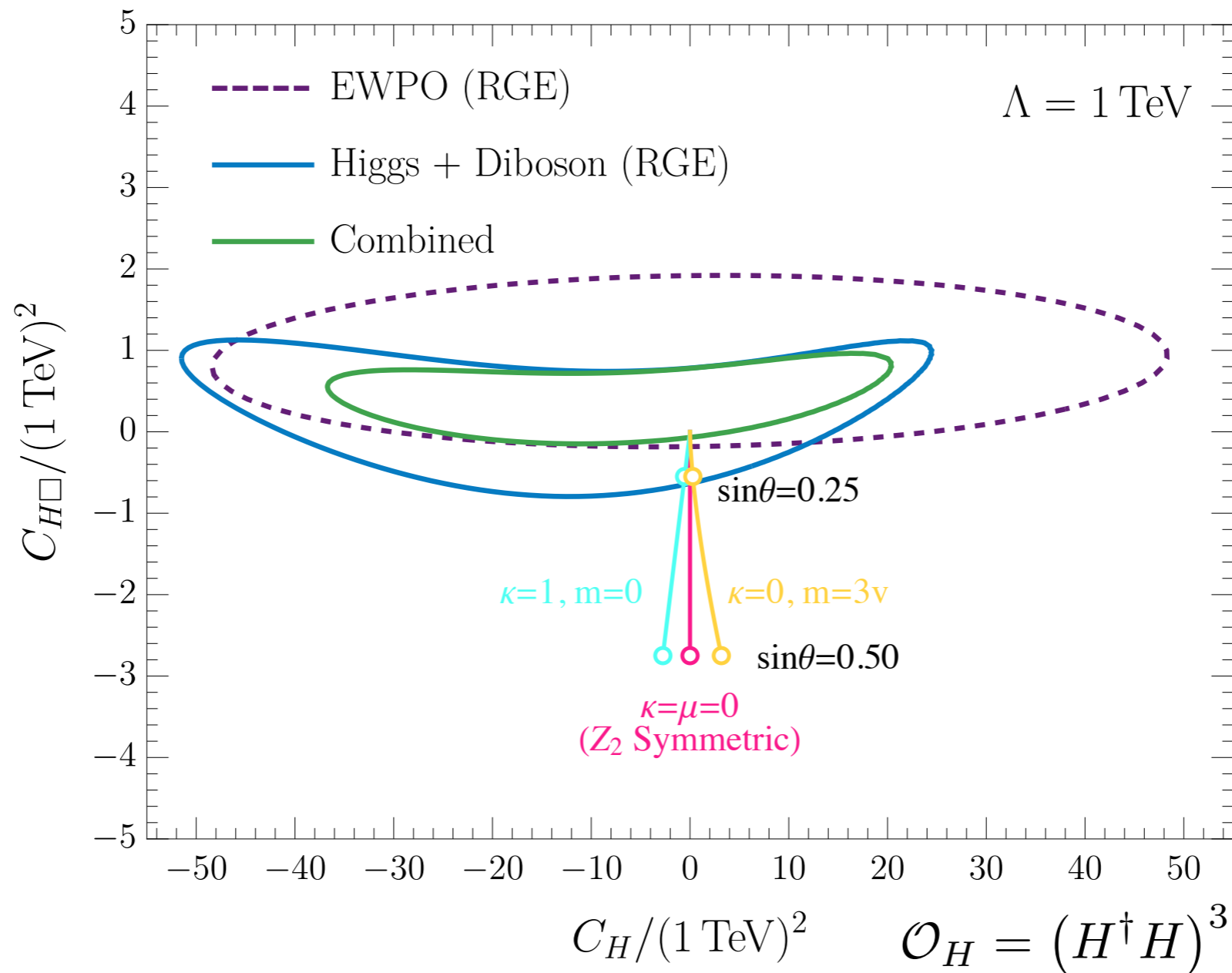
These operators introduce

$$C_{HD}, C_{tH}, C_{bH}, C_{\tau H}, C_{Hl}^{(3)}, C_{Hq}^{(3)}, C_{Htb}$$

at the weak scale from RG running

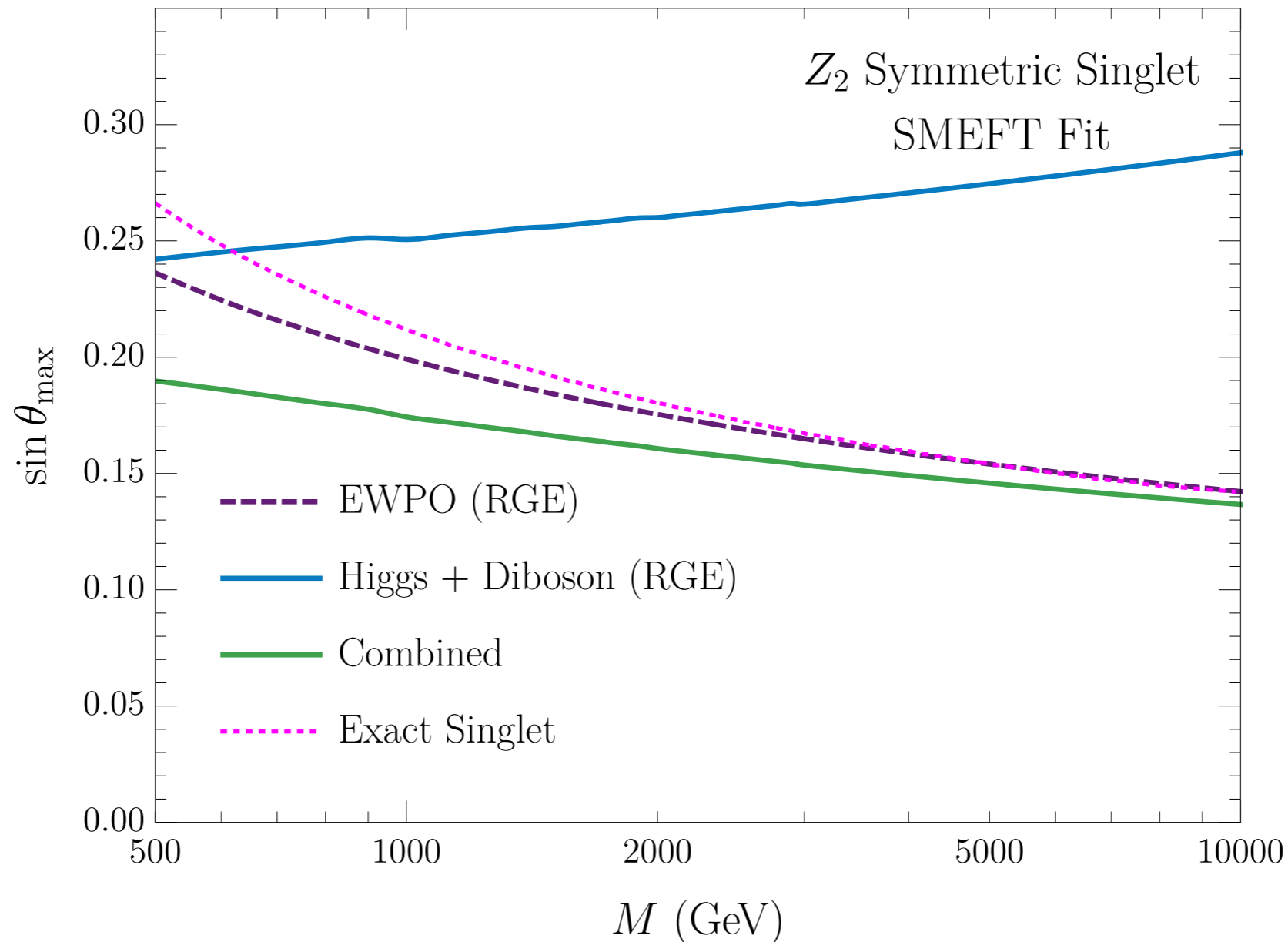


# Tree Level (+RGE) Results



Limits on the singlet from EWPO and LHC competitive — but most allowed coefficients cannot be generated in the model

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# One-Loop Matching

Jiang, Craig, Li, Sutherland [1811.08878],

Haisch, Ruhdorfer, Salvioni, Venturini, Weiler [2003.05936]

New contributions to  $C_H$ ,  $C_{H\Box}$  at the matching scale...

$$d_{H\Box} = -\frac{9}{2}\lambda c_{H\Box} + \frac{31}{36}(3g^2 + g'^2)c_{H\Box} + \frac{3}{2}c_H + \delta d_H + \delta d_{H\Box}^{\text{shift}}$$

$$d_H = \lambda \left[ \frac{1}{9}(62g^2 - 336\lambda)c_{H\Box} + 6c_H \right] + \delta d_H + \delta d_H^{\text{shift}}$$

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...as well as many operators that don't appear at tree-level

$$C_{HD}, C_{HW}, C_{HB}, C_{HWB}, C_{Hu}, C_{Hd},$$

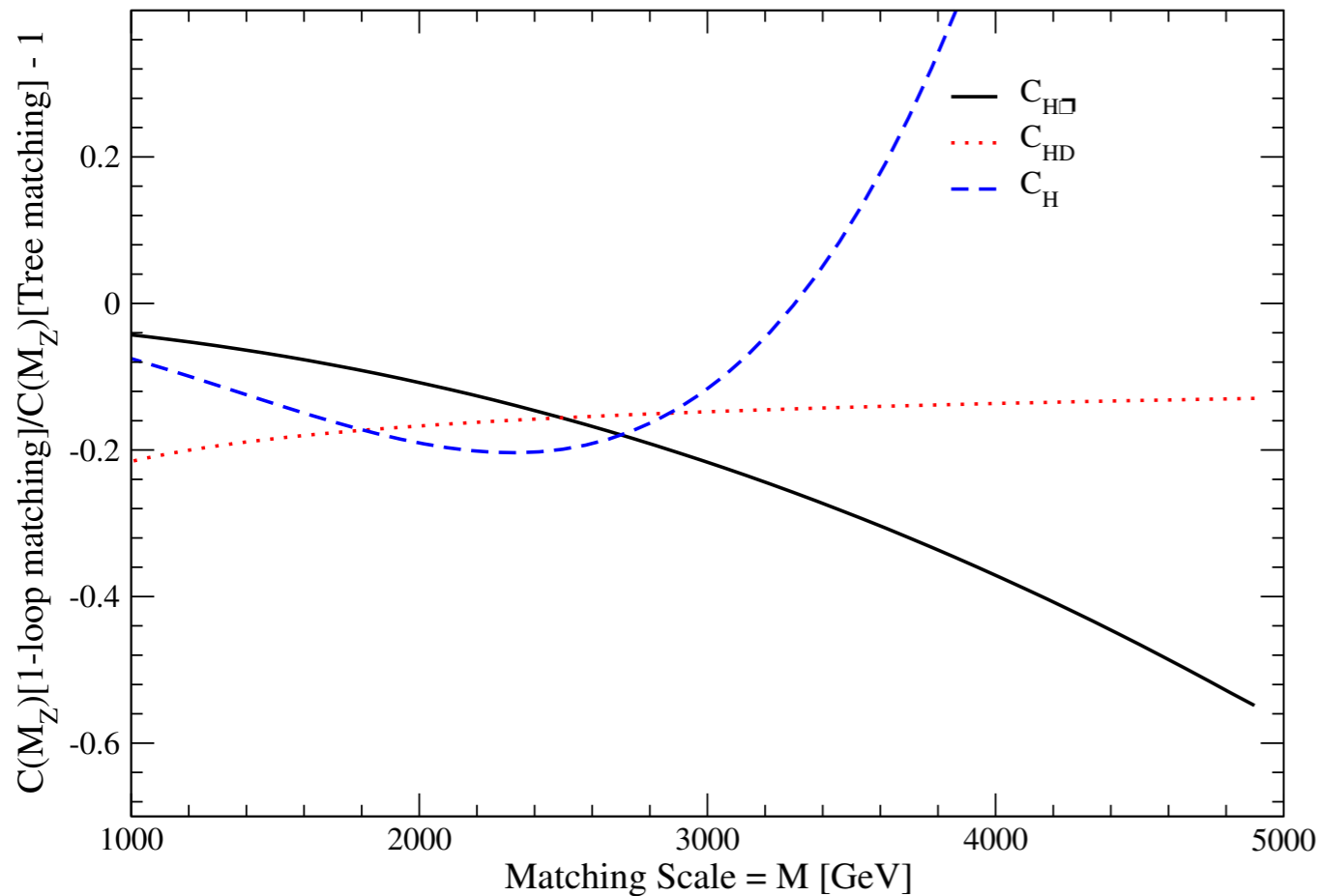
$$C_{Hq}^{(1)}, C_{Hq}^{(3)}, C_{Hl}^{(3)}, C_{tH}$$

**In principle of comparable size to RGE-induced contribution!**

# One-Loop Matching

SMEFT Limit of Singlet Model

$\cos \theta = .98, \kappa = .5, m_\zeta = M/4, \lambda_s = .03$



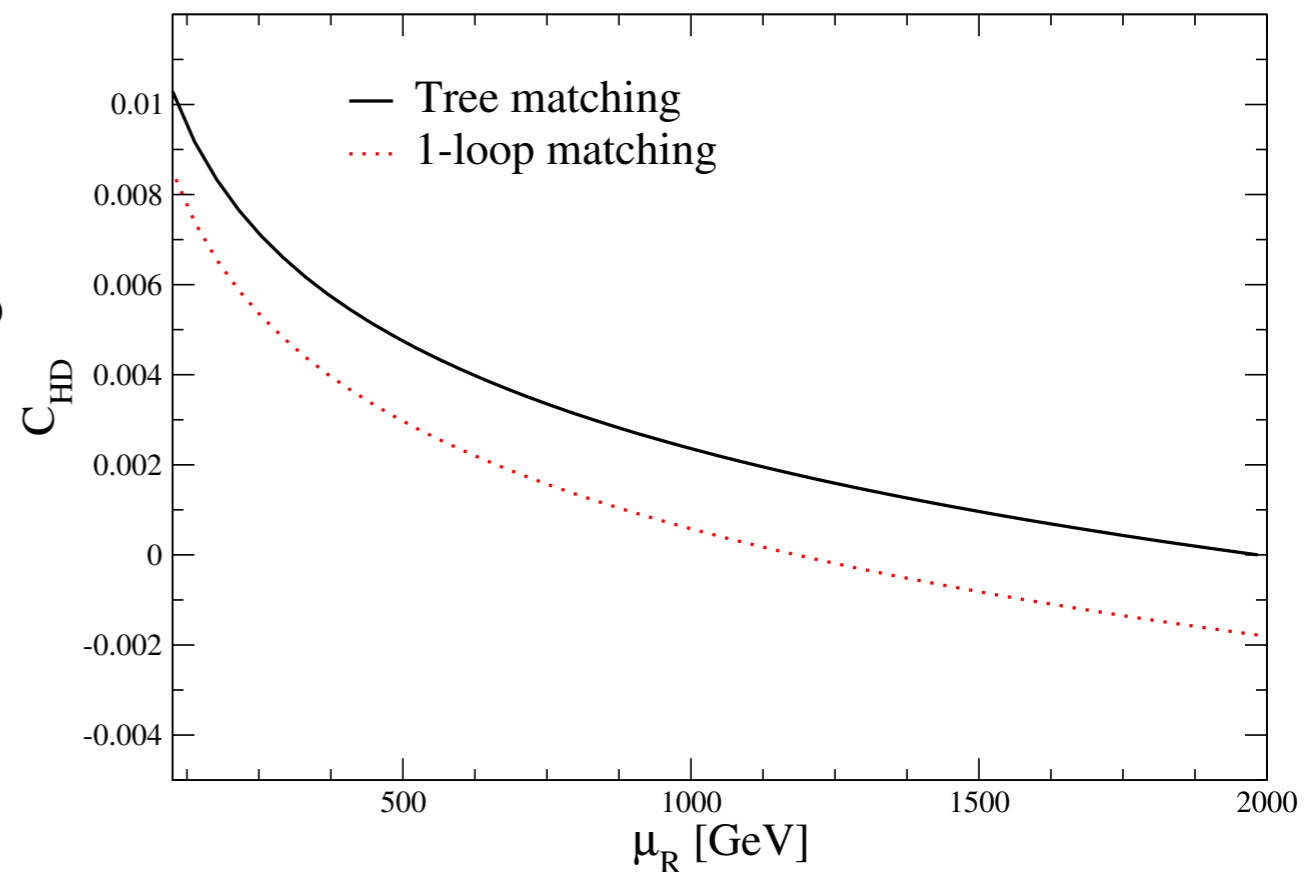
One-loop matching changes operators by  $\sim 10\text{-}20\%$  as measured at the weak scale

Include only one-loop RGEs

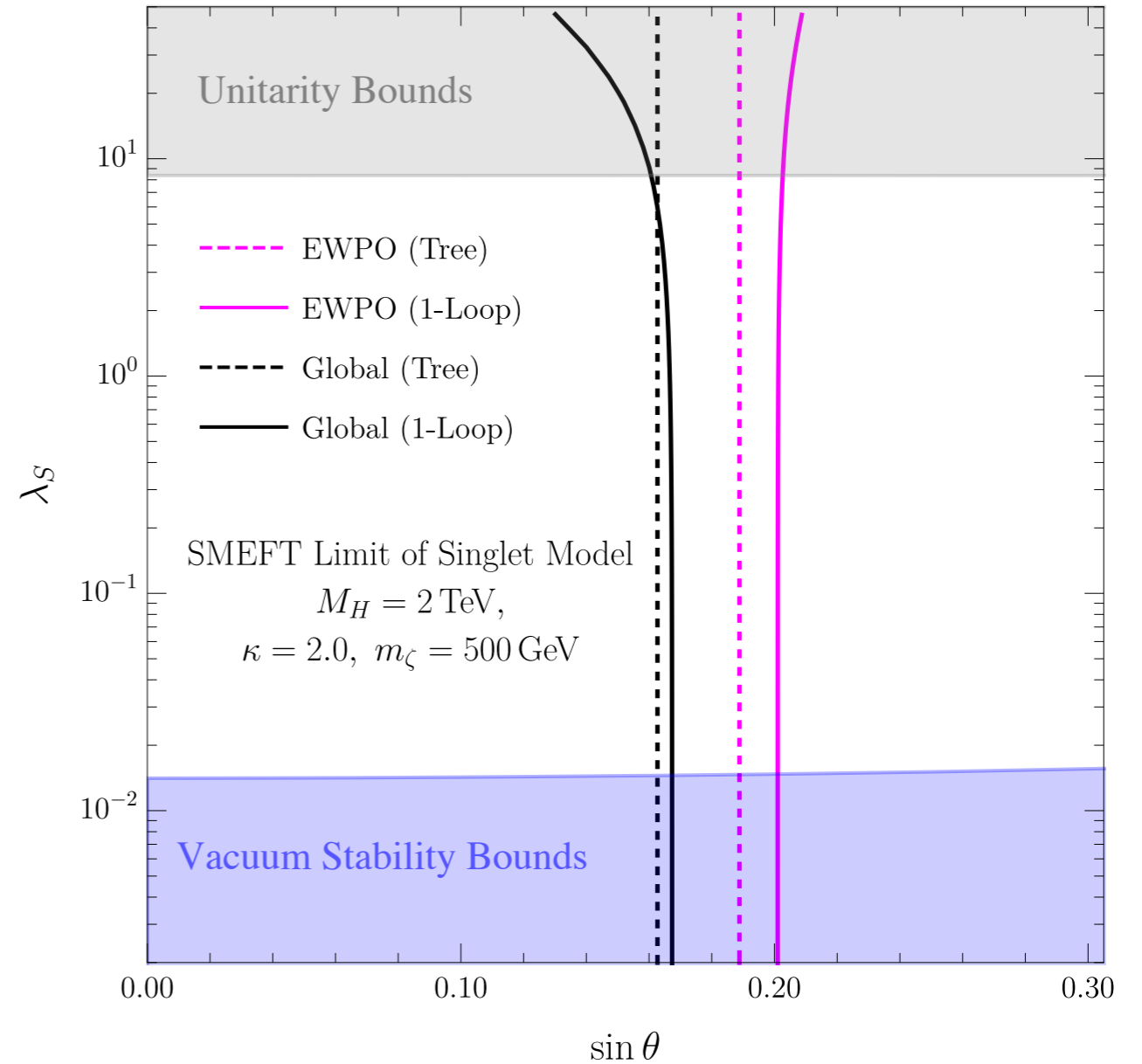
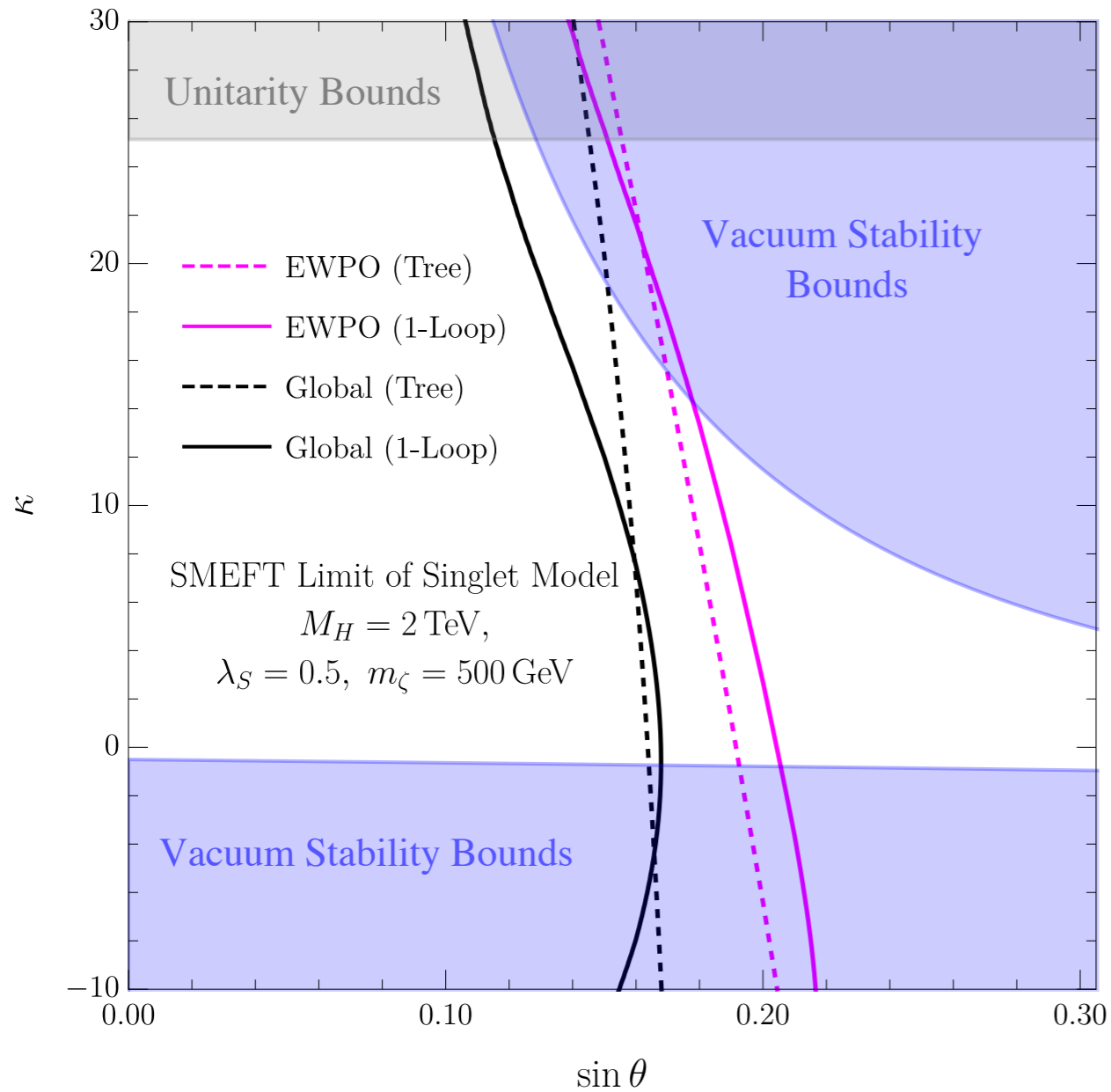
(two loops unavailable, but necessary to run one-loop induced operators)

SMEFT Limit of Singlet Model

$M_H = 2 \text{ TeV}, \cos \theta = .99, \kappa = -.5, m_\zeta = 500 \text{ GeV}, \lambda_s = .03$

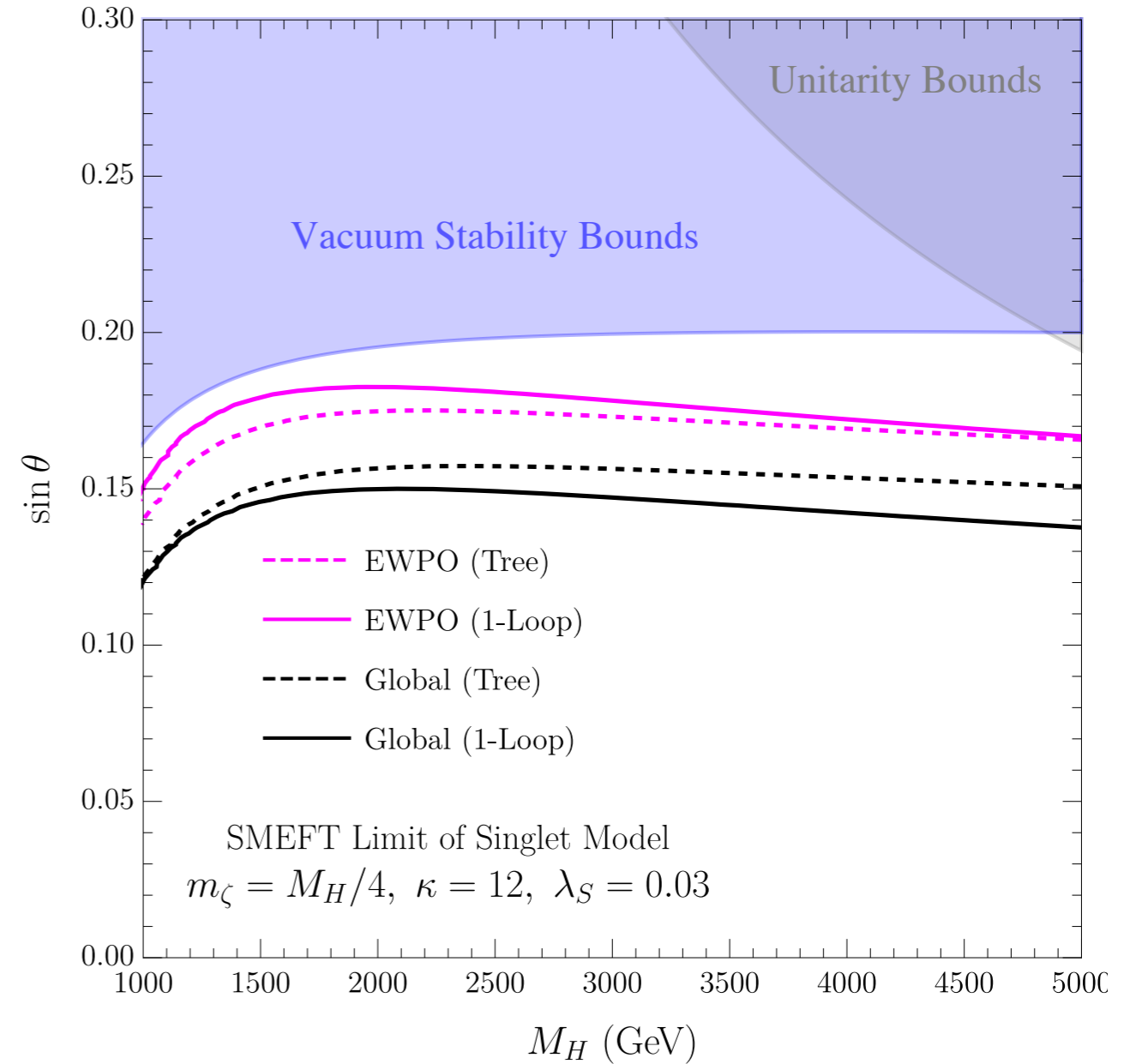
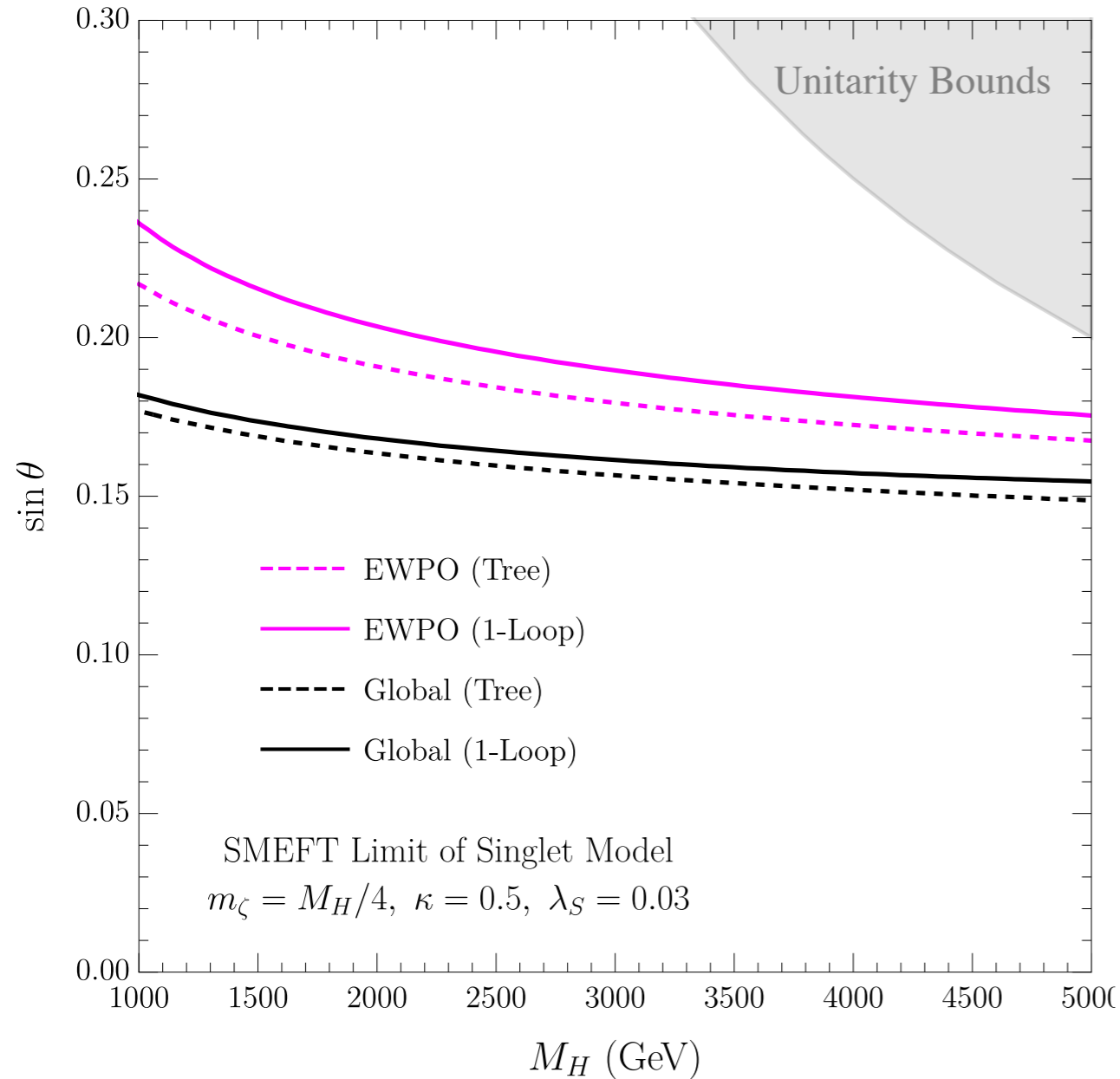


# Effects on the Fit



Effects mostly  $O(10\%)$ , except for large values of portal coupling

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# Conclusions

- SMEFT Fits may be the “legacy” measurements of the LHC, but important to keep UV models in mind!
- Tree level interpretations of SMEFT Fits aren’t the whole story!  
*RG evolution of coefficients is extremely important.*

Lots of other recent work on this topic!

See:

- Ellis, et al., [2012.02779]
- Das Bakshi, et al., [2012.03839]
- Marzocca, et al., [2009.01249]
- Brivio et al., [2108.01094]
- Almeida et al., [2108.04828],
- ... and others!



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- Tree level interpretations of SMEFT Fits aren’t the whole story!  
*RG evolution of coefficients is extremely important.*

- Considering explicit models lets us assess the importance of higher-order matching effects (1 loop, dim-8) in a concrete way.
- Higher order effects can change phenomenology / interpretation — what happens in even more complicated models?

Lots of other recent work on this topic!

See:

- Ellis, et al., [2012.02779]
- Das Bakshi, et al., [2012.03839]
- Marzocca, et al., [2009.01249]
- Brivio et al., [2108.01094]
- Almeida et al., [2108.04828],
- ... and others!

# Conclusions

- SMEFT Fits may be the “legacy” measurements of the LHC, but important to keep UV models in mind!
- Tree level interpretations of SMEFT Fits aren’t the whole story!  
*RG evolution of coefficients is extremely important.*
- Considering explicit models lets us assess the importance of higher-order matching effects (1 loop, dim-8) in a concrete way.
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**Thanks for your attention!**